

# Nonlinear Resistors

## Resistance effect in polycrystalline metallic oxide (ceramics)

Type	Physical effect	Materials
Temperature-dependent resistance (Thermistor)*		
• Negative Temperature Coefficient (NTC)	hopping-conduction in metallic oxide	spinel, e.g. $(\text{Ni,Mn})_3\text{O}_4$ $\sigma \approx 10^{-2} (\Omega\text{-m})^{-1}$
• Positive Temperature Coefficient (PTC)	grain boundary phenomena in semiconducting ferroelectrics	n-doped $\text{BaTiO}_3$ $\sigma \approx 10^2 \dots 10^3 (\Omega\text{-m})^{-1}$
Voltage-dependent resistance (Varistor)*	grain boundary phenomena in semiconducting ceramics	SiC n-doped ZnO

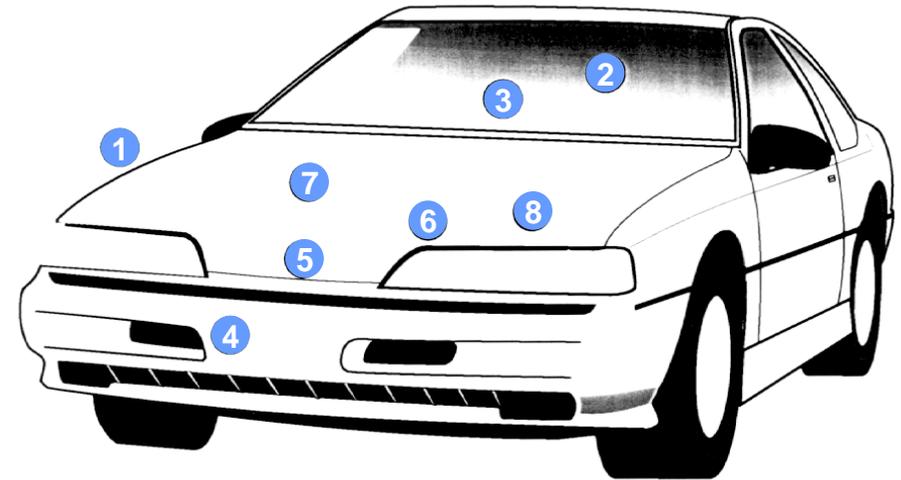
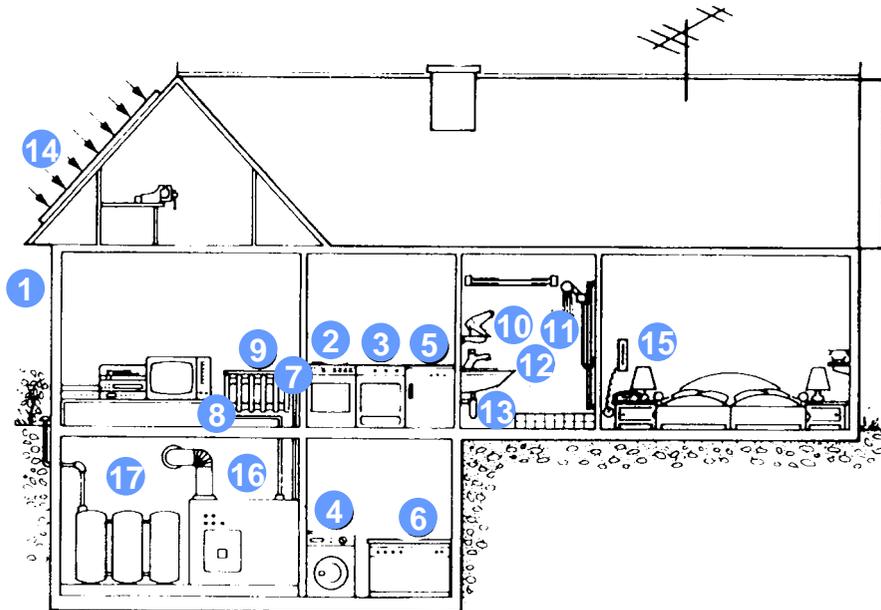
\* Thermistor: thermal sensitive resistor

Varistor: variable resistor

# Nonlinear Resistors / NTC

## Application of Negative Temperature Coefficient Resistors

- Temperature measuring and controlling

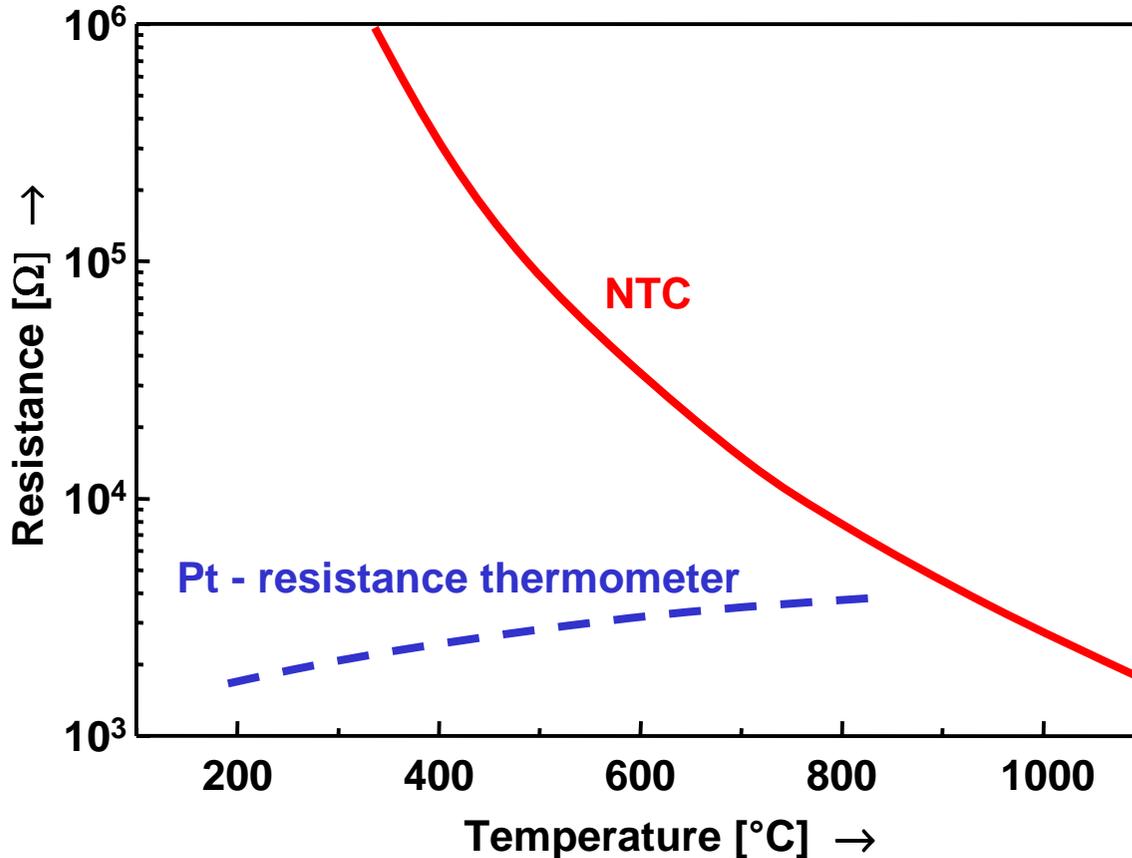


- |                               |  |
|-------------------------------|--|
| 1. Outside/inside temperature | 10. Hand dryer   |
| 2. Electric cooker            | 11. Dryer hood   |
| 3. Dishwasher                 | 12. Hair blower  |
| 4. Washing machine            | 13. Warm water heater  |
| 5. Refrigerator               | 14. Solar heater   |
| 6. Freezer                    | 15. Clinical thermometer   |
| 7. Room heater                | 16. Lamp starter   |
| 8. Underfloor heater          | 17. Switch-on current limitation<br>(small motor, circuit divider) |
| 9. Storage heater             |  |

- |                        |
|------------------------|
| 1. Outside temperature |
| 2. Inside temperature  |
| 3. Air conditioner     |
| 4. Air intake          |
| 5. Cooling water       |
| 6. Motor oil           |
| 7. Transmission oil    |
| 8. Brake fluid         |

# Nonlinear Resistors / NTC

## Resistance - temperature Characteristic Curve of NTC



**Example:**

**high temperature NTC**

**range of use: up to 1000 °C**

**Material:**

**metallic oxide**

The temperature-dependent electric conductivity will be determined by the charge carrier mobility:

$$\mu_n = \frac{K_1}{T} \cdot e^{-\frac{W_A}{kT}}$$

**K<sub>1</sub>: constant**

**W<sub>A</sub>: activation energy**

# Nonlinear Resistors / NTC

## Polycrystalline Semiconducting Metallic Oxide as NTC

**Materials:** Metallic oxide e.g. Mn, Fe, Co, Ni, Cu, Zn (transition metals)

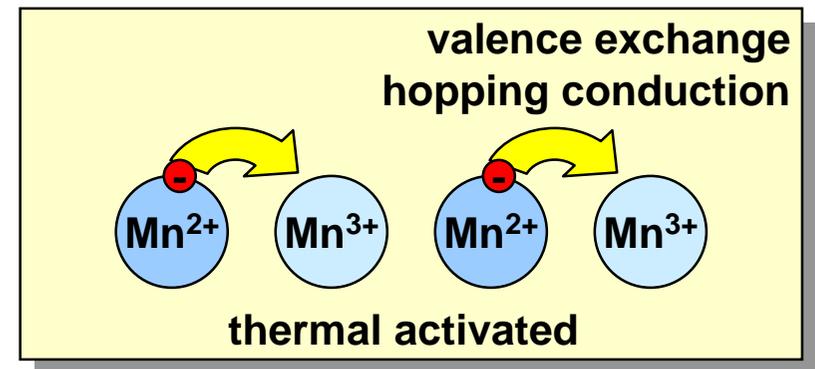
**Bond type:** predominantly or partially heteropolar (ionic) bond  
(metal: cation, oxygen: anion)

Semiconducting properties can result from valence exchange of the cations in the oxide.  
charge transport through hopping-mechanism (valence „transfer“)

element:	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn
valence:		+2	+2	+2	+2	+2	+2	+2	+2
	+3	+3	+3	+3	+3	+3	+3		
	+4	+4	+4	+4	+4				
		+5							

