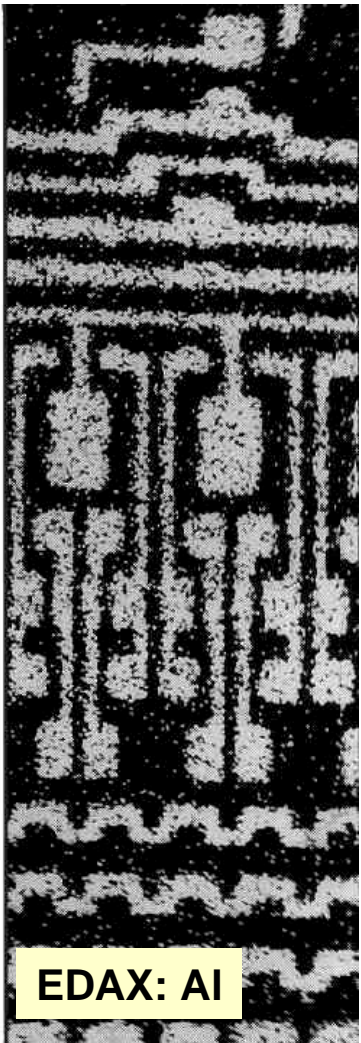
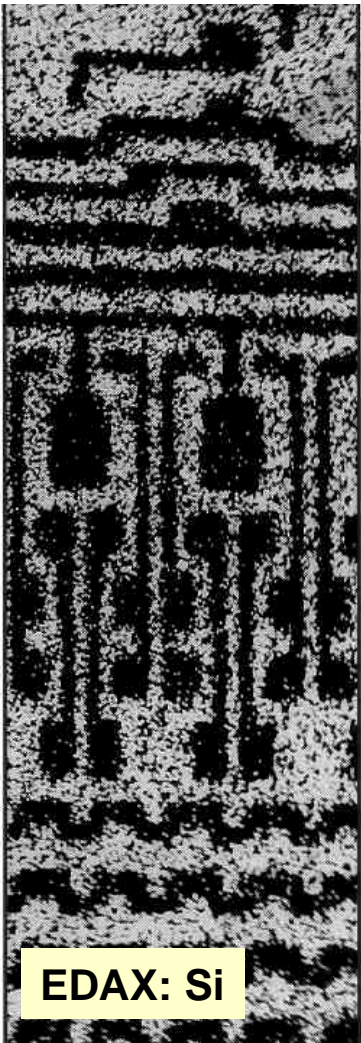
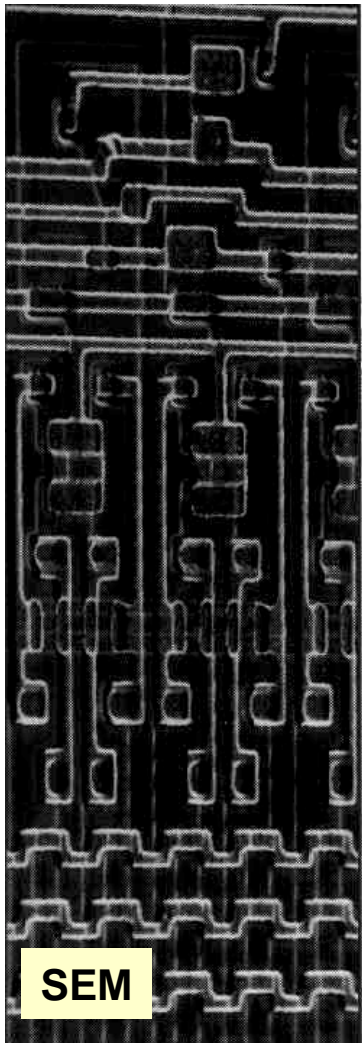


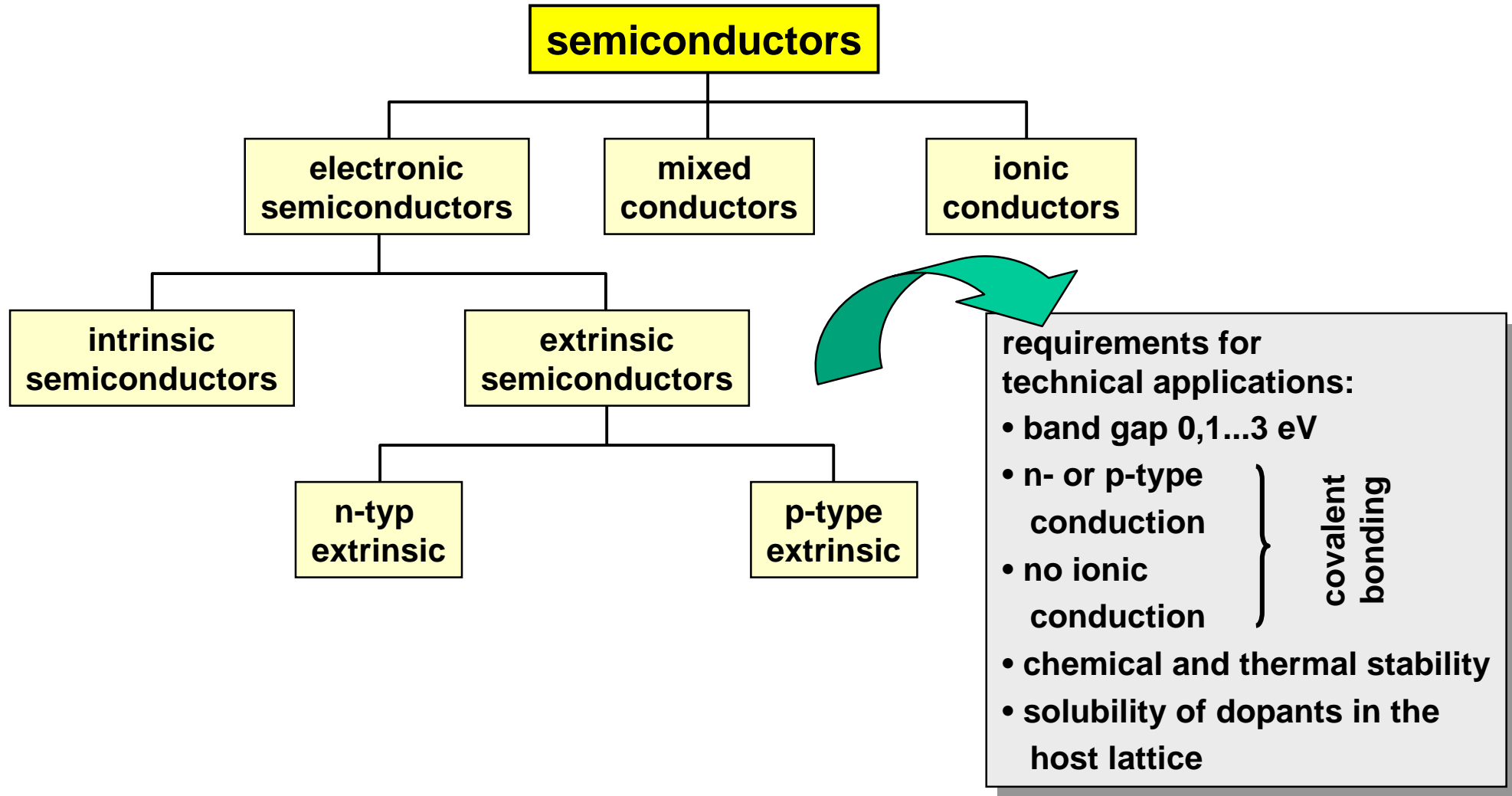
Semiconductors



SEM and EDAX images of an integrated circuit

Semiconductors

Classification



Semiconductors

Elemental Semiconductors and Dopants

period	group					
	II	III	IV	V	VI	VII
2	Be	B	C	N	O	F
3	Mg	Al	Si	P	S	Cl
4	Ca Zn	Ga	Ge	As	Se	Br
5	Sr Cd	In	Sn	Sb	Te	I

<p>p-type</p> <p>n-type</p> <p>- dopants for Si and Ge</p>

band gap E_g / eV
of different semiconductors

	T = 0 K	T = 300 K
Si	1,17	1,11
Ge	0,74	0,68
GaAs	1,52	1,38
InAs	0,36	0,35
InSb	0,23	0,18
CdS	2,58	2,42
CdTe	1,61	1,45
ZnO	3,44	3,20

Semiconductors

Elemental and Compound Semiconductors

elemental s.	compound s.		number of electrons per unit
IV - IV bonding	III - V bonding	II - VI bonding	
C			6
SiC			10
Si	AIP		14
GeSi	AlAs, GaP	ZnS	23
Ge	AlSb, GaAs, InP	ZnSe, CdS	32
	GaSb, InAs	ZnTe, CdSe, HgS	41
Sn	InSb	CdTe, HgSe	50
		HgTe	66

