

Занятие 1.

1. Таблица производных

Составить таблицу интегралов

2. Теорема об инвариантности.

$$\int f(x)dx = F(x) + C, \text{ то } \int f(u(x))dx = F(u(x)) + C.$$

Примеры.

$$1. \int \sin x \, d\sin(x).$$

$$2. \int \frac{d(1+x^2)}{\sqrt{1+x^2}}.$$

$$3. \int \frac{d(1+\ln x)}{\cos^2(1+\ln x)}.$$

$$4. \int (x+1)^{15} dx.$$

$$5. \int \frac{1}{(2x-3)^5} dx.$$

$$6. \int e^{\sin(x)} d\sin(x).$$

$$7. \int \frac{d(\arcsin x)}{\arcsin x}.$$

$$8. \int \sin^3 x \cos x \, dx.$$

$$9. \int x \cos x^2 dx.$$

$$10. \int e^{x^3} x^2 dx.$$

$$11. \int \frac{\sqrt{\ln x}}{x} dx.$$

$$12. \int \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$$

$$13. \int \frac{1}{x \ln x} dx.$$

$$14. \int \frac{(\operatorname{arctg} x)^2}{1+x^2} dx.$$

$$15. \int \frac{\sin 2x}{\sqrt{\cos 2x}} dx.$$

$$16. \int \frac{\sin 3x}{e^{\cos 3x}} dx$$

$$17. \int \frac{dx}{(\arcsin 3x)^3 \sqrt{1-9x^2}}.$$

$$18. \int \cos^{10} x \sin(2x) dx.$$

2. Выделение целой части

1. $\int \frac{x}{x-1} dx$. 2. $\int \frac{2x+3}{x+2} dx$. 3. $\int \frac{6+x^2}{2x^2+4} dx$.
4. $\int \frac{1+2x^2}{x^2(1+x^2)} dx$.

Дома

1. $\int \operatorname{tg} x dx$.
2. 2. $\int \operatorname{ctg} x dx$.
3. 3. $\int x \sqrt{x^2+1} dx$.
4. $\int \frac{x^2}{9+x^6} dx$
 $\int x^2 \sqrt[5]{x^3+2} dx$.
5.
6. $\int \frac{x^4 dx}{\sqrt{4-25x^{10}}}$.
7. $\int \frac{x^2}{9+3x^6} dx$.
8. $\int \frac{x}{x-3} dx$.
9. $\int \frac{3x}{2x-3} dx$
10. $\int \frac{x^2}{5+x^2} dx$.
11. $\int \frac{x^2}{1-2x^2} dx$.