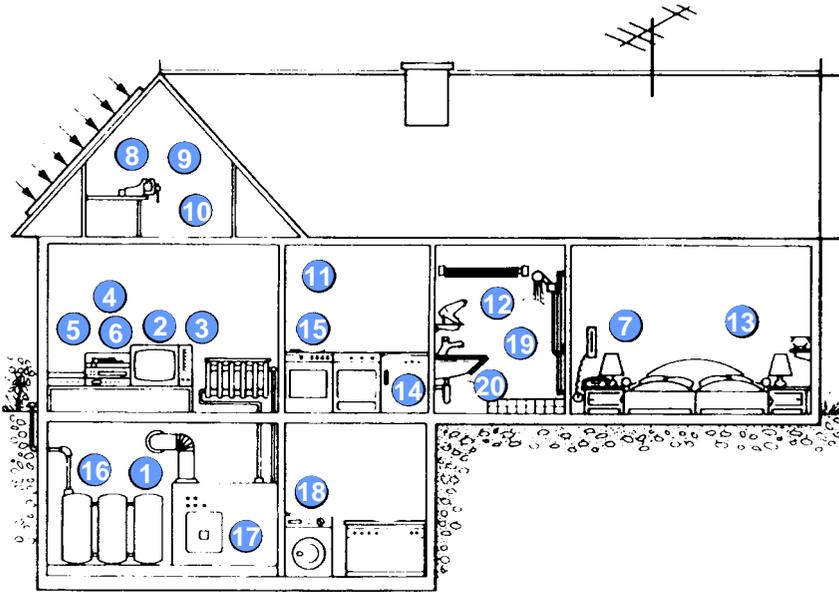
**Lattice structure:**  $A^{2+} B^{3+}_2 O^{2-}_4$  (spinel)

**typical NTC:**  $Ni^{2+} Mn^{3+}_2 O^{2-}_4$

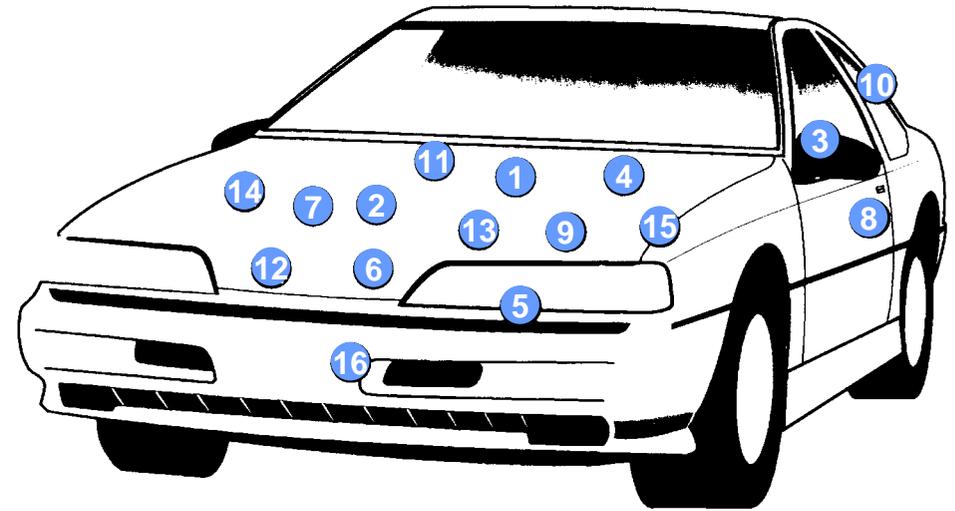


# Nonlinear Resistors / PTC

## Applications of Positive Temperature Coefficient Resistors



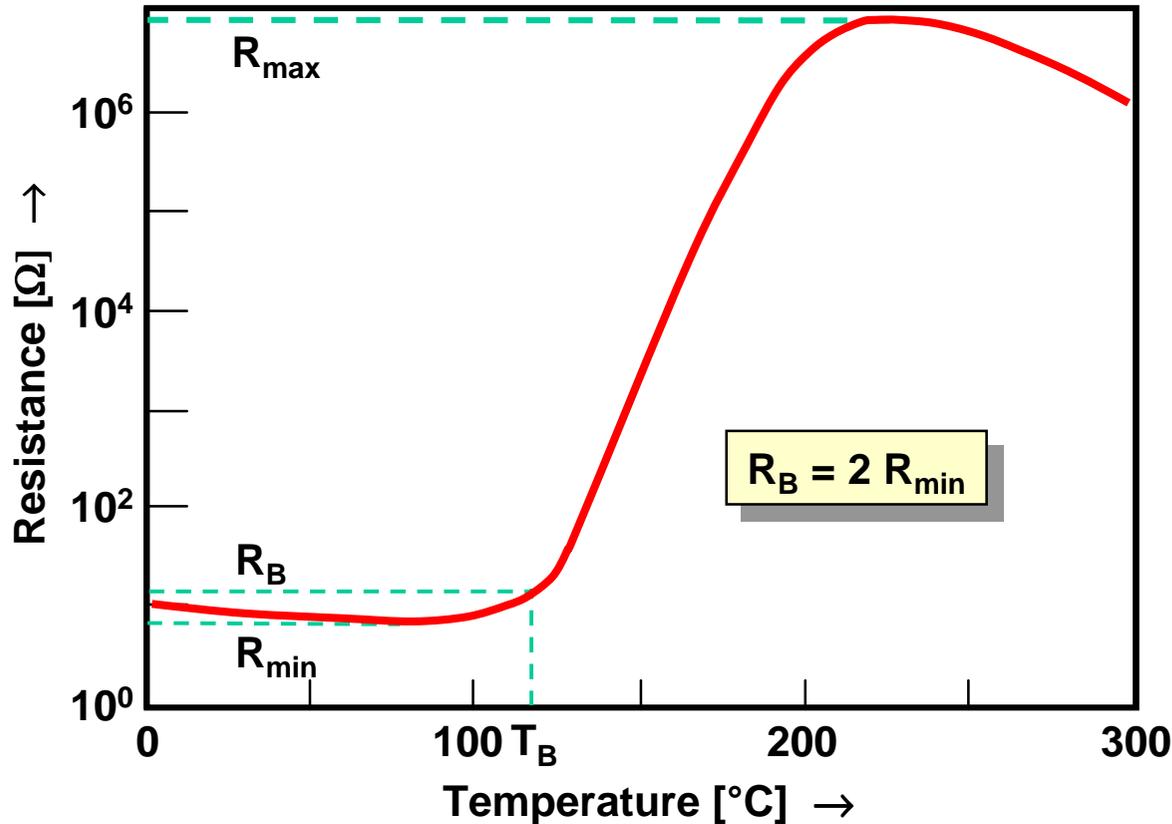
1. Lamp protection
2. TV-demagnetizing
3. Switching power supply overload protection
4. Video overload protection
5. Loudspeaker protection
6. Switching power supply startup
7. Telephone over-current protection
8. Sticking pistol door locking
9. Styrofoam cutter
10. Voltage tester
11. Overload protection for small motors
12. Curls rolling rod
13. Insect annihilator
14. Engine start compressor
15. Warm retaining plate
16. Tank overfilling protection
17. Oil preheating
18. Washing machine
19. Hand dryer
20. heater



1. Thermal valve heating
2. Carburetor heating
3. Mirror heating
4. Spray nozzle heating
5. Headlight washing system
6. Preheating of intake air (carburetors)
7. Mixture preheating (injector)
8. Door lock heating
9. Überlastschutz (elec. small motor)
10. Back window ventilation
11. Windshield wiper system check
12. Brake fluid check
13. Oil level check
14. Cooling water check
15. Gasoline display

# Nonlinear Resistors / PTC

## Resistance - temperature Characteristic Curve of PTC



**Material:**

semiconducting  $\text{BaTiO}_3$   
(n- i.e. donor doped)

$R_{\min}$ ,  $R_{\max}$ :

extreme values of the PTC  
branch with sign change in  
temperature coefficients

$R_{\max}/R_{\min}$ :

available resistance ratio  
maximal proportion:  $10^7$

$T_B$ :

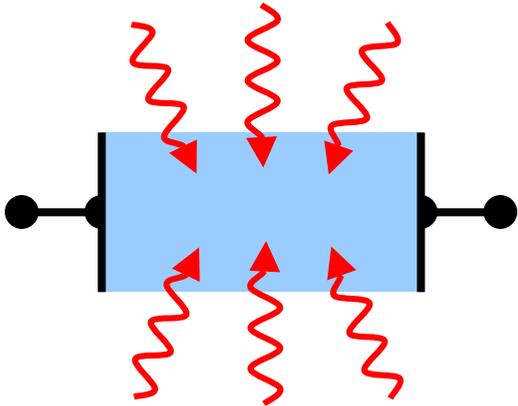
reference- or rated temperature  
of the component at  $R_B = 2 R_{\min}$   
 $T_B$ -values from  $-30\dots+250\text{ }^{\circ}\text{C}$

$\text{TK}_R$ : Temperature coefficient of the resistance  $\text{TK}_R = \frac{1}{R} \cdot \frac{dR}{dT}$ ,  $\text{TK}_R$ -values from 0,1...0,3  $\text{K}^{-1}$

# Nonlinear Resistors / PTC Applications

**Sensor**

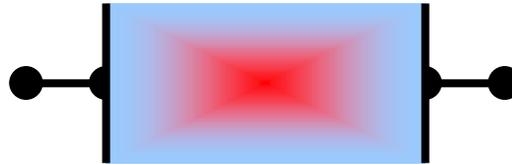
heat from the environment



- electrical thermometer
- temperature rise protection

**Controller**

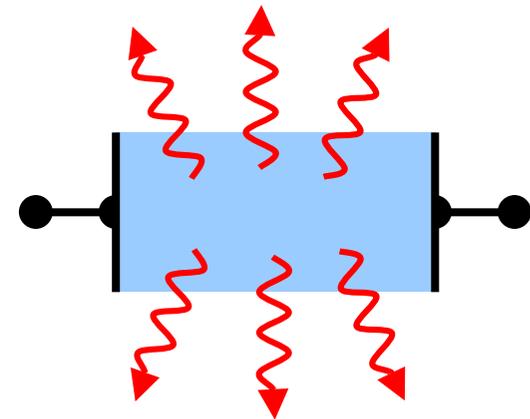
self-heating



- current stabilization
- switch time delay
- level monitoring
- current measurement