atomic bonding forces become more ionic

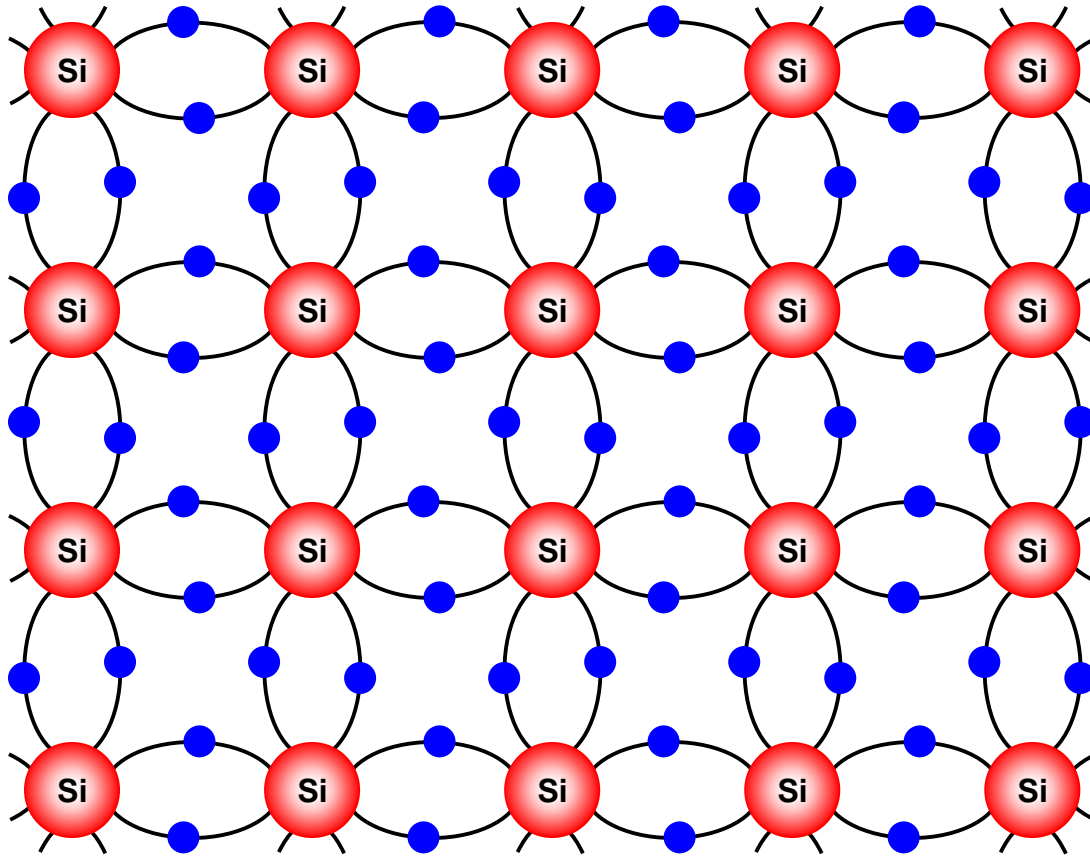
Semiconductors

Properties of Elemental and Compound Semiconductors

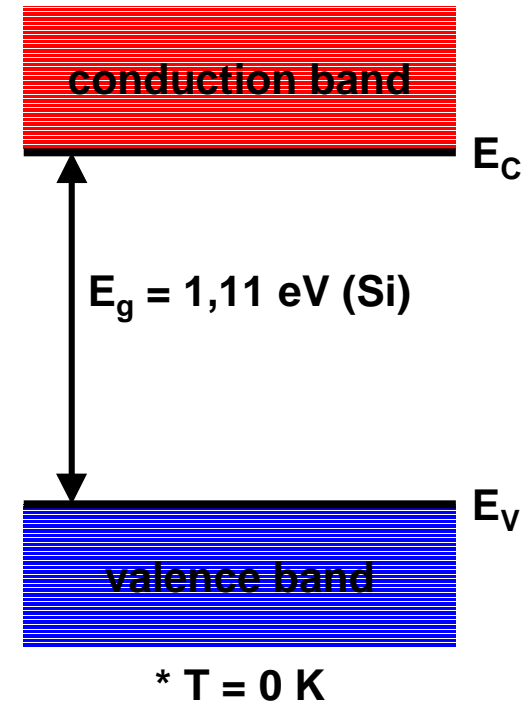
<i>Material</i>	<i>Band Gap</i> (<i>eV</i>)	<i>Electrical</i> <i>Conductivity</i> [$(\Omega\text{-m})^{-1}$]	<i>Electron Mobility</i> ($\text{m}^2/\text{V}\text{-s}$)	<i>Hole Mobility</i> ($\text{m}^2/\text{V}\text{-s}$)
Elemental				
Si	1.11	4×10^{-4}	0.14	0.05
Ge	0.67	2.2	0.38	0.18
III-V Compounds				
GaP	2.25	—	0.05	0.002
GaAs	1.42	10^{-6}	0.85	0.45
InSb	0.17	2×10^4	7.7	0.07
II-VI Compounds				
CdS	2.40	—	0.03	—
ZnTe	2.26	—	0.03	0.01

Semiconductors

Electrical Conduction in Intrinsic Silicon at $T = 0 \text{ K}$



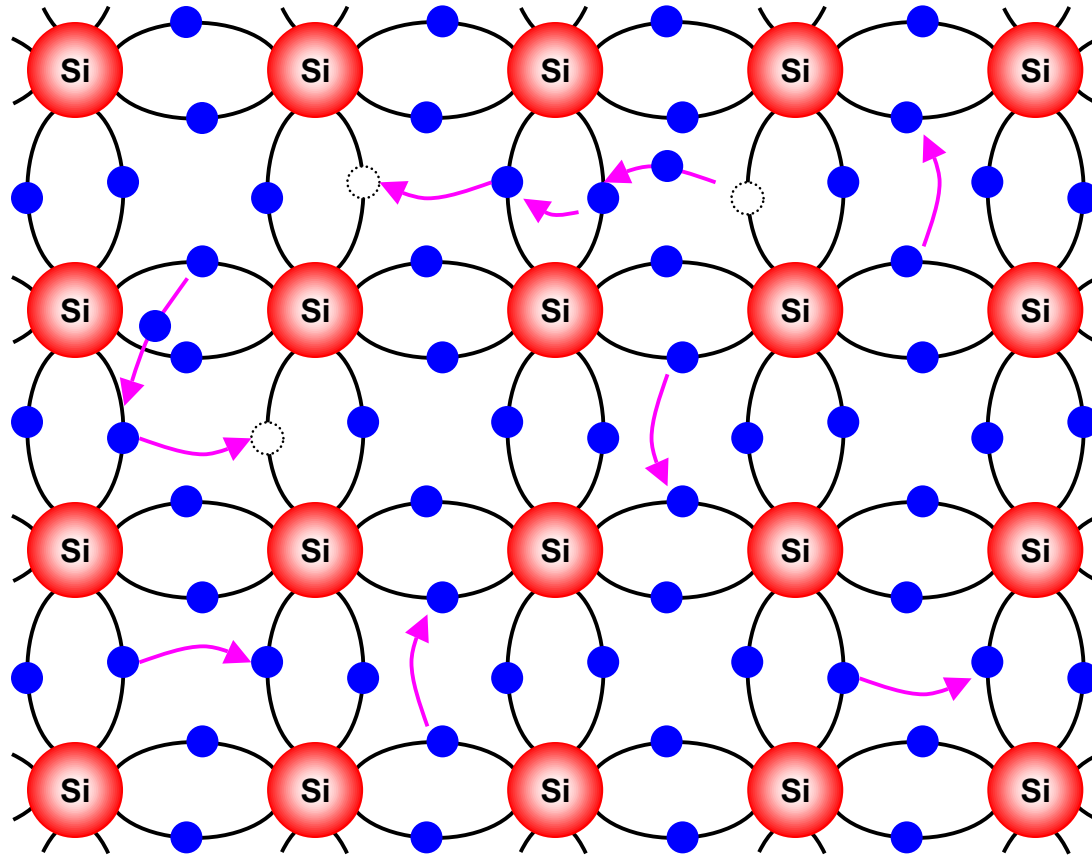
band structure



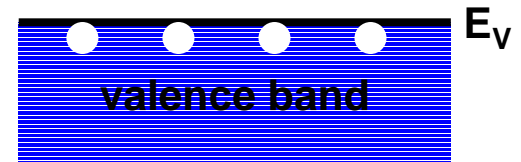
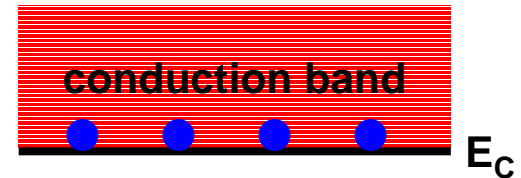
Si^{4+} (Ge^{4+}): 4 outer electrons (sp^3 -hybride) \Rightarrow no electrons in the conduction band*

Semiconductors

Electrical Conduction in Intrinsic Silicon at $T > 0$ K



band structure



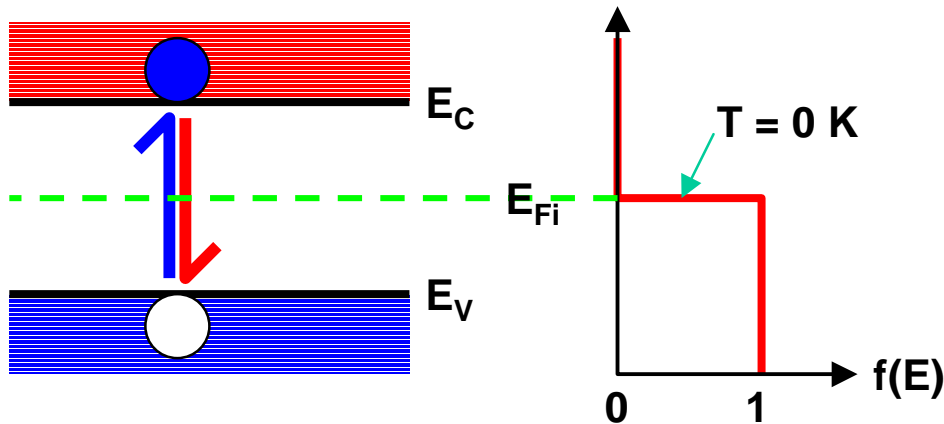
charge carriers at $T > 0$ K



- (mobile) electrons in the conduction band
- (mobile) holes in the valence band

Semiconductors

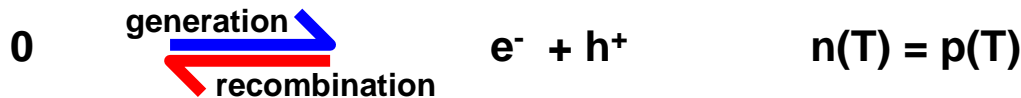
Charge Carriers in Intrinsic Semiconductors



$$f(E) = \frac{1}{1 + e^{\frac{E - E_{Fi}}{kT}}}$$

E_{Fi} : fermi-level for intrinsic semiconductor

- thermal equilibrium



- intrinsic charge carrier concentration n_i

$$n_i = n = p$$

n : (mobile) electrons in the conduction band

p : (mobile) holes in the valence band

Semiconductors

Charge Carrier Concentration and Fermi Level

- electron concentration n (conduction band)

$$n = N_C \cdot e^{\frac{-(E_C - E_{Fi})}{kT}}$$

$$N_C = 2 \cdot \left(\frac{2\pi \cdot m_n^* \cdot kT}{h^2} \right)^{\frac{3}{2}}$$

- hole concentration p (valence band)

$$p = N_V \cdot e^{\frac{-(E_{Fi} - E_V)}{kT}}$$

$$N_V = 2 \cdot \left(\frac{2\pi \cdot m_p^* \cdot kT}{h^2} \right)^{\frac{3}{2}}$$

- intrinsic charge carrier concentration n_i

$$n_i = N_{eff} \cdot e^{\frac{-E_g}{2kT}}$$

$$N_{eff} = \sqrt{N_C \cdot N_V}$$

- fermi level in an intrinsic semiconductor

$$E_{Fi} = E_V + \frac{1}{2} E_g + \frac{3}{4} kT \cdot \ln \frac{m_p^*}{m_n^*} \quad \text{with } E_g = E_C - E_V \quad \text{for } m_p^* = m_n^*$$

