Solving optimization problems

The objectives of the task: Strengthen the skills of the solution of linear programming problems.

Task Requirements: Solve linear programming problems.

Instructions for performing:

- 1. Creat matrix of left side of inequalities A. 0.4 points
- 2. Creat matrix of free coefficients of inequalities **b**. 0.4 points
- 3. Create matrix of the objective function **c**. 0.4 points
- 4. Create matrix of boundary conditions **lb** and **ub**. 0.4 points
- 5. Solve linear programming problem with help **karmarkar**. 0.6 points
- 6. Output to the command window the result. 0.4 points
- 7. Available Comments 0.4 points.

Maximum evaluation are 3 points

You need to create a script file with all matrixs and solution, then obtain result in the command window. After that, then you need you should make a scan of the command window and send me the script file and the scan with result.

Criteria for evaluation: Available Comments, no mistakes.

Variants of tasks.

1.
$$W = 2x_1 - x_2 + x_4 \rightarrow \min$$

$$\begin{cases} x_1 + x_2 + x_3 - x_4 \leqslant 1 \\ x_1 - x_2 + x_3 - x_4 \leqslant 0 \\ 2x_1 + x_2 + x_3 - x_4 \geqslant 3 \end{cases}$$

$$2. \ W = x_1 + x_3 \to \max \\ \begin{cases} 2x_1 - 7x_2 + 22x_3 \leqslant 22 \\ 2x_1 - x_2 + 6x_3 \leqslant 6 \\ 2x_1 - 5x_2 + 2x_3 \leqslant 2 \\ -4x_1 + x_2 + x_3 \leqslant 1 \end{cases}$$

$$3. \ W = 3 + 2x_2 + x_3 \rightarrow \max \\ \begin{cases} x_1 - x_2 + 2x_3 + x_4 \geqslant 1 \\ 2x_1 - x_2 + x_3 - x_4 \geqslant 1 \\ x_1 - 2x_2 + x_3 - x_4 \geqslant -1 \\ x_1 + x_2 + x_3 + 2x_4 \leqslant 5 \end{cases}$$

4.
$$W = x_3 + 3x_4 \rightarrow \min$$

$$\begin{cases}
x_1 + x_2 - x_3 - x_4 \leqslant 2 \\
x_1 - x_2 - x_3 + x_4 \geqslant 0 \\
-x_1 - x_2 + 2x_3 - x_4 \geqslant -3 \\
x_1 \geqslant 1
\end{cases}$$

5.
$$W = -x_1 + x_2 \rightarrow \max$$

$$\begin{cases} x_1 - 2x_2 \ge 2 \\ 2x_1 - x_2 \ge 2 \\ x_1 + x_2 \ge 5 \end{cases}$$

$$6. \ W = x_1 - x_2 - 2x_4 \rightarrow \max \\ \begin{cases} 2x_1 - x_2 + 2x_3 - x_4 \leqslant 4 \\ x_1 - 2x_2 + x_3 - 2x_4 \geqslant 2 \\ x_1 - x_4 \geqslant 1 \\ x_2 + x_3 \leqslant 1 \end{cases}$$

7.
$$W = x_1 - x_2 + 3x_3 + x_4 \rightarrow \max$$

$$\begin{cases} x_1 - x_2 + x_4 \leqslant 1 \\ x_2 - x_3 + x_4 \leqslant 1 \\ x_1 + x_3 + 2x_4 \leqslant 2 \\ -2x_2 + x_4 \leqslant 0 \end{cases}$$

8.
$$W = -x_2 - 2x_3 + x_4 \rightarrow \min$$

$$\begin{cases}
3x_1 - x_2 \leqslant 2 \\
x_2 - 2x_3 \leqslant -1 \\
4x_3 - x_4 \leqslant 3 \\
5x_1 + x_4 \geqslant 6
\end{cases}$$

9.
$$W = x_1 + x_2 + 3x_3 - x_4 \rightarrow \max$$

$$\begin{cases}
x_1 - 5x_2 + 4x_3 \leq 5 \\
x_1 - 2x_2 - 3x_3 \leq 4 \\
x_1 + 6x_2 + 5x_3 \leq 4 \\
x_2 + x_3 \leq 1
\end{cases}$$

10.
$$W = -4 - 2x_1 - x_2 - x_3 \rightarrow \min$$

$$\begin{cases}
x_1 - 2x_2 + 3x_3 - 4x_4 \geqslant -10 \\
x_1 + x_2 - x_3 - x_4 \leqslant -4 \\
x_1 - x_2 + x_3 - x_4 \geqslant -6 \\
x_1 + x_2 + x_3 + x_4 \leqslant 10
\end{cases}$$

$$11. \begin{tabular}{l} W = x_1 + x_2 + x_3 + 1 \to \min \\ & \begin{cases} x_1 + x_2 \geqslant 0 \\ x_1 + x_3 \geqslant 1 \\ x_2 - x_3 \geqslant 1 \\ x_1 + 2x_2 + 3x_3 \geqslant 0 \\ \end{tabular}$$

12.
$$W = 2 + 2x_2 - x_3 + 3x_4 \rightarrow \max$$

$$\begin{cases}
-x_1 + x_2 - 2x_4 \geqslant -1 \\
x_1 + x_3 + x_4 \geqslant 1 \\
x_2 + x_3 - x_4 \geqslant 1 \\
x_3 \leqslant 4; \quad x_2 \leqslant 10
\end{cases}$$

13.
$$W = x_1 + x_2 + 3 \rightarrow \max$$

$$\begin{cases}
x_1 - x_2 \leqslant 1 \\
x_1 - 2x_2 \geqslant -2 \\
-x_1 + x_2 \geqslant -1 \\
2x_1 + x_2 \geqslant -2
\end{cases}$$

14.
$$W = x_1 - 10x_2 + 100x_3 \rightarrow \max$$

$$\begin{cases}
x_1 + x_2 + x_3 \leq 1 \\
x_1 - x_2 - x_3 \leq 2 \\
-x_1 + 2x_3 \leq 0 \\
x_1 + 2x_3 \leq 5
\end{cases}$$

$$\begin{array}{ll} 15. \ W = -3 + x_1 + 3x_2 + 5x_3 \to \max \\ \left\{ \begin{array}{l} x_1 - x_2 + x_3 \leqslant 1 \\ 2x_1 + x_2 + x_3 \leqslant 1 \\ x_1 + 2x_2 + x_3 \leqslant 1 \\ x_1 + x_2 + 2x_3 \leqslant 1 \end{array} \right. \end{array}$$