**Heater**

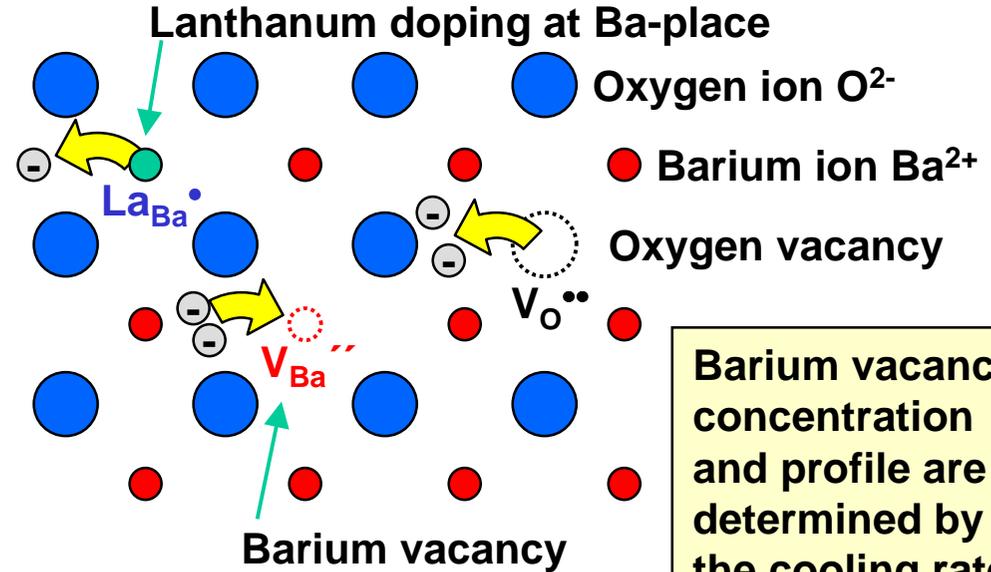
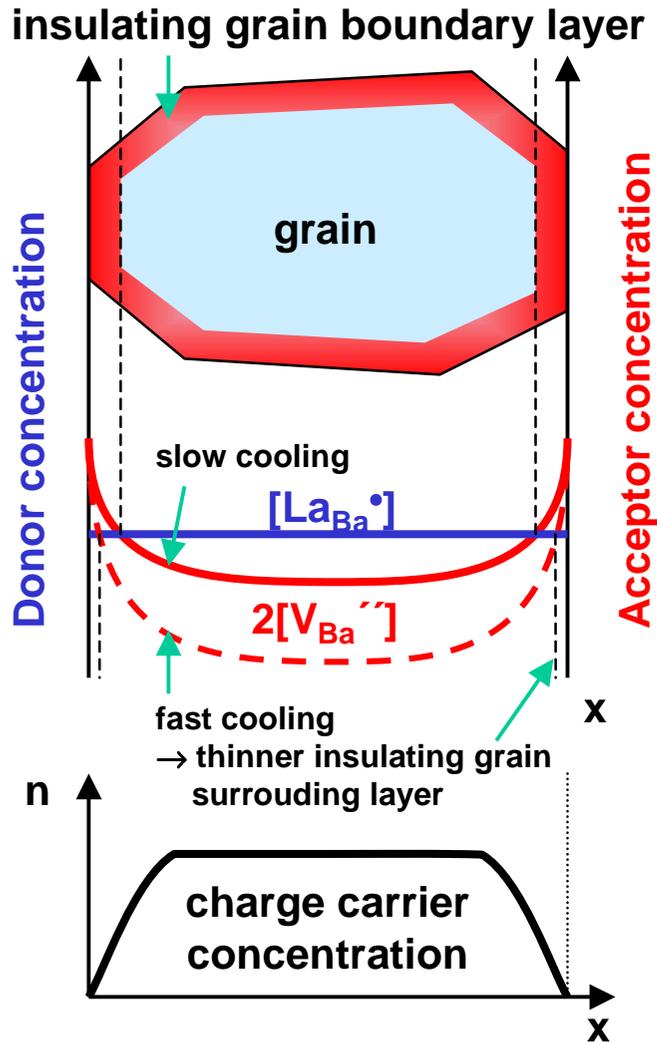
heat emission



- heating components self-regulating

# Nonlinear Resistors / PTC

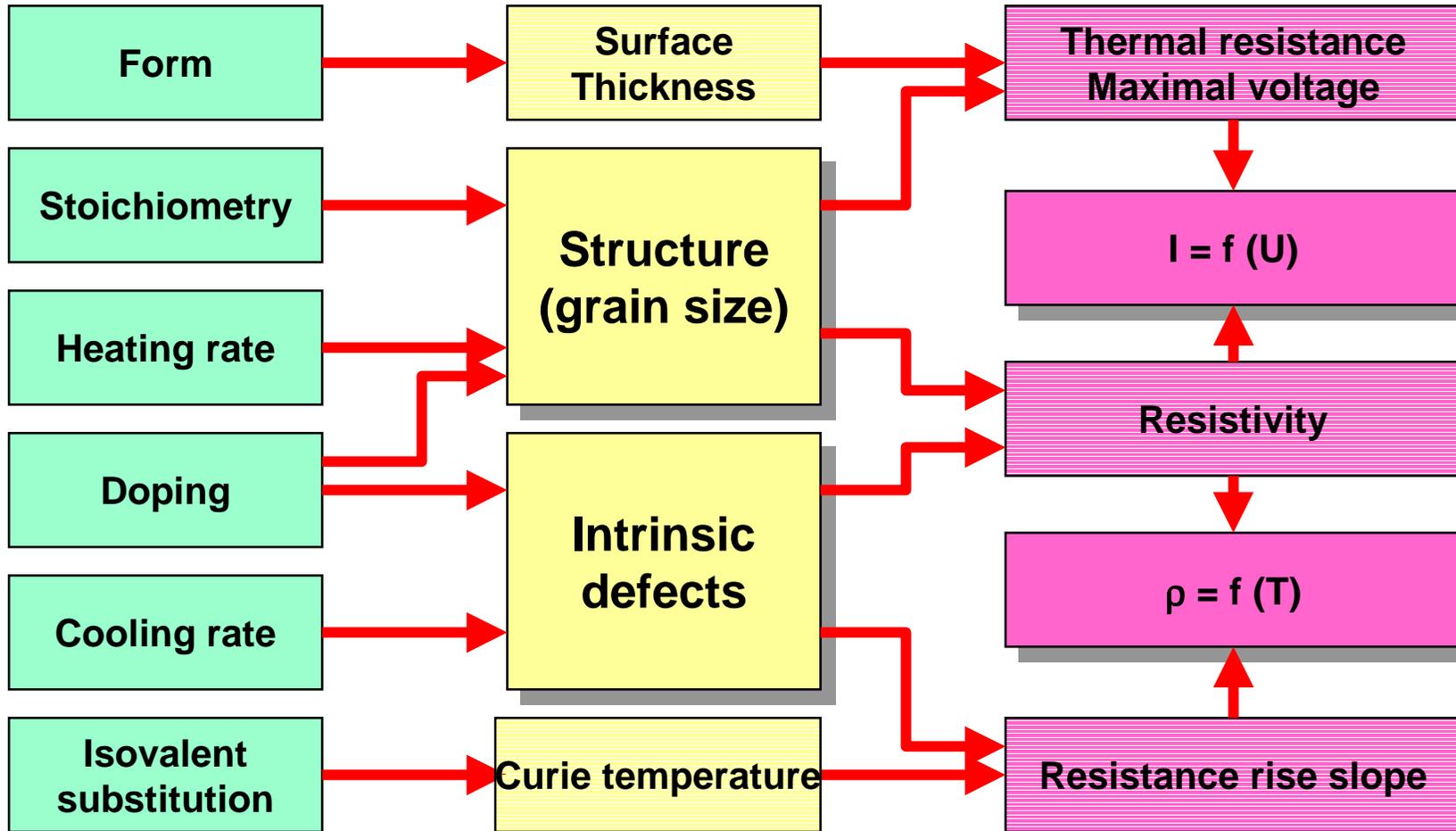
## Vacancy and Doping Profile



$V_{Ba}^{\prime\prime}$ :	Ba-vacancy (acceptor)
$V_O^{\bullet\bullet}$ :	O-vacancy (donor)
$La_{Ba}^{\bullet}$ :	$La^{3+}$ (doping) at $Ba^{2+}$ -place, (donor)
$\ominus e^-$ , (n):	electron (-concentration)

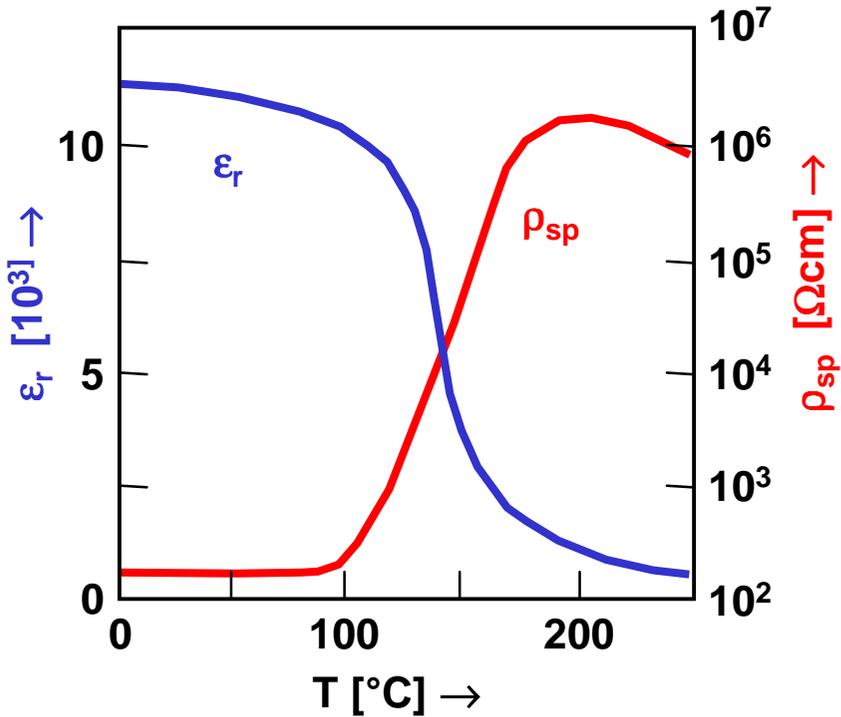
# Nonlinear Resistors / PTC

## Material Engineering with Ceramic PTC Resistors



# Nonlinear Resistors / PTC

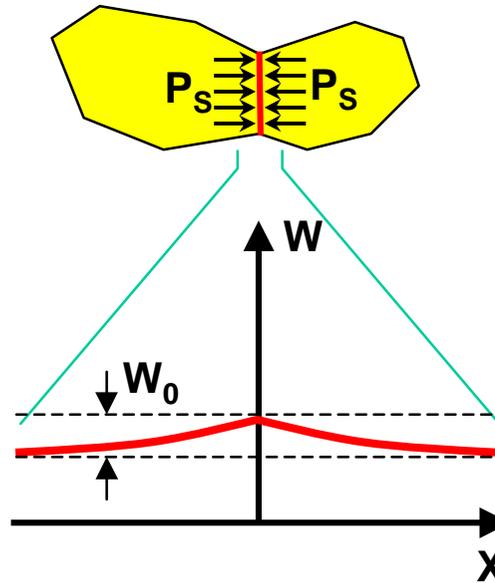
## Temperature-dependent Potential Barrier at Grain boundary in BaTiO<sub>3</sub>



$$W_0 \sim \epsilon_r^{-1} \sim T - T_C$$

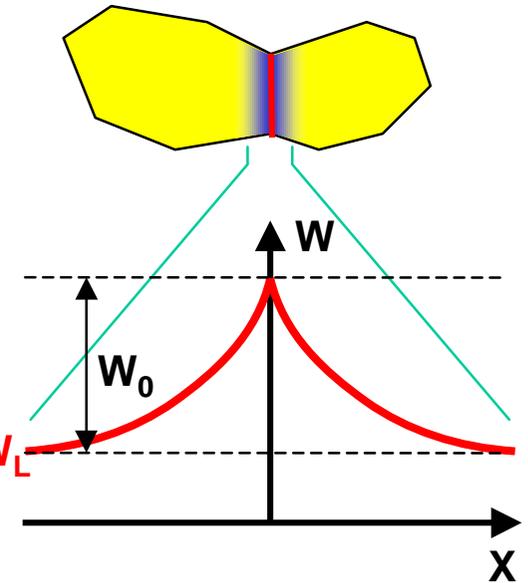
$$\rho_{sp} \sim e^{\frac{W_0}{kT}}$$

$T < T_C$  : ferroelectricity  
→ spontaneous polarization



polarization charges  
compensate negative  
grain boundary charges  
→  $W_0$  small