$$E_{Fi} = E_V + \frac{1}{2} E_g$$

Semiconductors

Intrinsic Conductivity

- **intrinsic conductivity by excitation of free electron-hole-pairs**

$$\sigma_i = n_i \cdot e_0 \cdot (\mu_n + \mu_p)$$

- **mobility of free electrons and holes**

$$\mu_n = \frac{e_0 \cdot \tau_n}{m_n^*}$$

$$\mu_p = \frac{e_0 \cdot \tau_p}{m_p^*}$$

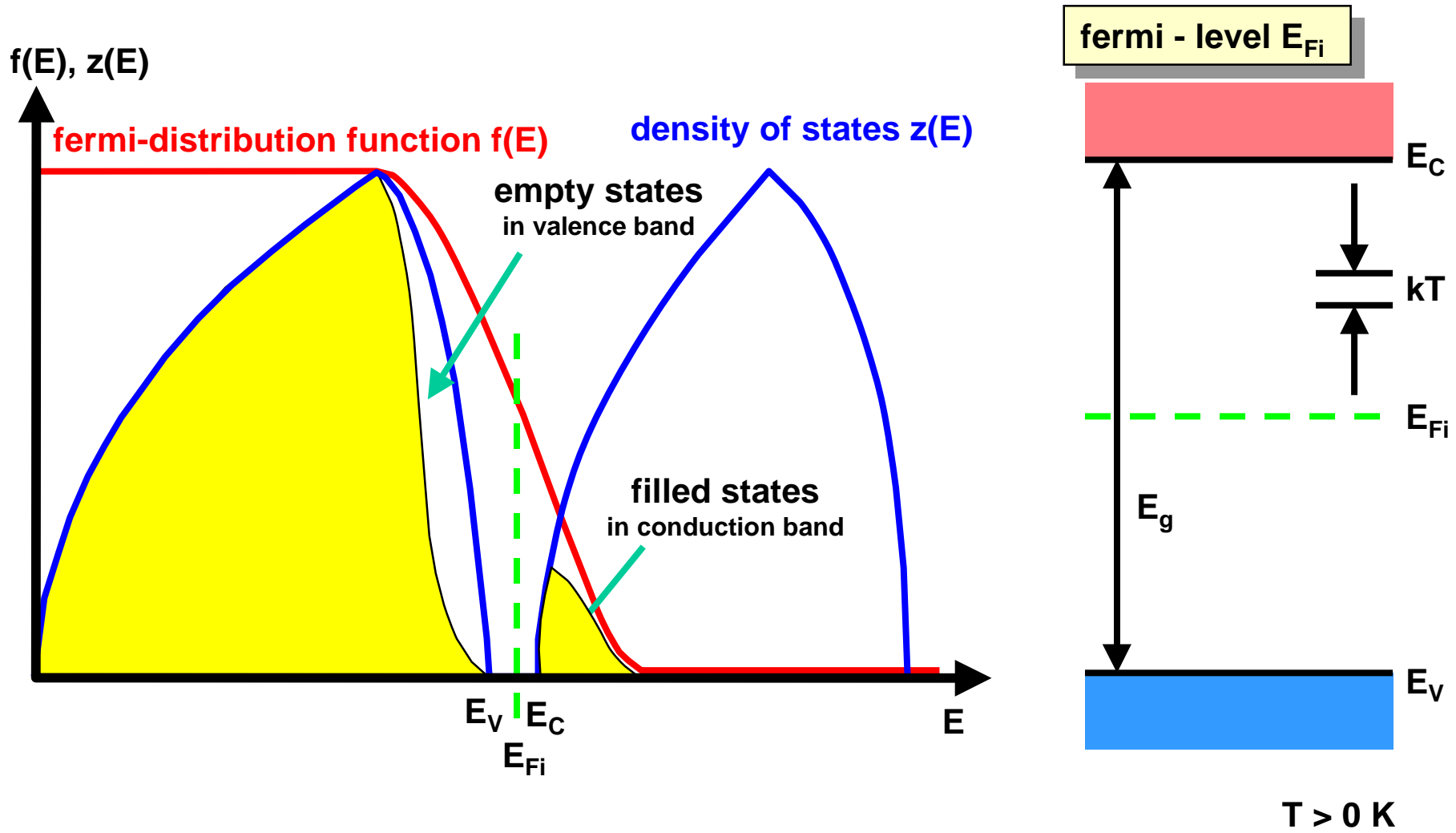
- **temperature dependence of electron and hole mobility**

$$\mu_n = T^{-\beta_n}$$

$$\mu_p = T^{-\beta_p}$$

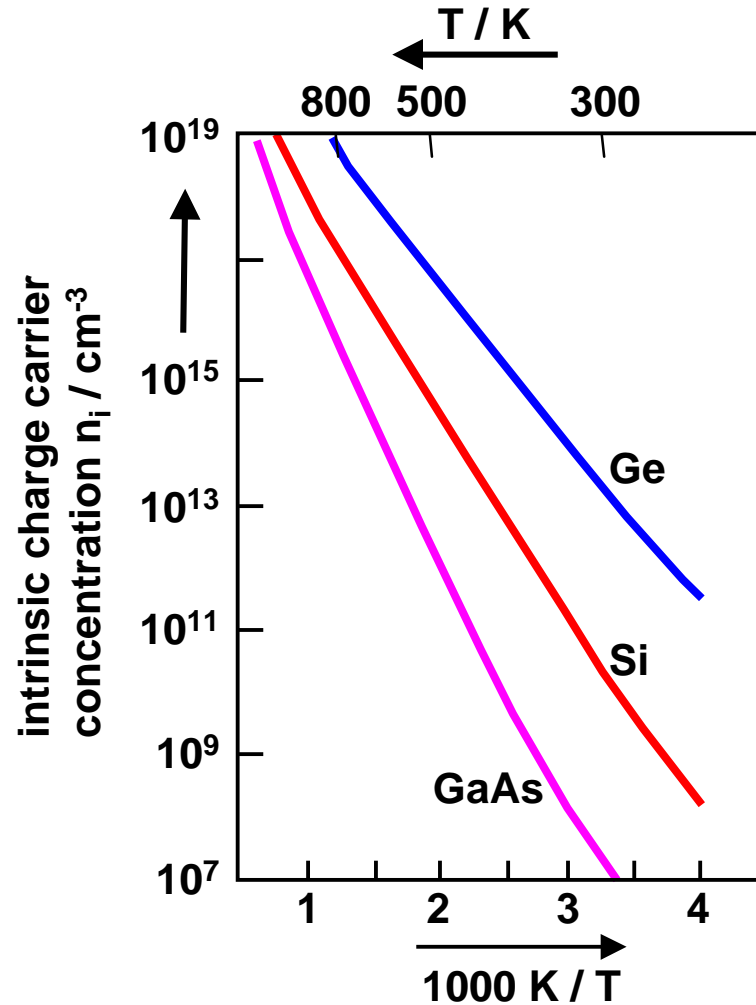
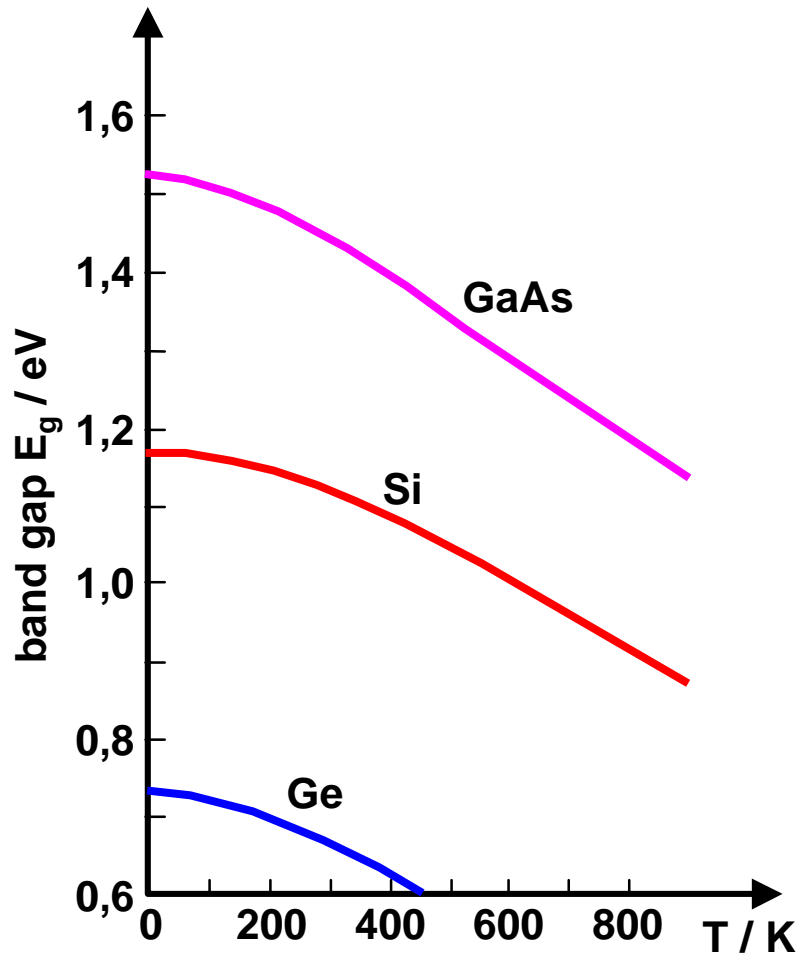
Semiconductors

Fermi Distribution Function, Density of States and filled Electron States



Semiconductors

Band Gap E_g and Concentration of Charge Carriers as $f(T)$



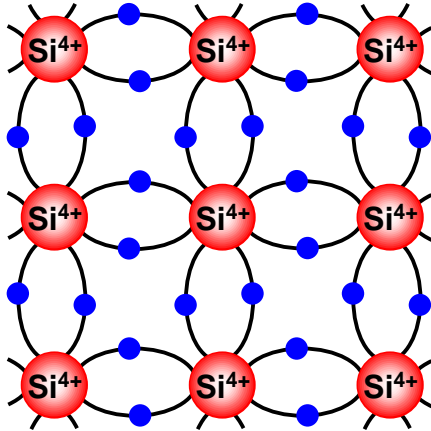
Semiconductors

Intrinsic and Extrinsic (n- and p-Type) Semiconductors

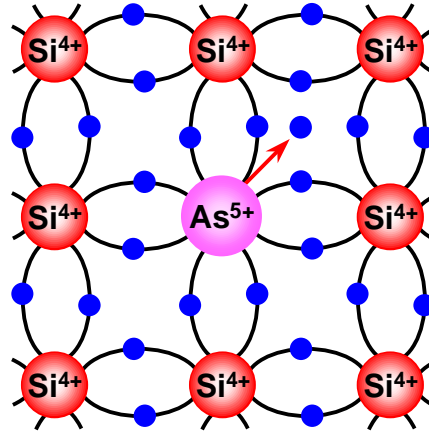
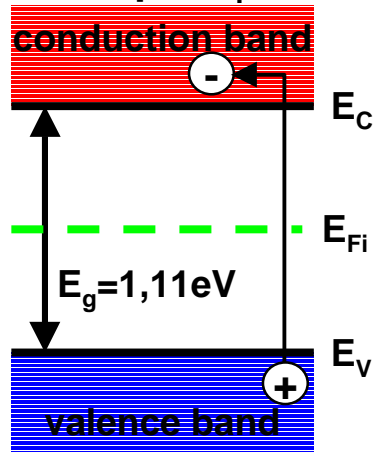
intrinsic semiconductor

extrinsic n-type (donor-doped)

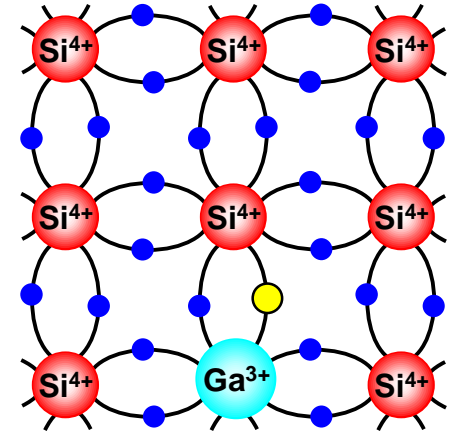
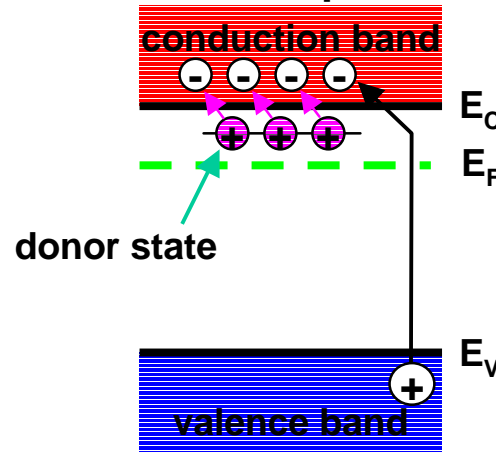
extrinsic p-type (acceptor-doped)