$T > T_C$  : disappearance  
of the spontaneous polarization

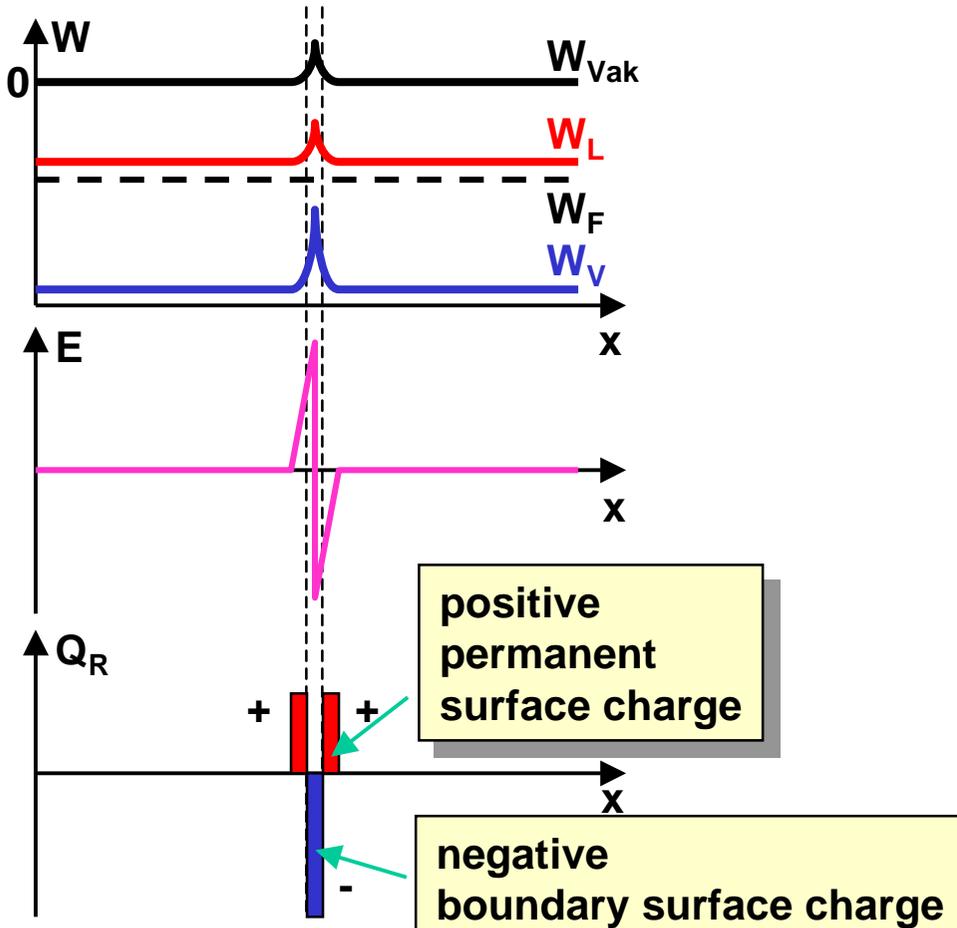


space charges  
compensate negative  
grain boundary charges  
→  $W_0$  large

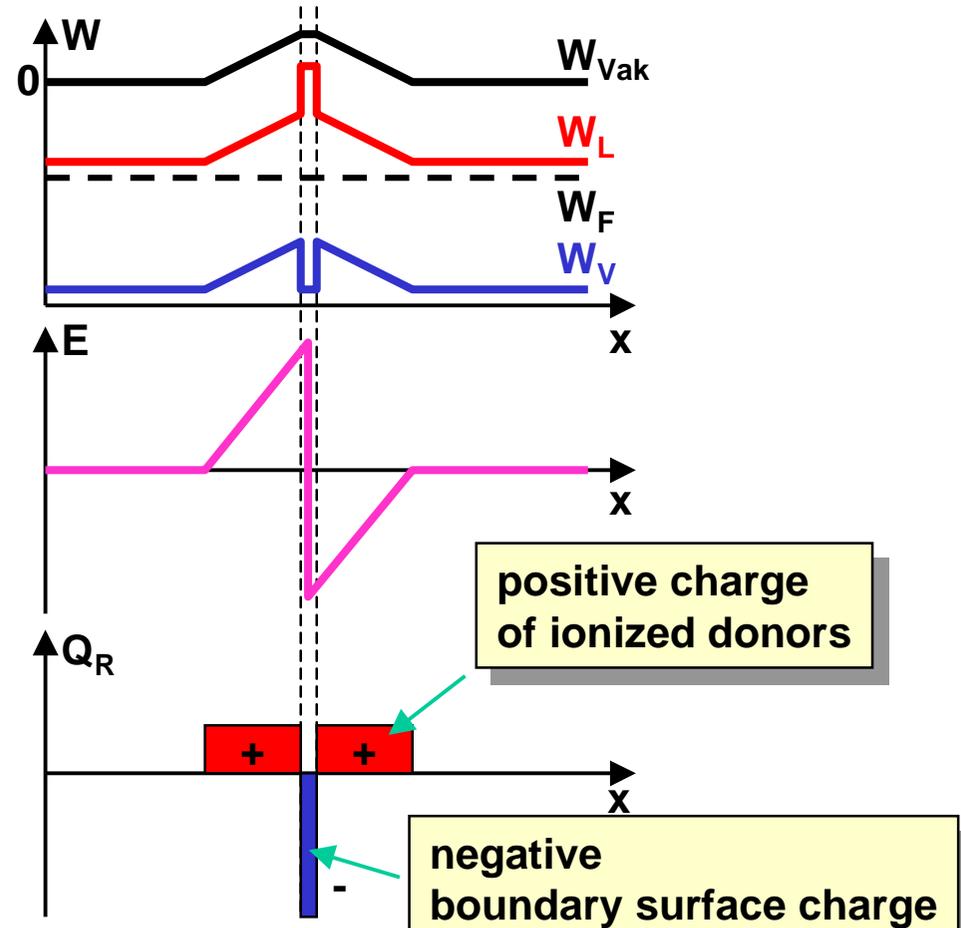
# Nonlinear Resistors / PTC

## Band Model, E-field Strength and Space Charge at the Grain Boundary

$T < T_C \rightarrow$  ferroelectricity: permanent dipole

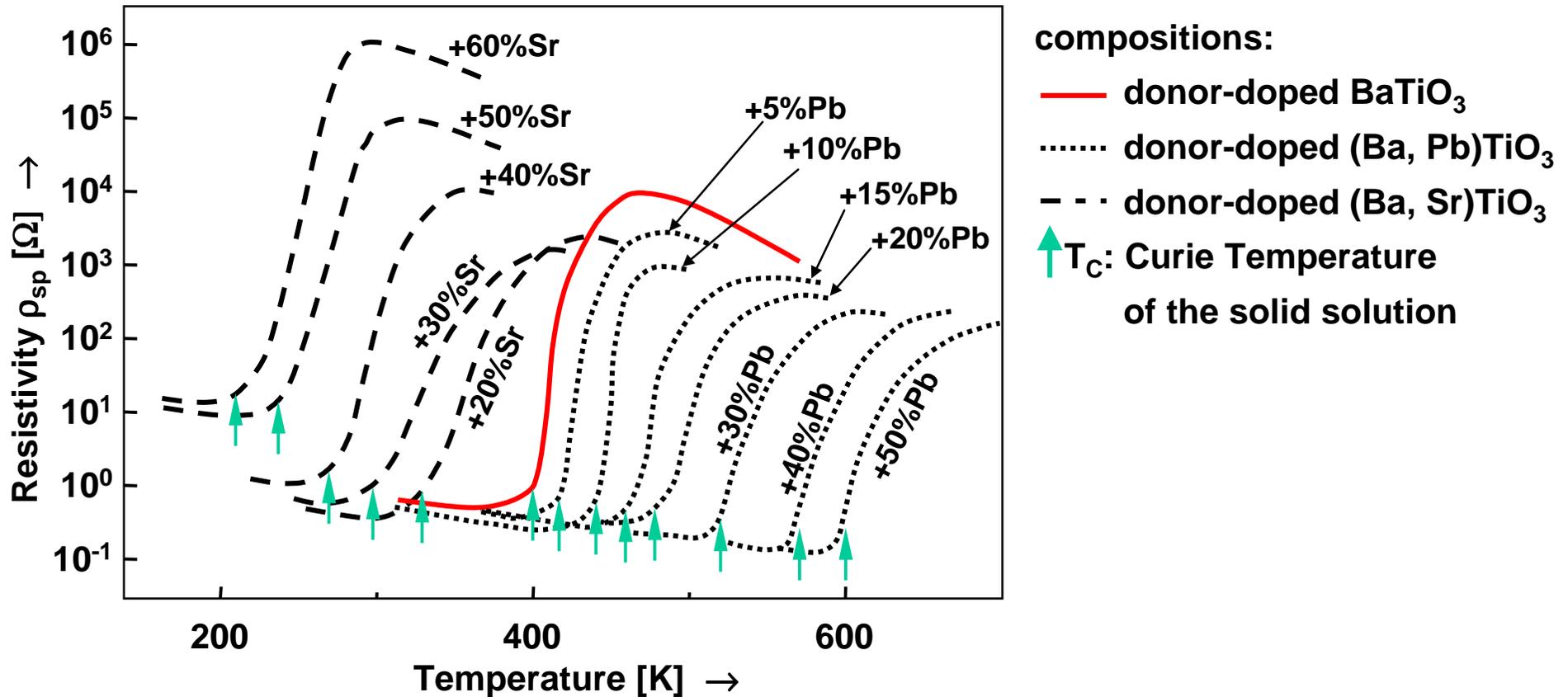


$T > T_C \rightarrow$  space charge of ionized donors



# Nonlinear Resistors / PTC

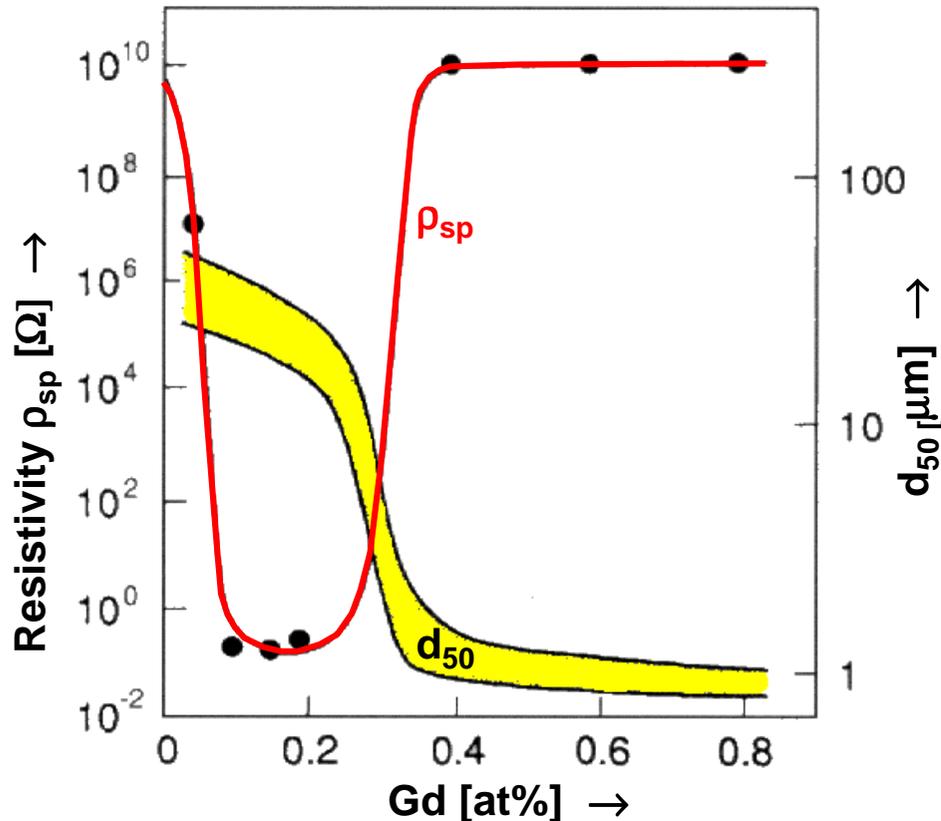
## Temperature dependence of resistivity $\rho_{sp}$ of PTC ceramics



Ferroelectric, semiconducting  $\text{BaTiO}_3$  shows an anomaly of resistance at  $T > T_C$  (PTC-effect)

# Nonlinear Resistors / PTC

## Middle Grain Size and $\rho_{sp}$ as a Funktion of the Dopant Concentration



- donor doping in perovskite



→  $\text{A}^{3+}$  in stead of  $\text{Ba}^{2+}$ :  $\text{La}^{3+}$ ,  $\text{Y}^{3+}$ ,  $\text{Gd}^{3+}$

→  $\text{B}^{5+}$  in stead of  $\text{Ti}^{4+}$ :  $\text{Sb}^{5+}$ ,  $\text{Nb}^{5+}$ ,  $\text{Ta}^{5+}$

- doping effects

→ decrease of the resistivity  $\rho_{sp}$   
(electron conduction) only with  
donor concentration  $\leq 0,3$  at%

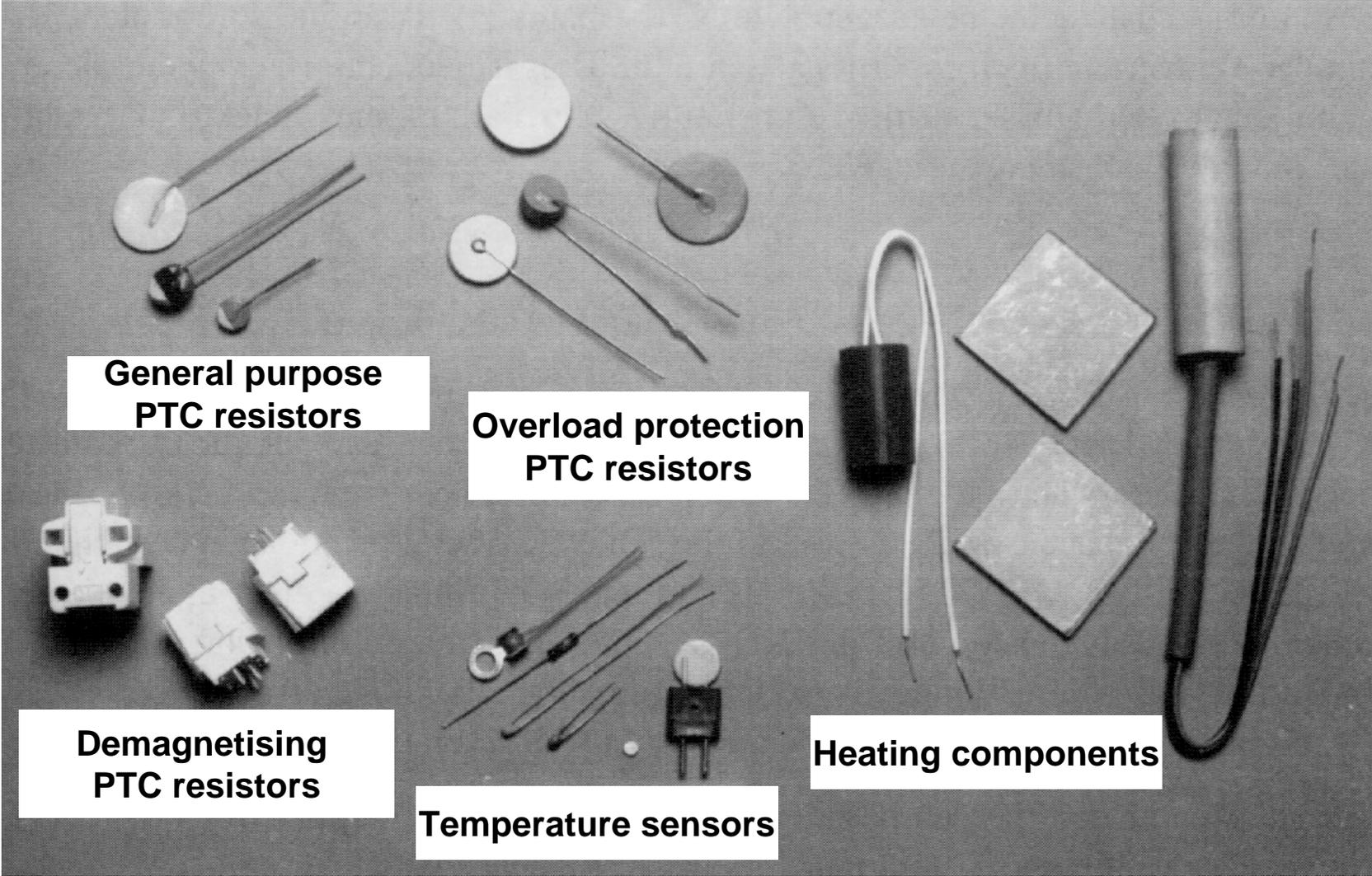
→ decrease of the middle grain size  $d_{50}$   
with increasing donor concentration

variation of  $\rho_{sp}$  und  $d_{50}$  :

independent of the type of donor  
strongly dependent on the donor concentration

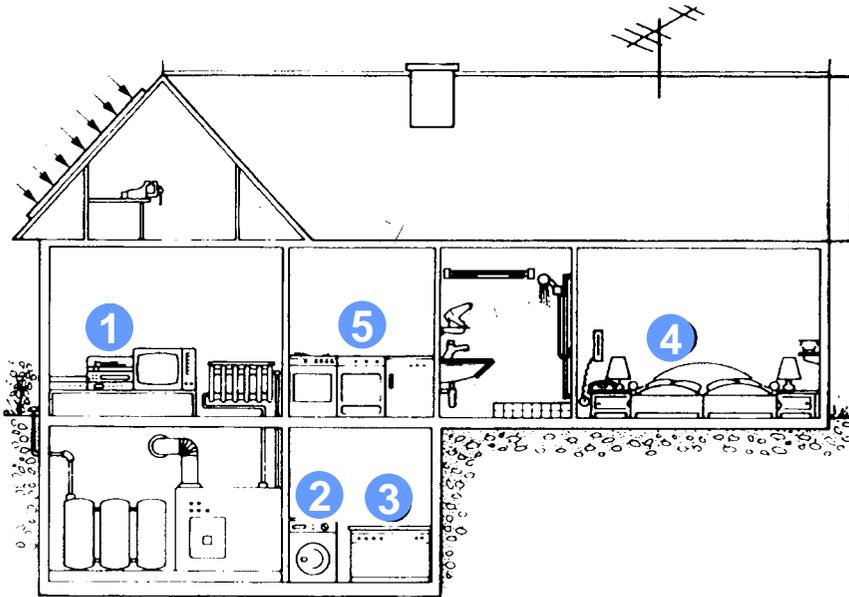
# Nonlinear Resistors / PTC

## Device Description

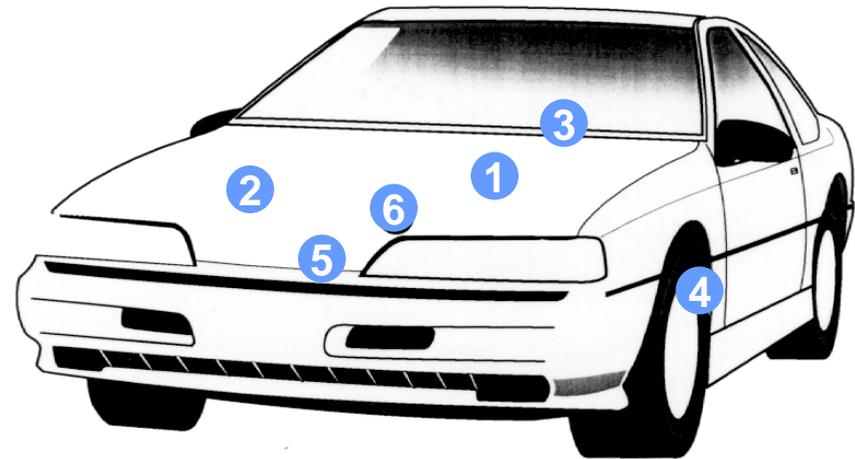


# Nonlinear Resistors / Varistors

## Applications of Varistors



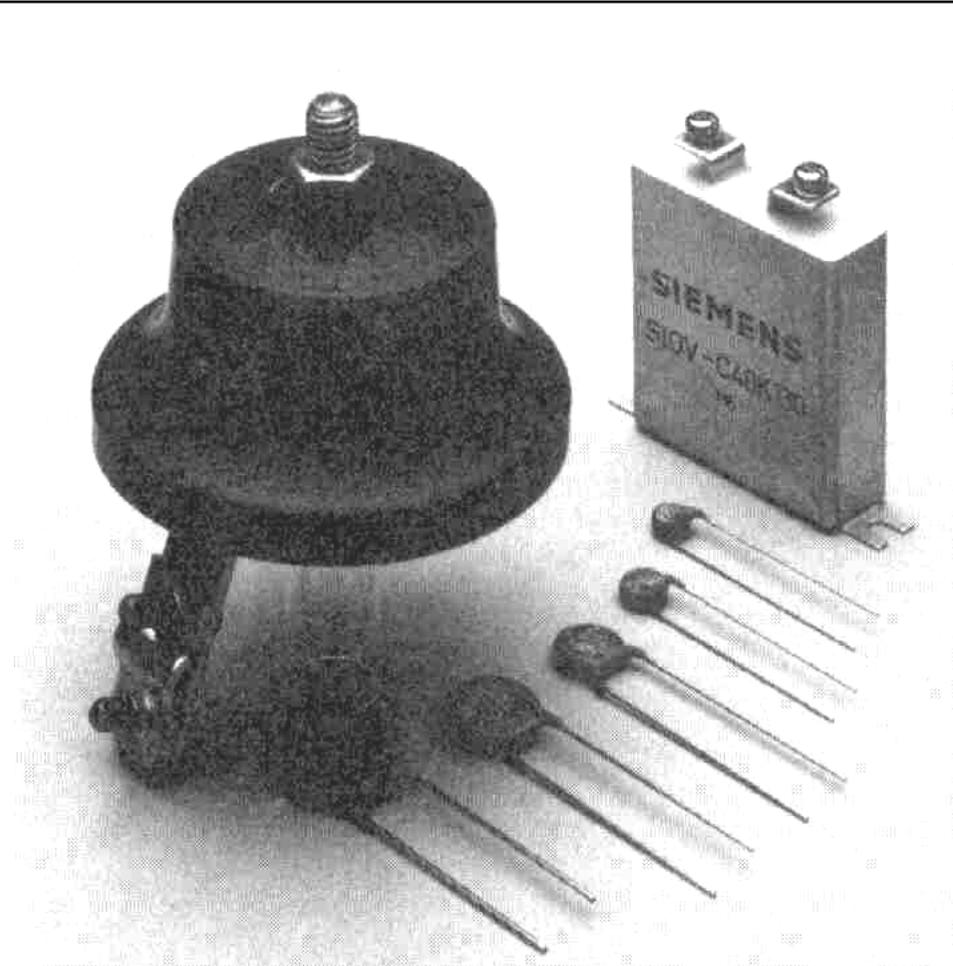
1. Lightning protection for television, video, PC, ...
2. Washing machine
3. Deep-freezer
4. Telephone
5. Total protection