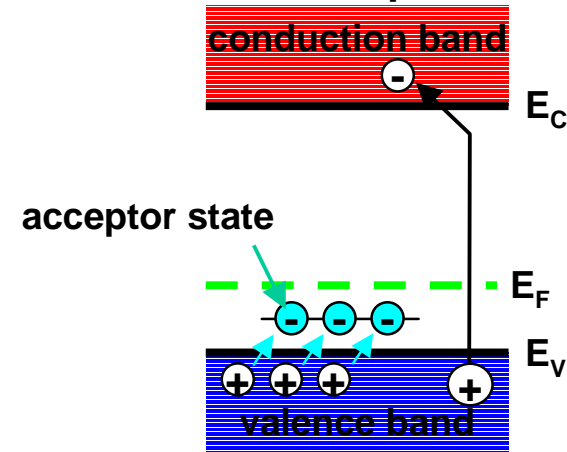
$$n = p = n_i$$



$$n \gg p$$



$$n \ll p$$



Semiconductors

Donors and Acceptors

donors

excitation from a donor state generates an electron in the conduction band

ionisation energy*:
$$\Delta E_D = \frac{m_n^* \cdot e_0^4}{2 \cdot (4\pi \cdot \epsilon_r \cdot \epsilon_0 \cdot \hbar)^2}$$

in Si: P	$\Delta E_D = 45 \text{ meV}$
Sb	$\Delta E_D = 39 \text{ meV}$
As	$\Delta E_D = 54 \text{ meV}$

acceptors

excitation from an acceptor state generates a hole in the valence band

ionisation energy*:
$$\Delta E_A = \frac{m_p^* \cdot e_0^4}{2 \cdot (4\pi \cdot \epsilon_r \cdot \epsilon_0 \cdot \hbar)^2}$$

in Si: B	$\Delta E_A = 45 \text{ meV}$
Al	$\Delta E_A = 67 \text{ meV}$
Ga	$\Delta E_A = 72 \text{ meV}$

* calculation using the hydrogen model $\text{H} \rightarrow \text{H}^+ + \text{e}^- \Rightarrow$

$$\Delta E_{\text{Ion}} = \frac{m_0 \cdot e_0^4}{2 \cdot (4\pi \cdot \epsilon_0 \cdot \hbar)^2} = 13,6 \text{ eV}$$

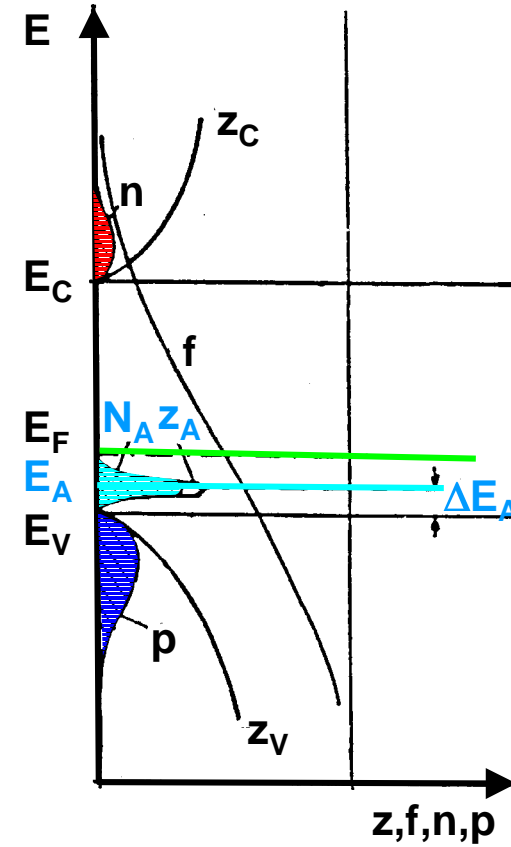
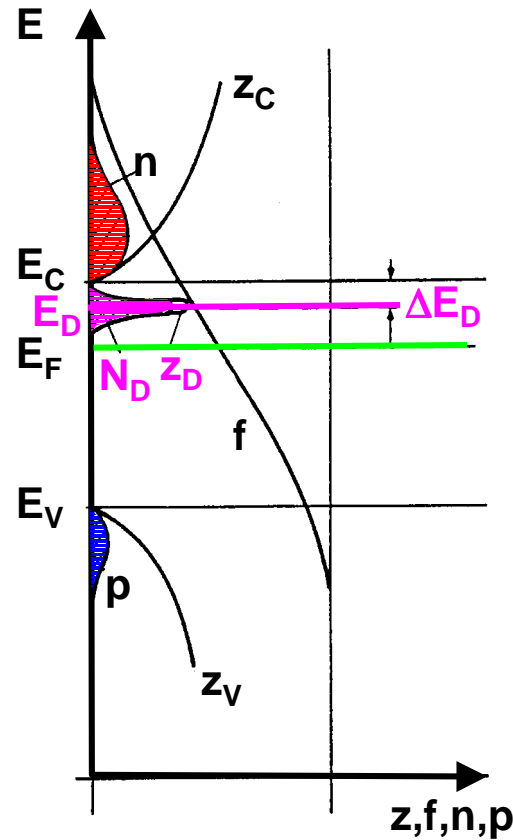
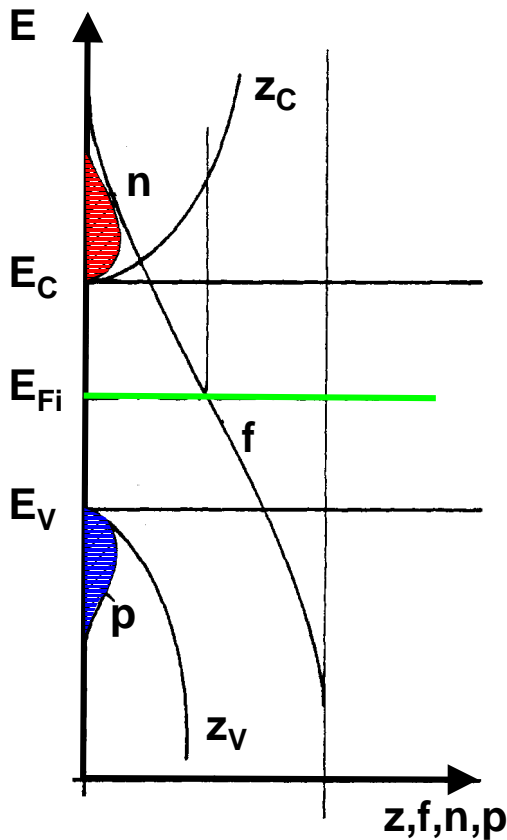
Semiconductors

Distribution Function $f(E)$, Density of States $z(E)$ and filled Electron States

intrinsic
 $n = p$

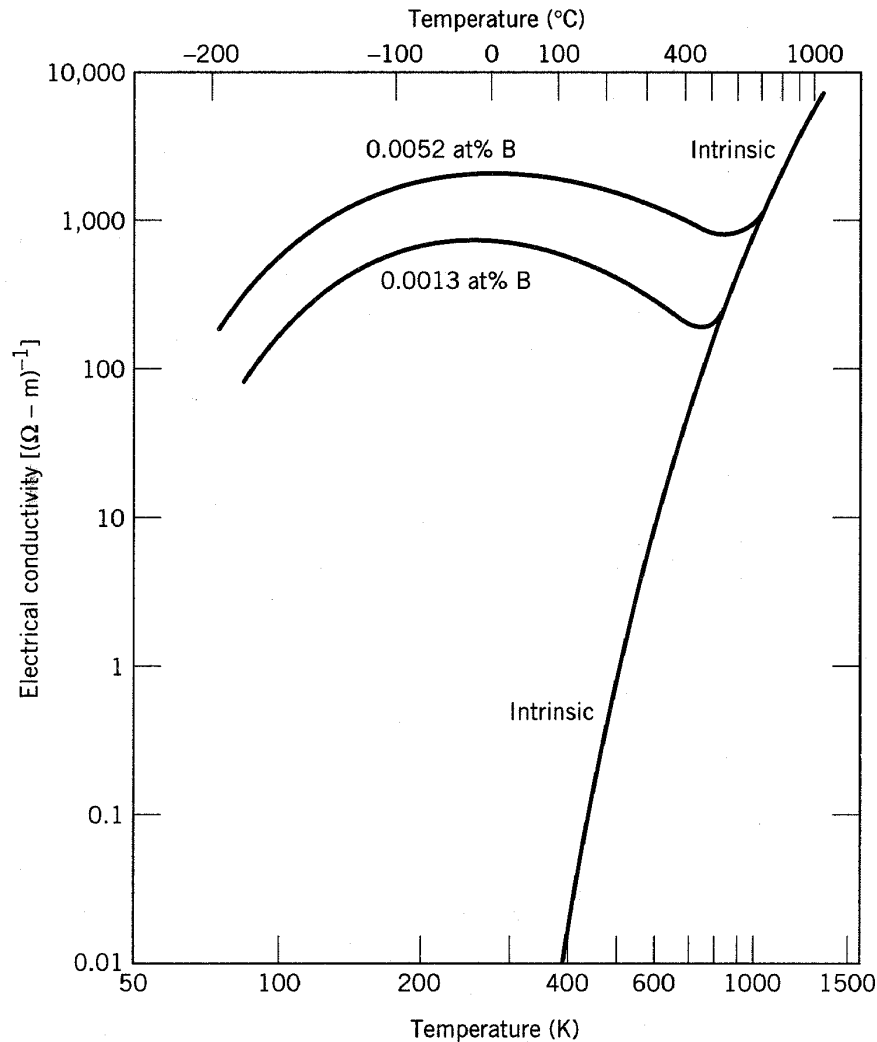
n-type (donor-doped)
 $n \gg p$

p-type (acceptor-doped)
 $p \gg n$



Semiconductors

Electrical Conductivity vs. Temperature



For intrinsic semiconduction:

$$\ln \sigma \cong C - \frac{E_g}{2kT}$$

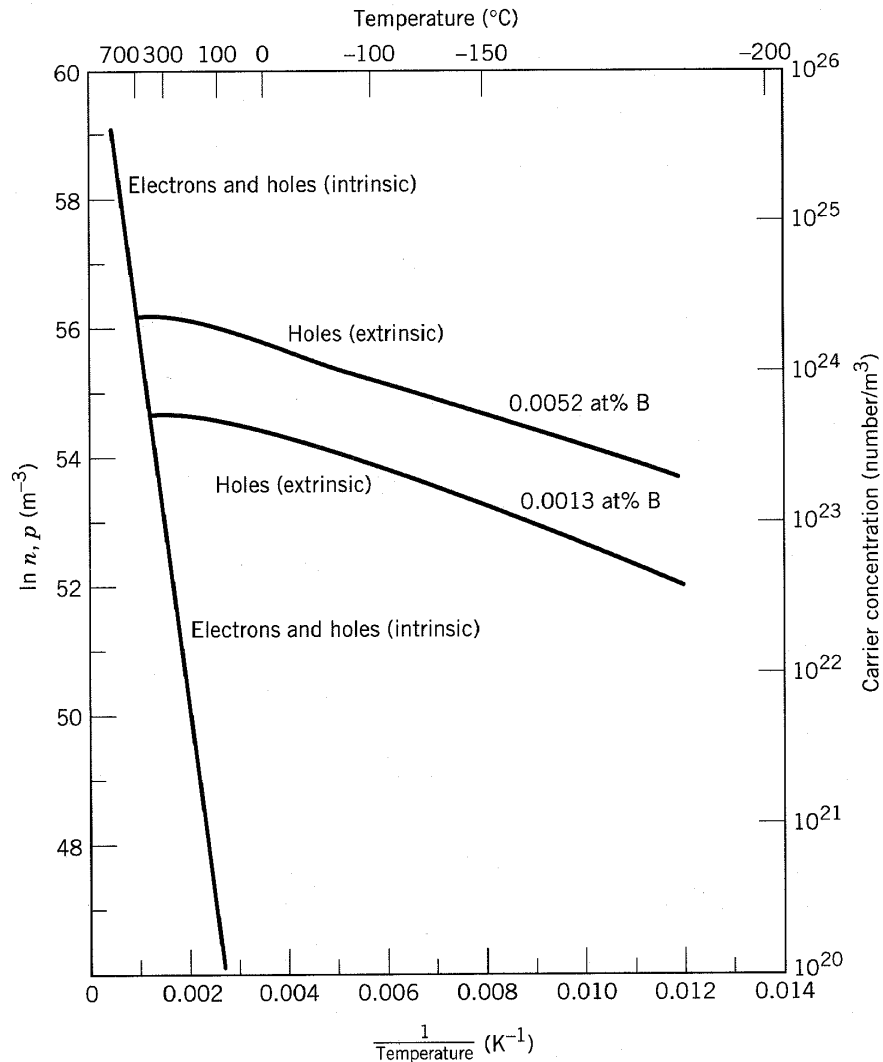
C - a temperature-independent constant

E_g - the band gap

k - Boltzmann's constant

Semiconductors

Charge Carrier Concentration vs. Reciprocal Temperature



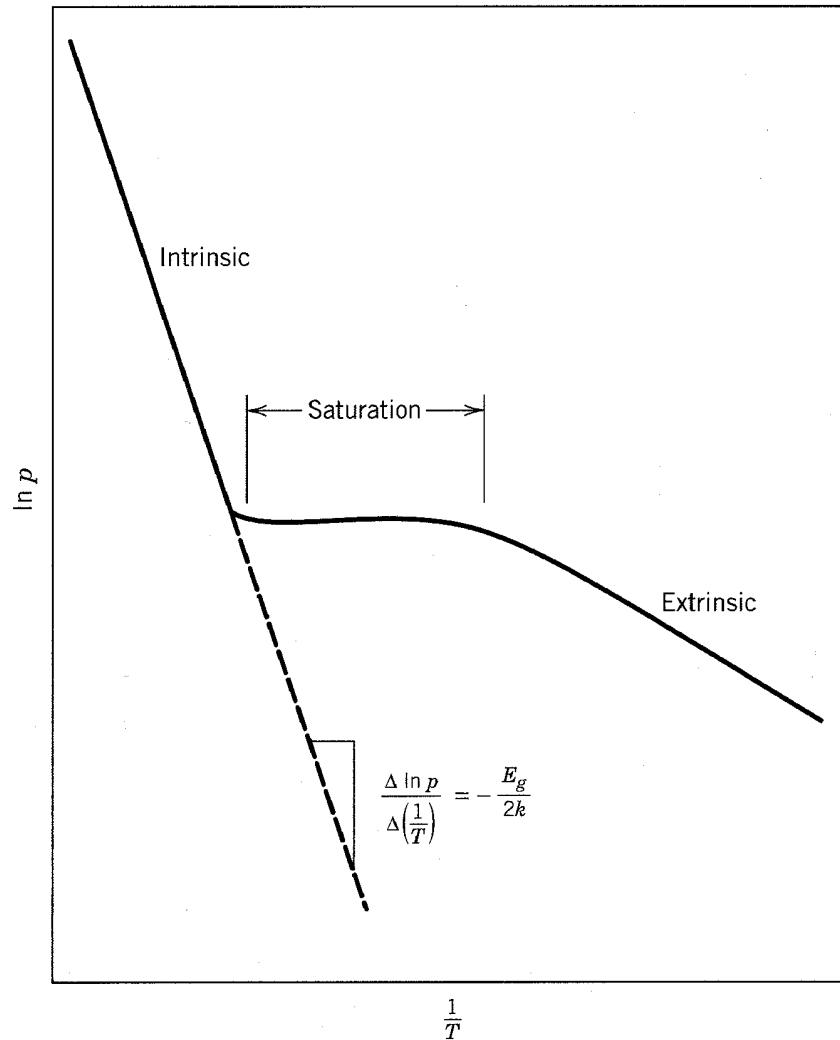
For intrinsic semiconduction:

$$\ln n = \ln p \cong C' - \frac{E_g}{2kT}$$

$$E_g = -2k \left(\frac{\Delta \ln p}{\Delta(1/T)} \right) = 2k \left(\frac{\Delta \ln n}{\Delta(1/T)} \right)$$

Semiconductors

Extrinsic, Saturation and Intrinsic Behavior vs. Reciprocal Temperature



p-type extrinsic semiconductor

Semiconductors

Intrinsic and Extrinsic Conduction

- **intrinsic conductivity ($n = p = n_i$)**

$$\sigma_i = n_i \cdot e_0 \cdot (\mu_n + \mu_p) = n \cdot e_0 \cdot (\mu_n + \mu_p) = p \cdot e_0 \cdot (\mu_n + \mu_p)$$

- **n-type intrinsic conductivity ($n \gg p, n \cdot p = n_i^2$)**

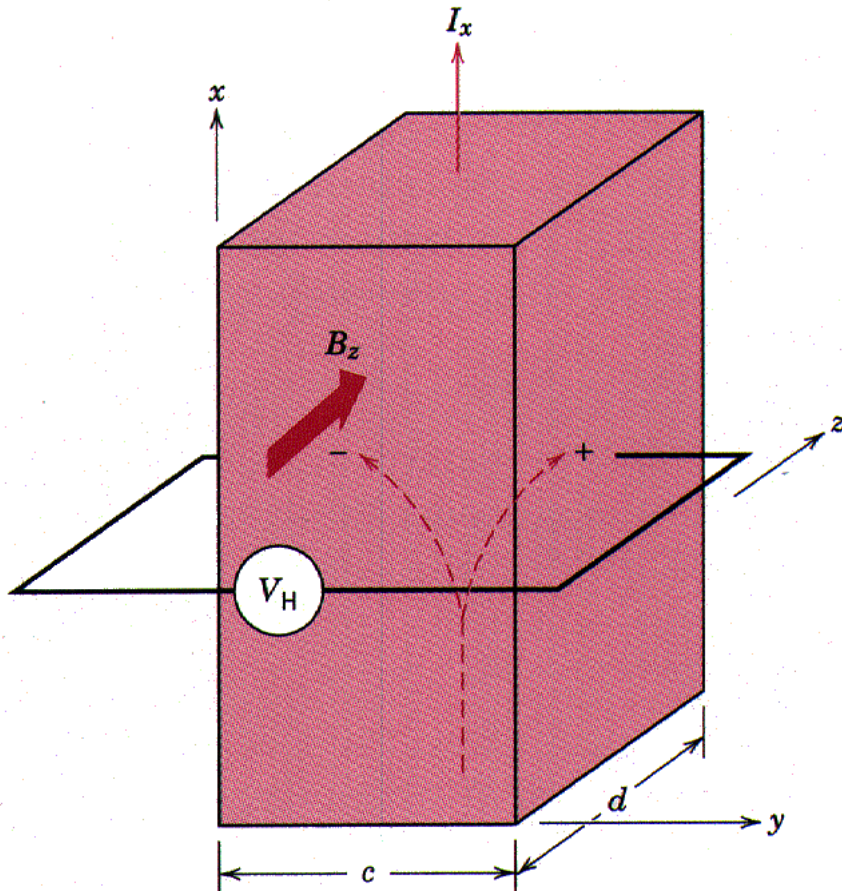
$$\sigma \cong n \cdot e_0 \cdot \mu_n$$

- **p-type intrinsic conductivity ($n \ll p, n \cdot p = n_i^2$)**

$$\sigma \cong p \cdot e_0 \cdot \mu_p$$

Semiconductors

Hall Effect Experiment



V_H : Hall voltage, depends on:

I_x : current

B_z : magnetic field

d : the specimen thickness

$$V_H = \frac{R_H \cdot I_x \cdot B_z}{d}$$

R_H : Hall coefficient (constant for a given material)

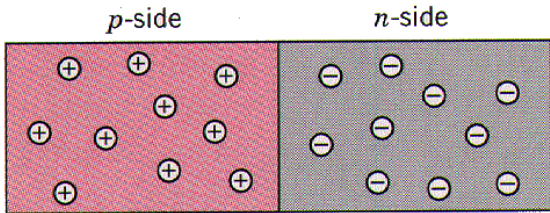
$R_H = 1/ne_0$, $\mu_n = |R_H| \cdot \sigma$, (n-type)

$R_H = -1/pe_0$, $\mu_p = |R_H| \cdot \sigma$, (p-type)