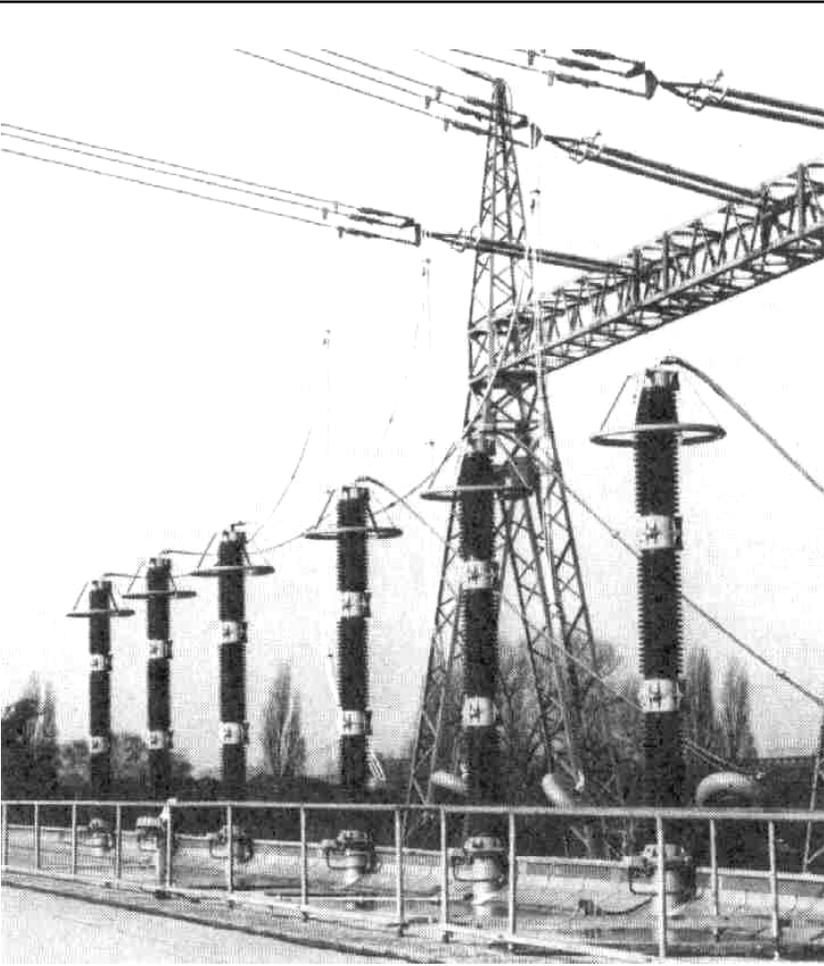
1. Central electrical system protection
2. Overvoltage-protected electronic ignition
3. Airbag
4. ABS
5. Board computer
6. Combination protection