Determination of majority charge carrier type,
concentration and mobility

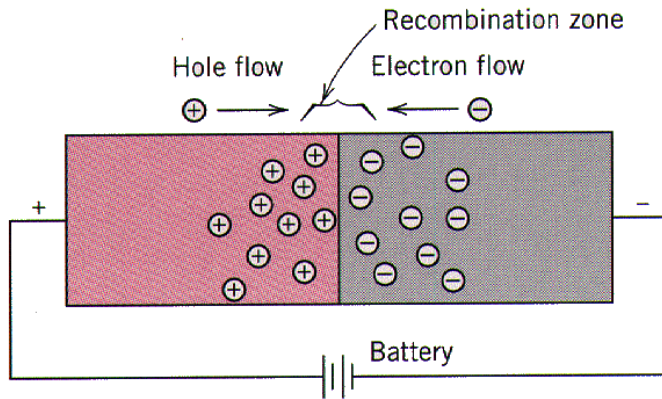
Semiconductors: Devices

p-n Rectifying Junction

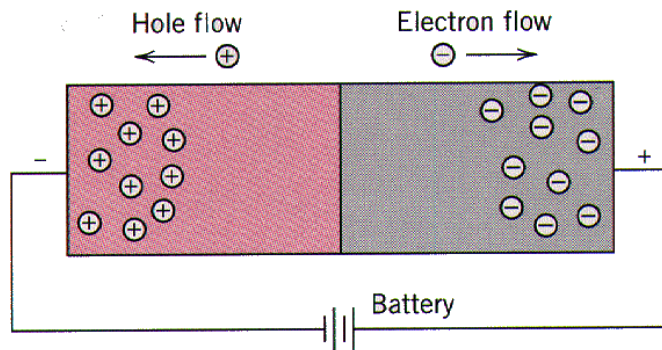


electron /hole distribution for:

no electrical potential



forward bias

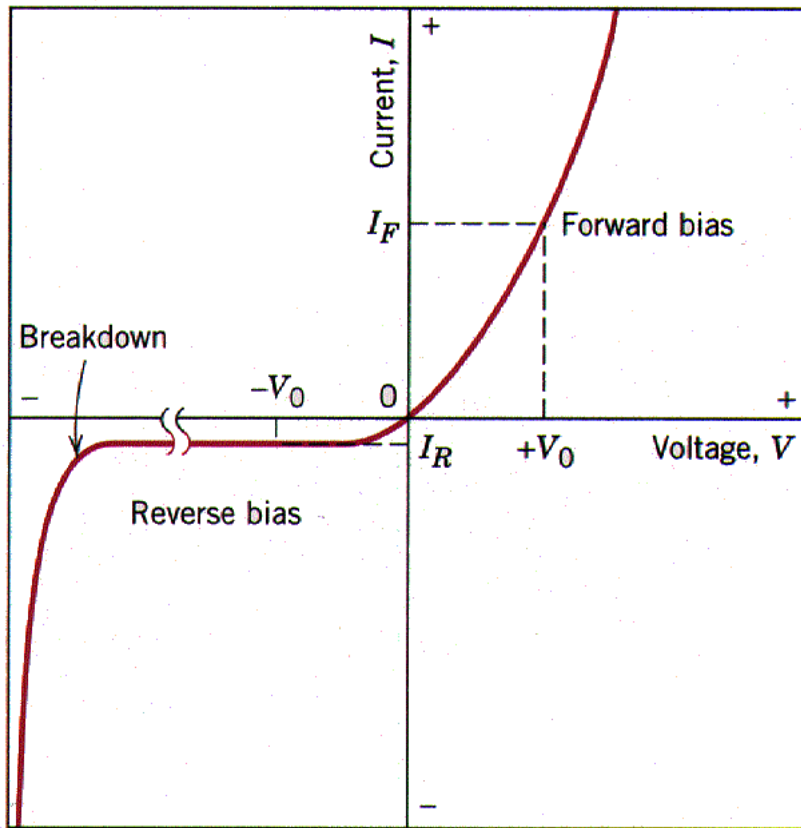


reverse bias

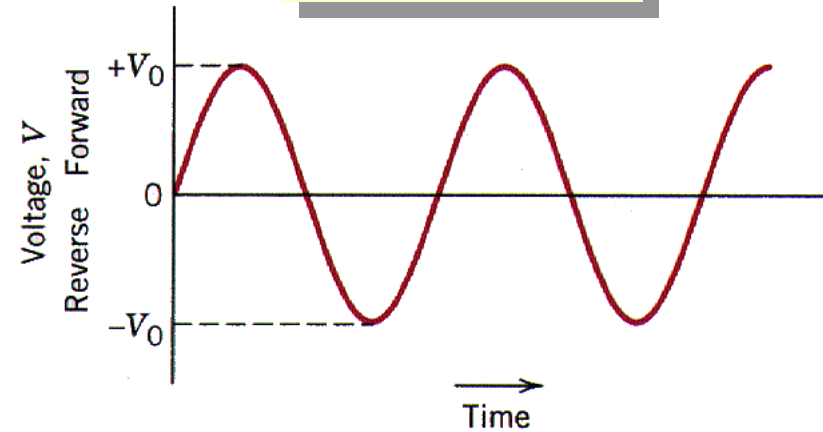
Semiconductors: Devices

p-n Rectifying Junction

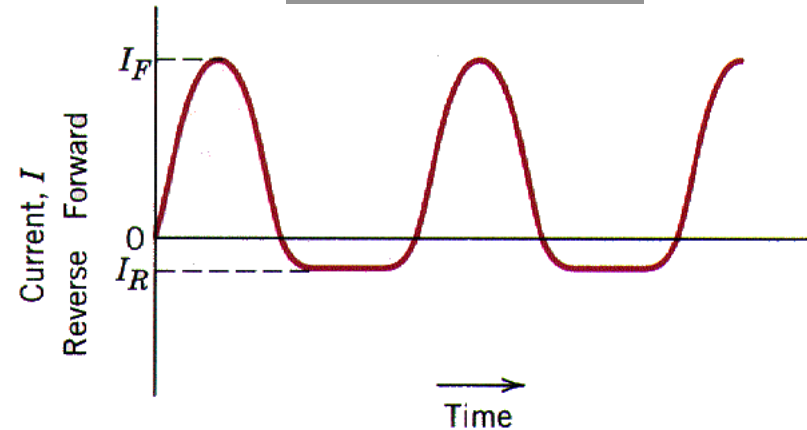
current - voltage characteristics



voltage vs. time



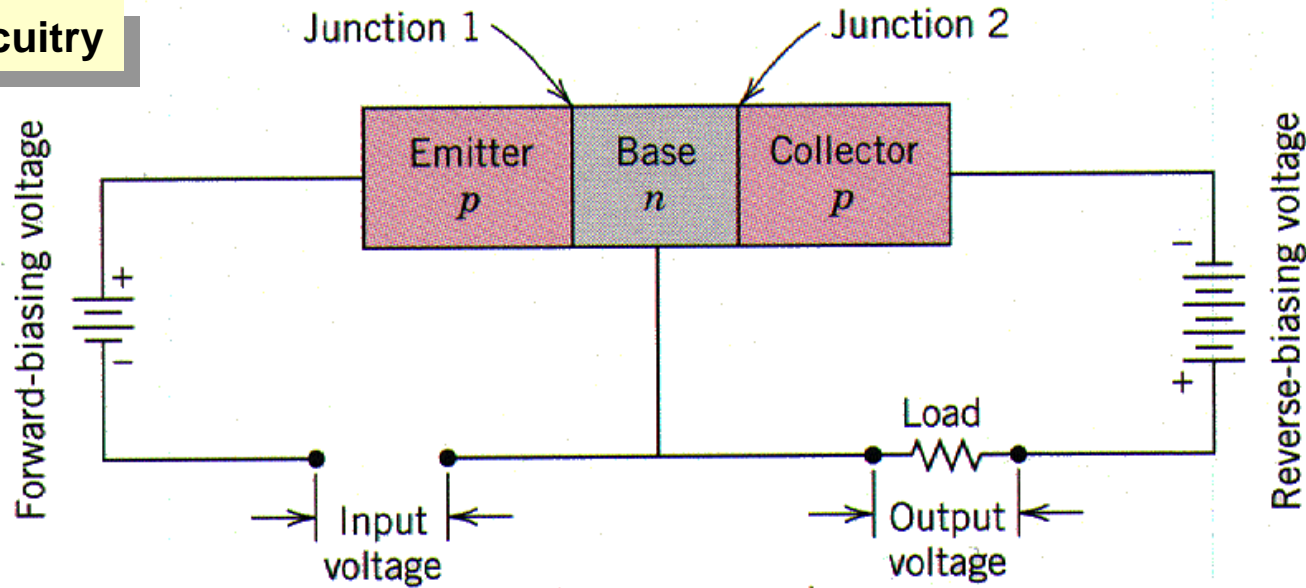
current vs. time



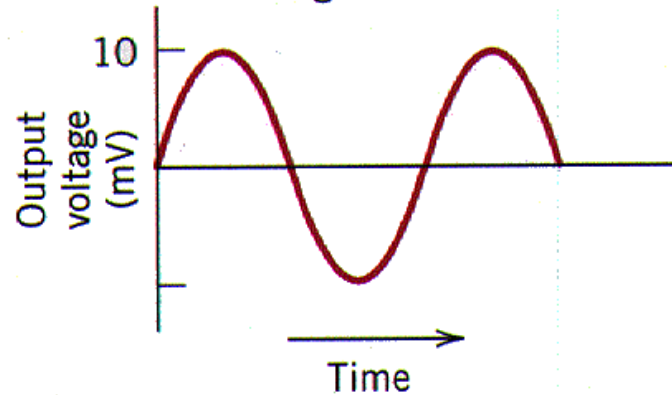
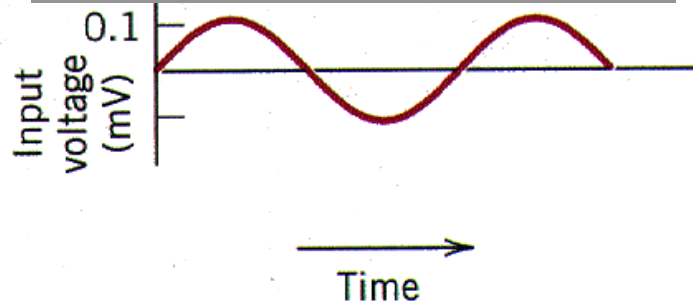
Semiconductors: Devices

p-n-p Junction Transistor

circuitry



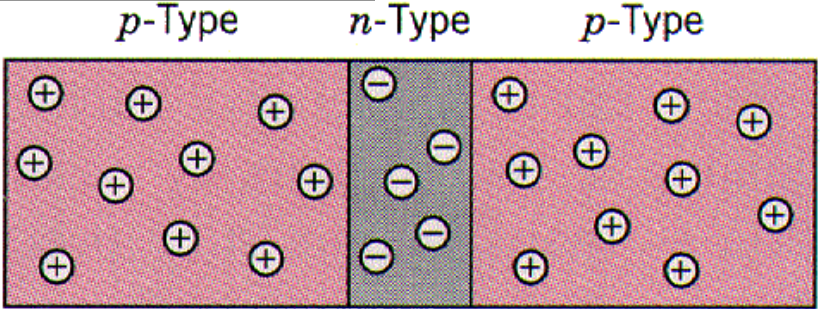
Input / output voltage vs. time



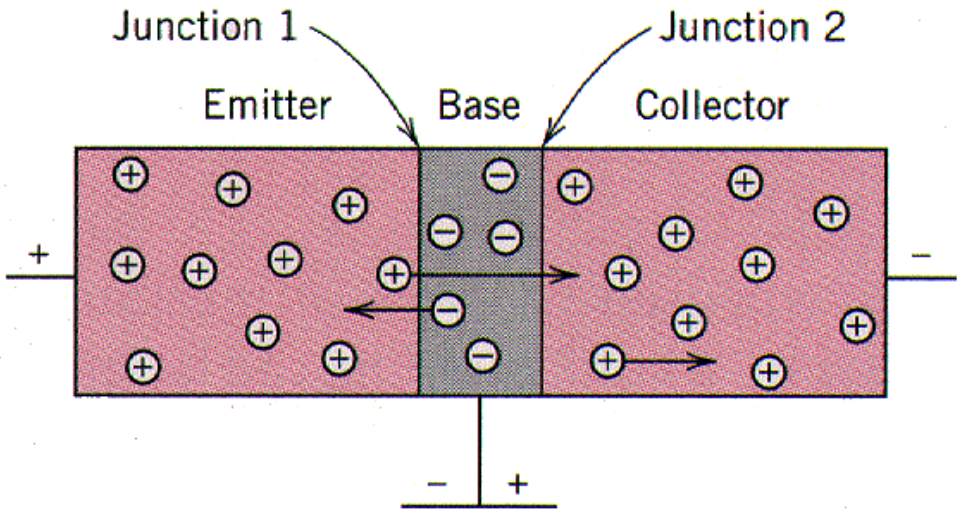
Semiconductors: Devices

p-n-p Junction Transistor

no potential applied

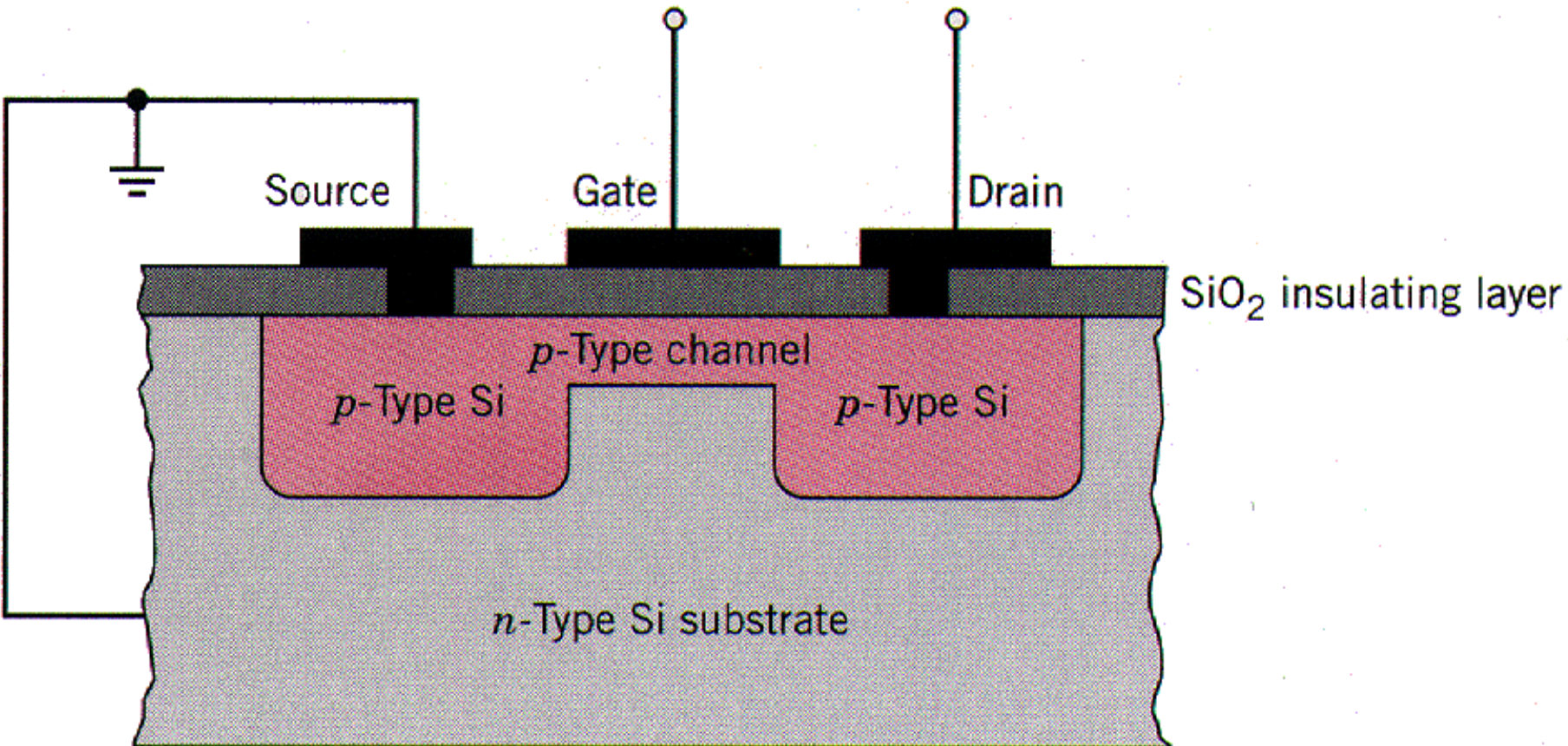


bias applied



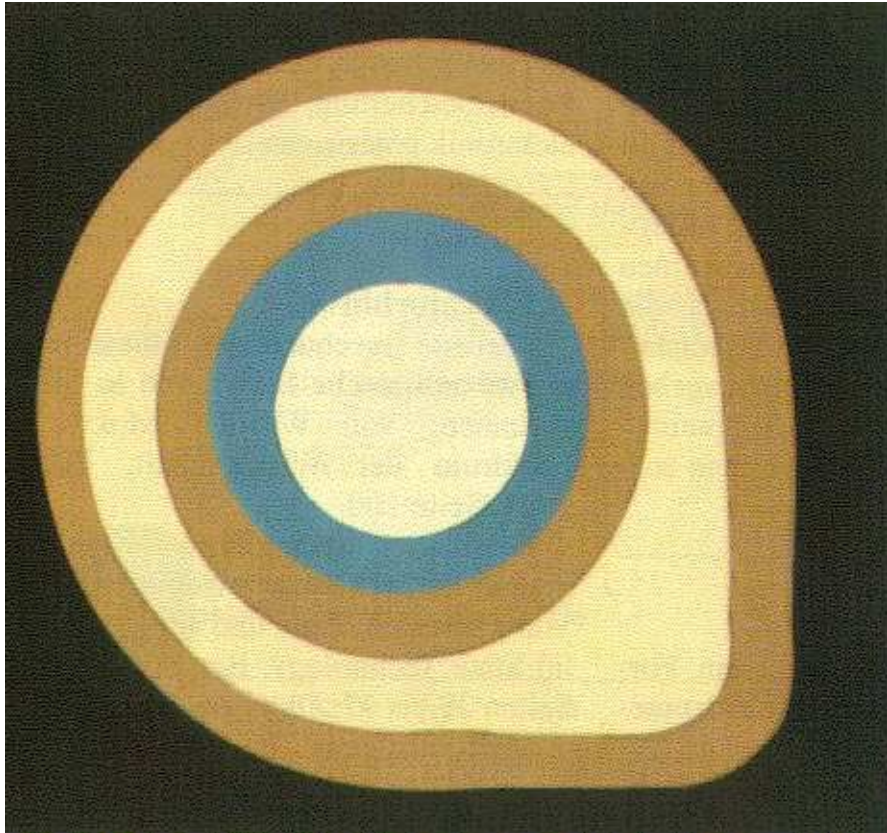
Semiconductors: Devices

MOSFET-Transistor



Semiconductors

Development of Microelectronics



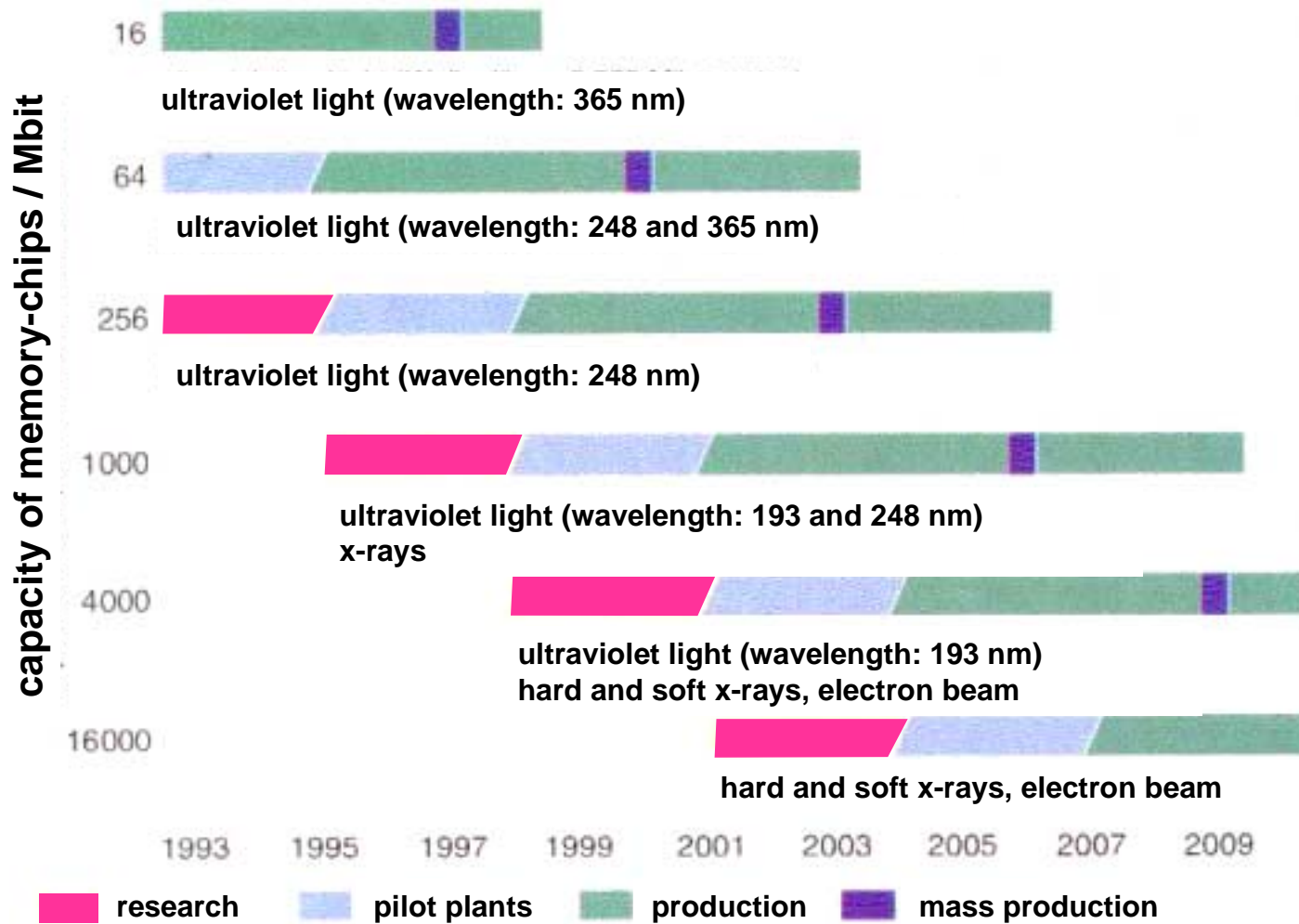
1959: 1st planar transistor
 \varnothing 764 μm