# Nonlinear Resistors / Varistors

## Examples



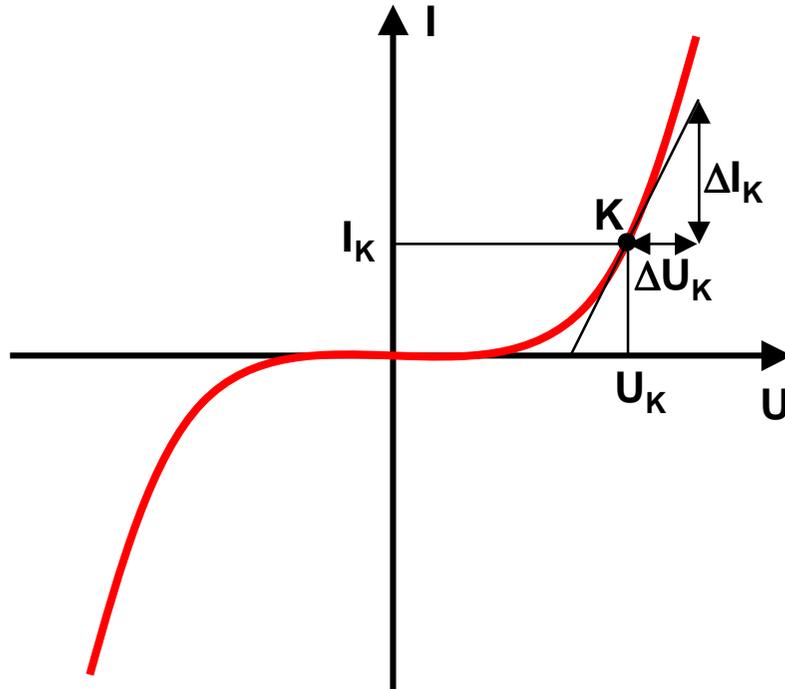
• Designs of ZnO Varistors



• Varistors as high voltage deflector

# Nonlinear Resistors / Varistors

## Current-Voltage-Characteristic Curve



### Varistor

#### Variable Resistor

voltage-dependent resistance  
with symmetric  $I(U)$ -characteristic curve

$$I = \pm K \cdot |U|^\alpha$$

geometry-  
dependent  
constant  $K$

nonlinear  
coefficient  $\alpha$

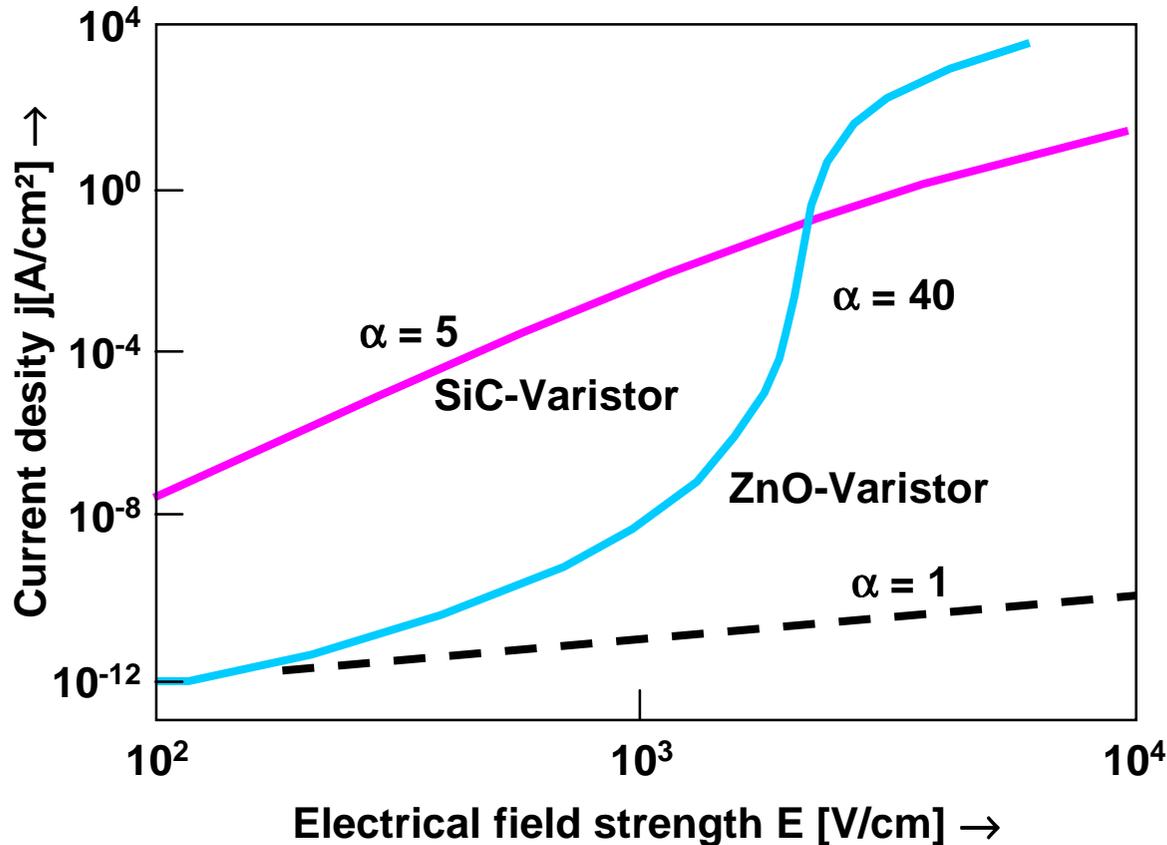
typical  $\alpha$ -values: 5...70

Materials: SiC, ZnO

**application of varistors as protection from overvoltages**

# Nonlinear Resistors / Varistors

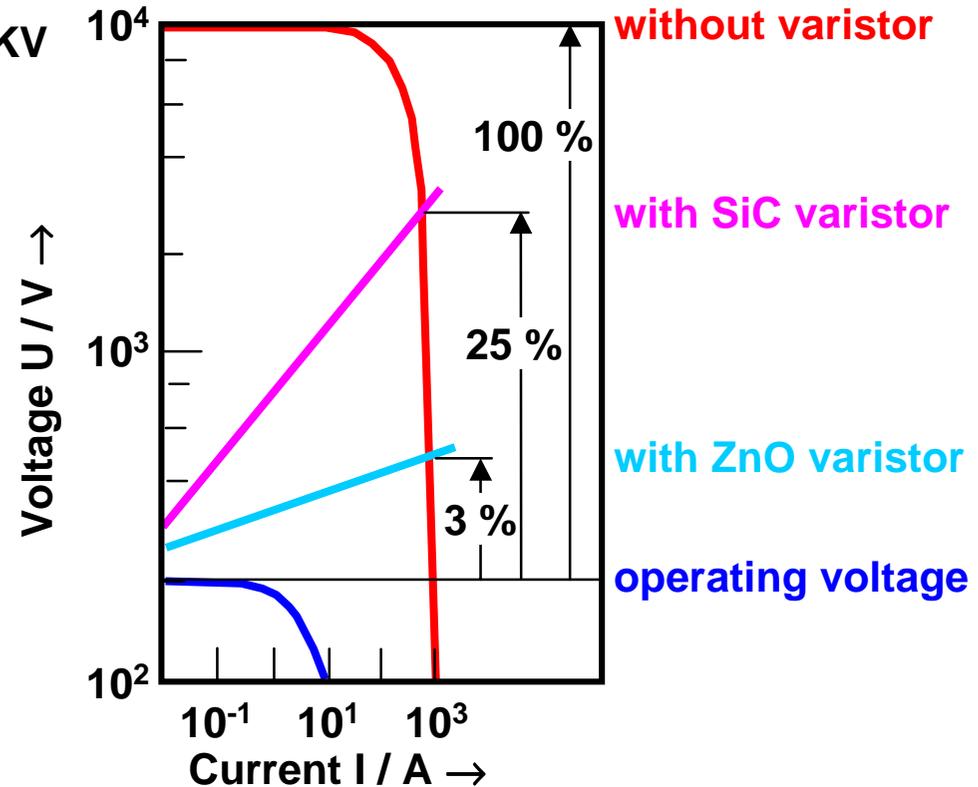
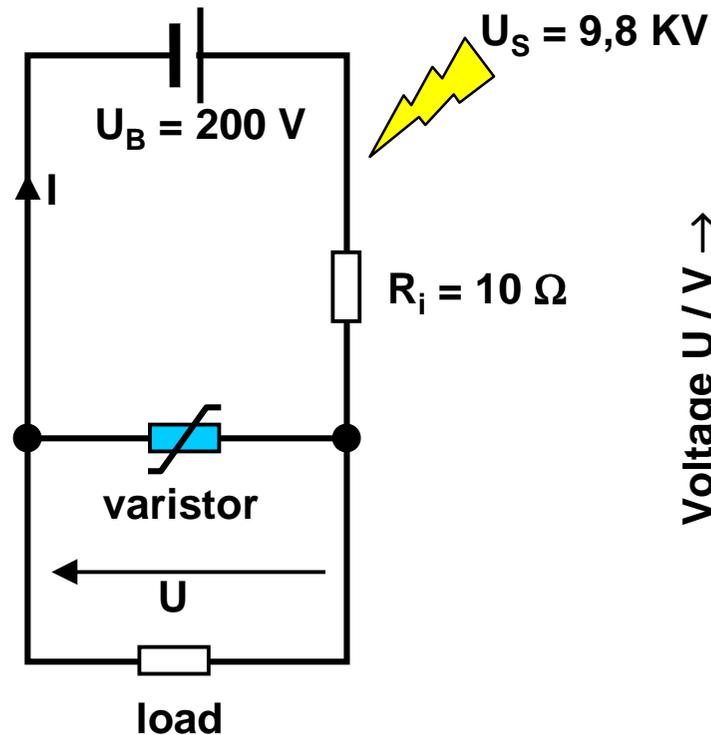
## Current-Voltage-Curve of SiC and ZnO Varistors



- ohmic resistance  $\alpha = 1$
- silicon carbide SiC varistor  
p-type (Al-doped) SiC  
grain size approx.  $100 \mu\text{m}$   
 $\alpha \approx 5 \dots 7$
- zinc oxide ZnO varistor  
n-type doped ZnO with  
insulating grain boundaries  
grain size variable:  
<  $1 \mu\text{m}$  to  $100 \mu\text{m}$   
 $\alpha$ -values from  $30 \dots 70$   
very low leakage current

# Nonlinear Resistors / Varistors

## Comparison of SiC and ZnO Varistors as Overvoltage Protection



The voltage  $U$  is temporary increased by an interference voltage  $U_S(t)$ .  
$$U(t) = U_S(t) + U_B - R_i \cdot I(t)$$

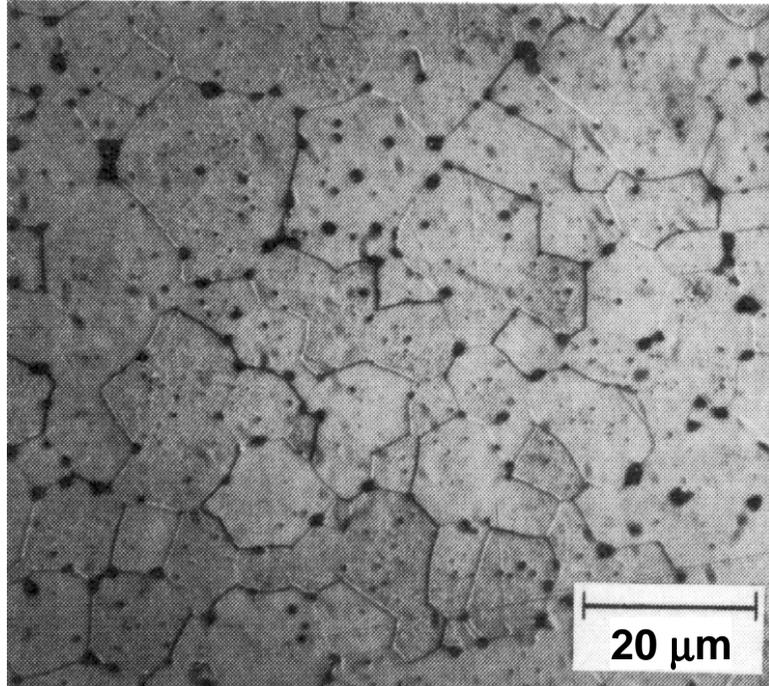
Double-logarithmic curve  $U(I)$

- during normal operating voltage
- during overvoltage  $U_S = 9,8 \text{ kV}$

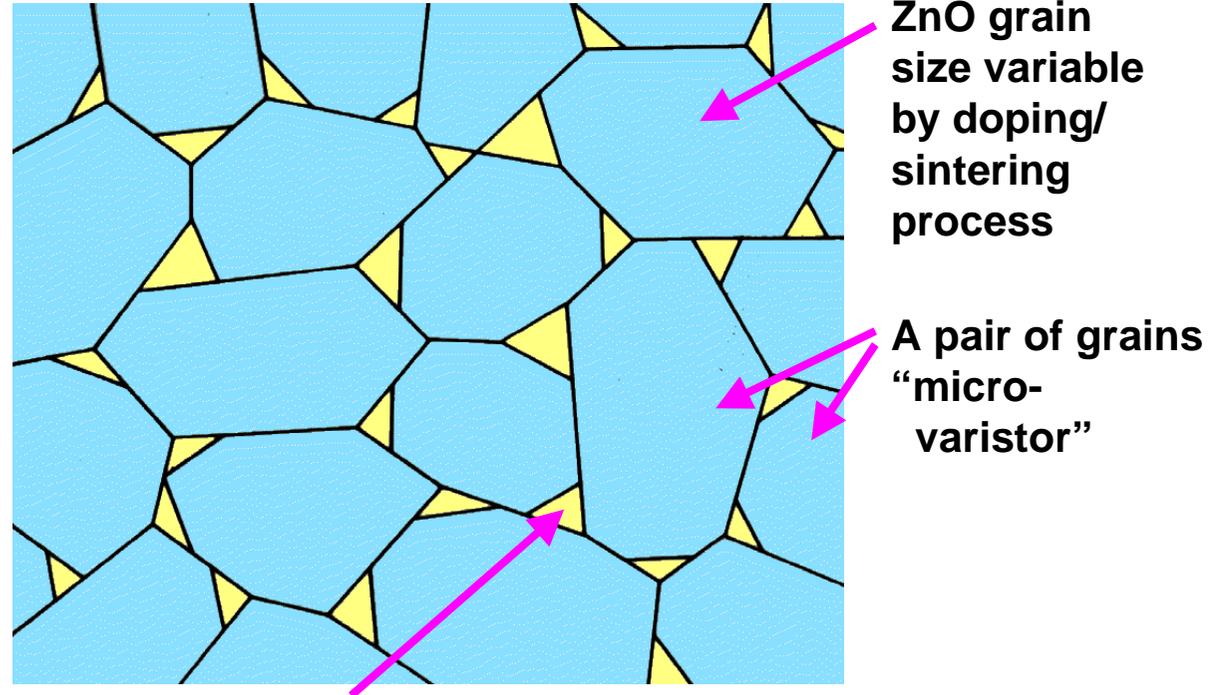
# Nonlinear Resistors / Varistors

## Polycrystalline ZnO - Structure with Secondary Phases

Micrograph of a ZnO varistor ceramic



Scheme of the structure of a ZnO varistor ceramic

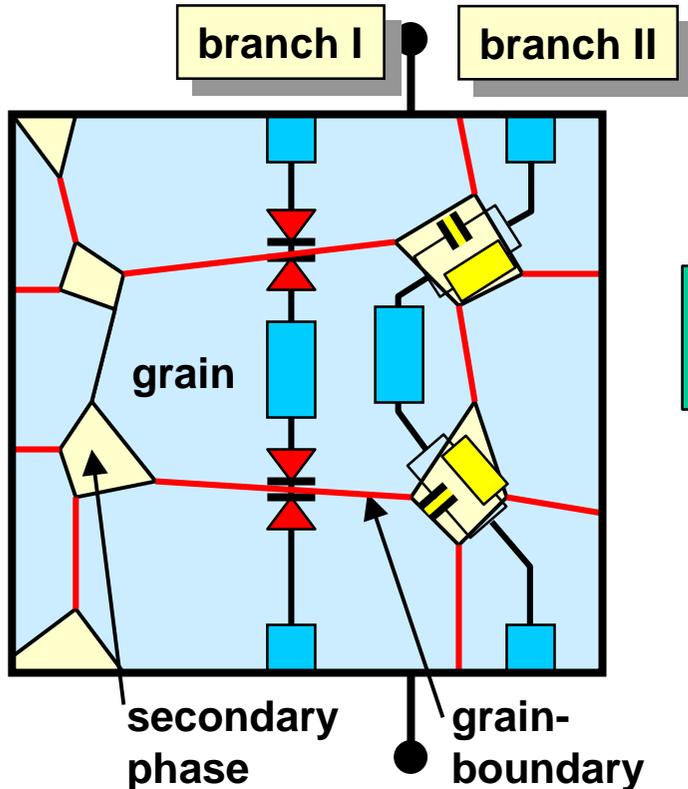


**Polycrystalline ceramic:** network from parallelly and serially connected micro-varistors  
**Varistor operating voltage:** depending on the grain size and geometry of the component

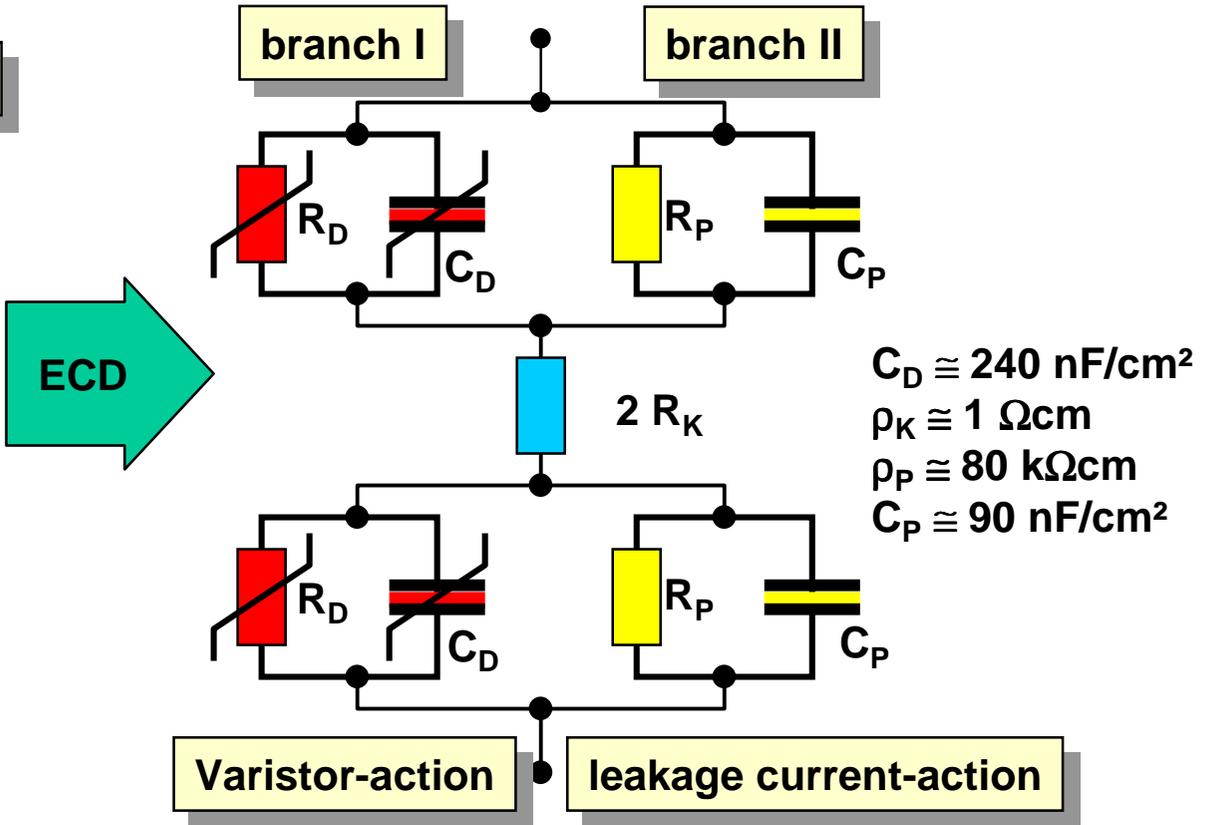
# Nonlinear Resistors / Varistors

## Polycrystalline ZnO - Structure: Eq. Circuit Diagram for Micro-varistors

### • structure scheme



### • equivalent circuit diagram



Series connection of grain resistance ( $R_K$ ) and barrier layer resistance ( $R_D$ )  
 parallel connection of  $R_D$  and  $C_D$   
 $R_D$  and  $C_D$ : voltage-dependent

leakage current action regions  
 $R_P, C_P$  parallel to  
 the varistor-action grain boundaries

# Nonlinear Resistors / Varistors

## Polycrystalline ZnO - Ceramic: Summary

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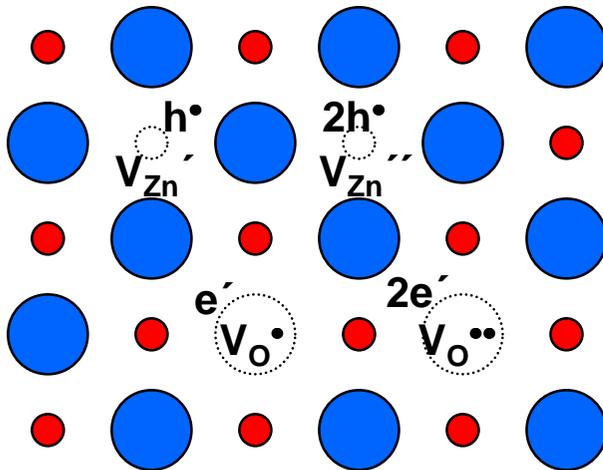
- **Varistor effect in doped ZnO ceramic is a characteristic of the grain boundary region. ZnO grains are low impedance.**
- **Varistor effect occurs at pairs of grains, which in direct contact to each other.**
- **Varistor effect starts with a breakthrough voltage of approx.  $3,0 \pm 0.5$  V / grain boundary.**
- **Grain boundary region forms a potential barrier of 0,6 eV.**
- **Response time of the nonlinear current is within several nanoseconds**
- **Available varistor system:  $\text{ZnO} + \text{Bi}_2\text{O}_3 + \text{MnO}_2 + \text{Co}_3\text{O}_4 + \text{Sb}_2\text{O}_3 + \text{Cr}_2\text{O}_3$  + further additives (up to 10 components are common practice, reason: optimization of the secondary characteristics of the respective type of varistor).**

# Nonlinear Resistors / Varistors

## Schottky-Defects and Band Scheme in ZnO

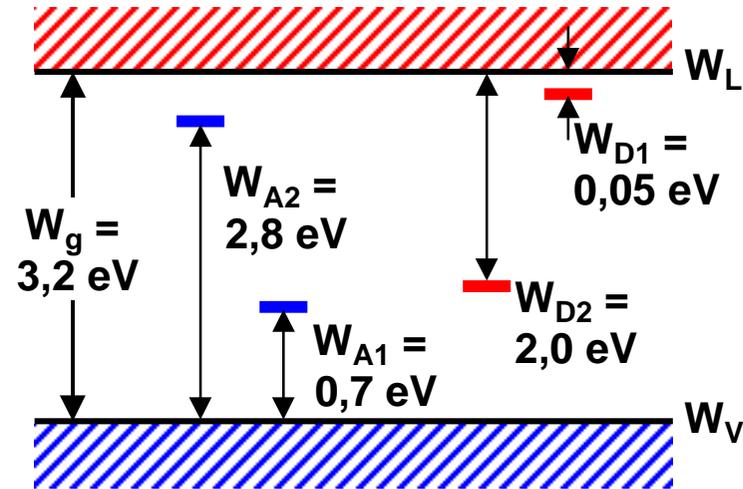
### Schottky-defects in ZnO

(2-dimension illustration)



$$n + [V_{Zn}'] + 2[V_{Zn}'] = p + [V_O^\bullet] + 2[V_O^{\bullet\bullet}]$$

$V_{Zn}'$ ,  $V_{Zn}''$ : one or two charged Zn-vacancy defect electrons (concentration)  
 $h^\bullet$ , (p): defect electrons (concentration)  
 $V_O^\bullet$ ,  $V_O^{\bullet\bullet}$ : one or two charged O-vacancy electrons (concentration)  
 $e'$ , (n): electrons (concentration)



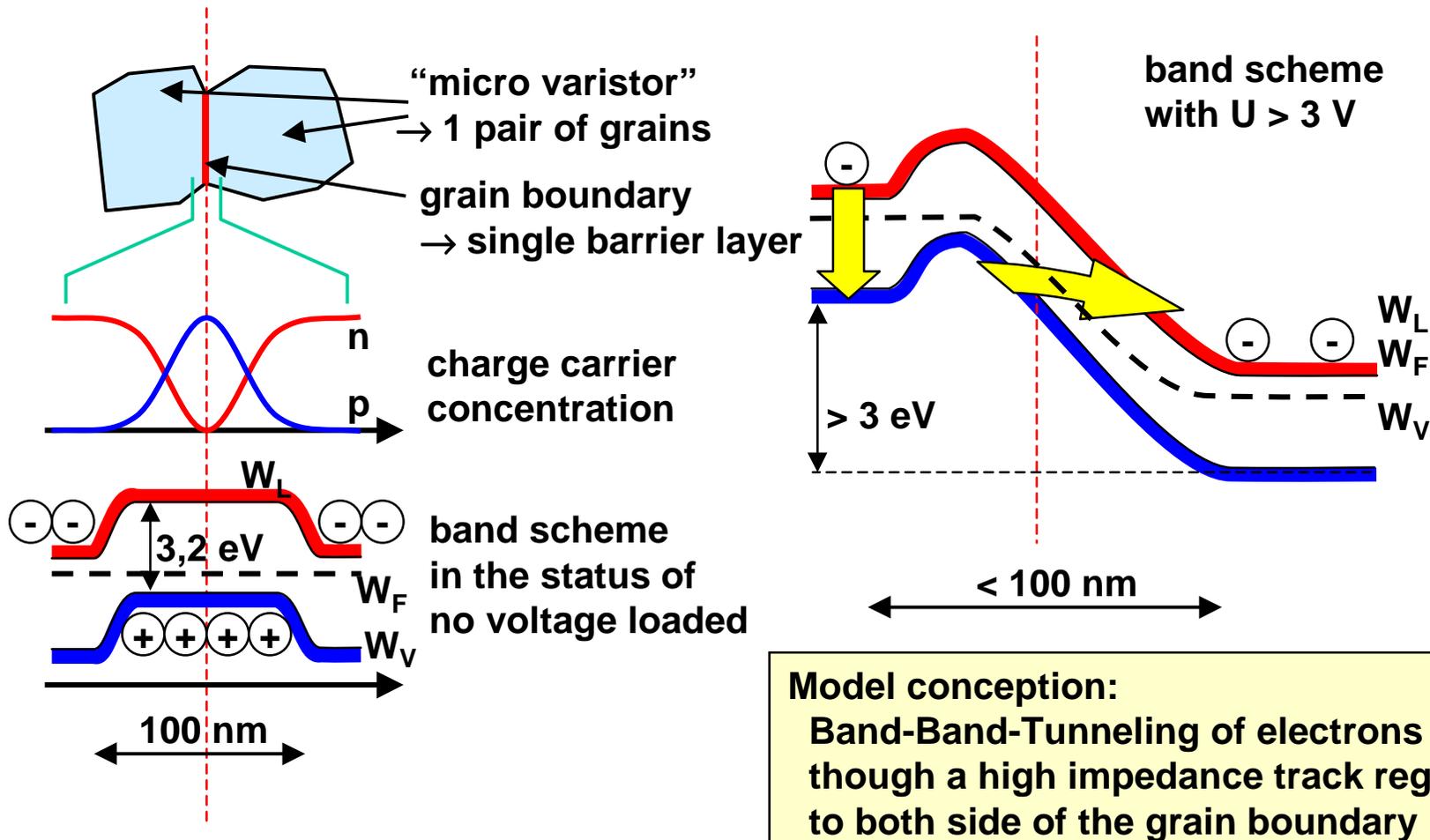
Band scheme with the energy levels of the Schottky-defects ( $W_A$ ,  $W_D$ )

( $W_{A1}$ ,  $W_{A2}$ ) A: acceptors

( $W_{D1}$ ,  $W_{D2}$ ) D: donors

# Nonlinear Resistors / Varistors

## Band Model of ZnO Varistor at Grain Boundary



# Nonlinear Resistors / Varistors

## Adjustment of the High Impedance Track Region at the Grain Boundary

- Production (sintering temperature  $\approx 1300\text{ }^\circ\text{C}$ )

$\Rightarrow$  high-temperature equilibrium:

excess of oxygen vacancy

charge carrier:  $n = [V_{O^\bullet}] + 2 \cdot [V_{O^{\bullet\bullet}}]$

- Operating temperature  $< 100\text{ }^\circ\text{C}$

$\Rightarrow$  low-temperature equilibrium:

$$[V_{Zn'}] + 2[V_{Zn''}] \approx [V_{O^\bullet}] + 2[V_{O^{\bullet\bullet}}]$$

$\Rightarrow n$  very small

adjustment of the low-temperature equilibrium only in the grain boundary layer