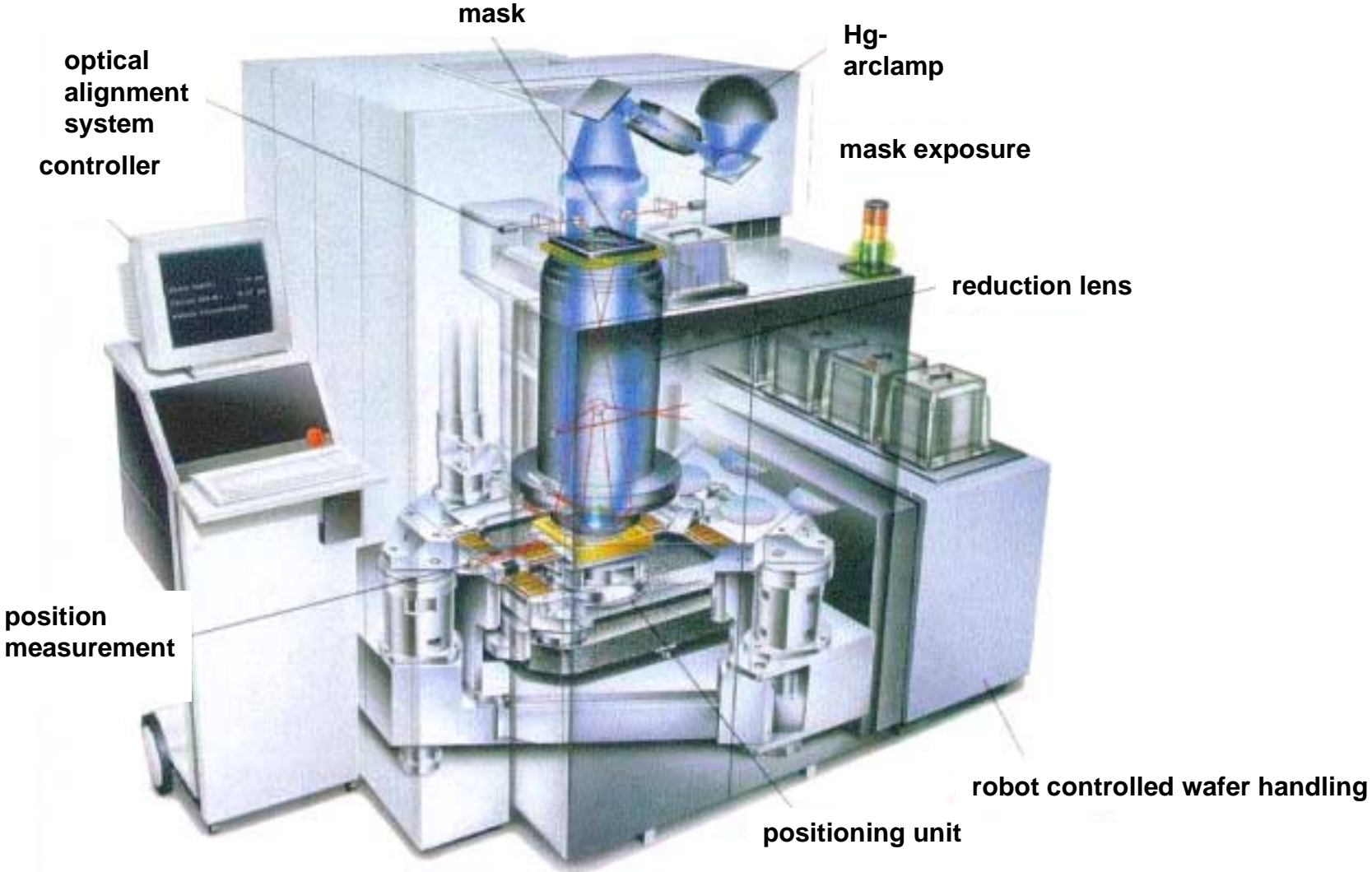
1995: transistor structures
between 0,4 and 1,3 μm

Semiconductors

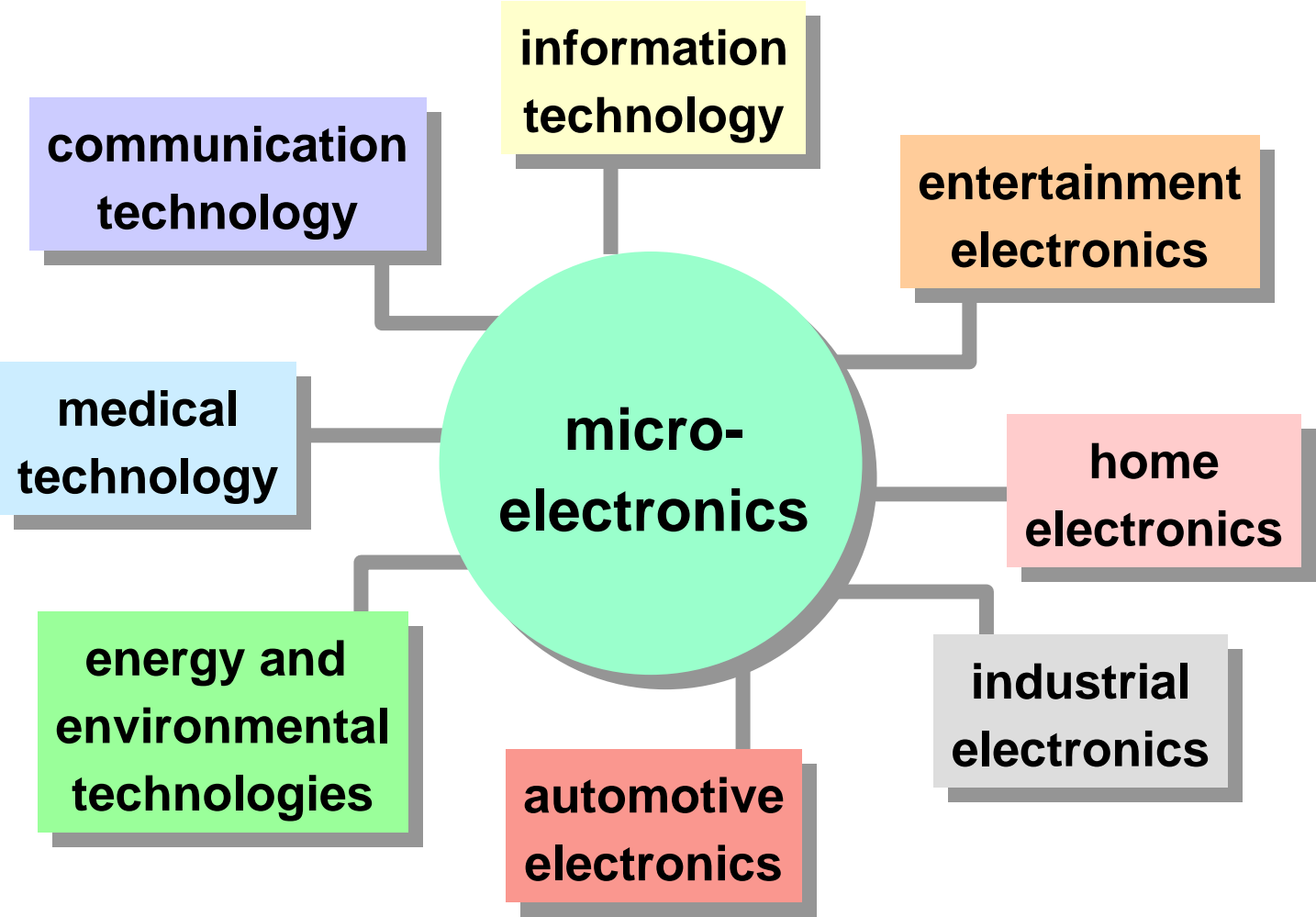
Development of Lithography Technology



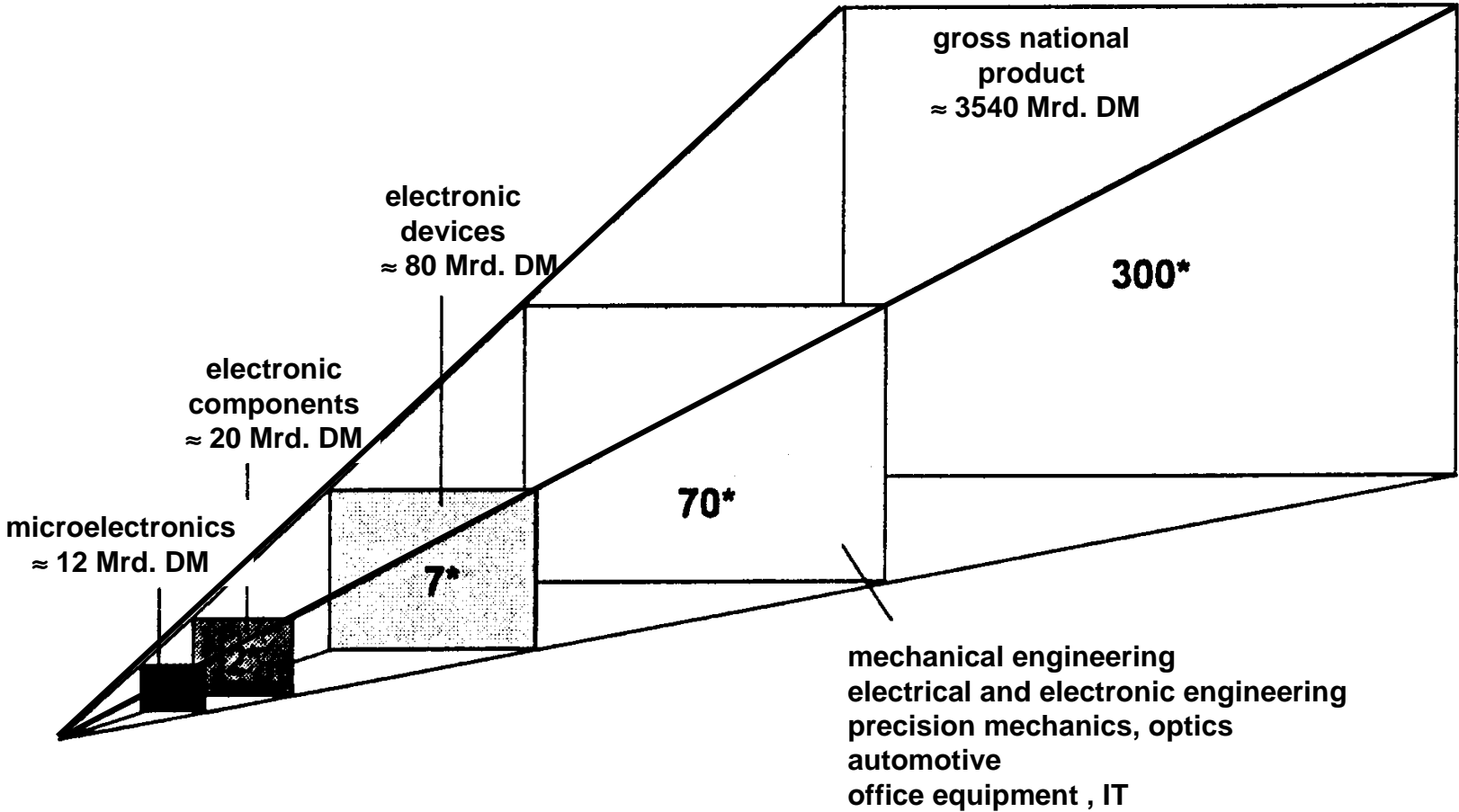
Semiconductors Photolithography System



Semiconductors



Semiconductors Sales 1996



*compared to microelectronics

Quelle: GMM

Semiconductors

Development of Integration

