

Tomsk Polytechnic University

PHYSICS I
Reports on Laboratory Experiments

Tomsk 2000

PHYSICS I

Reports on Laboratory Experiments

Mechanics and Molecular Physics

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All the laboratory experiments must be performed in the TPU Physics Laboratory. The estimation of students' laboratory activity is based on their ability to perform the laboratory experiment and to present the results in conventional format. The report must be carefully prepared. It must include all the measurements and calculations.

List of laboratory experiments

1. Measuring the linear dimensions of a body
2. Measuring the free fall acceleration
3. Determining the coefficient of sliding friction
4. Studying the distribution function of random variables
5. Elastic and inelastic collisions of balls
6. Studying dynamics laws with Athwood's machine
7. Determining the mean free path and the effective diameter of a molecule

Report on laboratory experiment No. 1

Measuring the linear dimensions of a body

The **objective** is to measure the linear dimensions of a body, to calculate its volume, and to estimate absolute and relative measurement errors

THEORY

There are two kinds of measurements:

direct _____

indirect _____

and two types of errors:

systematic _____

random _____

To measure the linear dimensions of a body, you can use _____

Principal scales of these devices are base rules and vernier calipers.

Vernier caliper is _____

One subdivision of the vernier caliper corresponds to $\frac{m-1}{m} = \left(1 - \frac{1}{m}\right)$

subdivisions of the basic ruler, where

m is _____

With the help of the vernier caliper, measurements are carried out with the accuracy

$\Delta x = y - x = \frac{y}{m}$, where _____

y _____

x _____

The accuracy of the vernier caliper is $\frac{y}{m} =$ _____ mm.

The length L measured by this device is $L = ky + n \frac{y}{m}$, where

k is _____

n is _____

The accuracy of the measuring scale of a micrometer caliper is $\frac{y}{m} =$ _____ mm.

Calculation formulas

The volume of a parallelepiped is $V_P =$

where a b c

The volume of a cylinder is $V_C =$

where

d h

Data of measurements

Table 1

No.	a , mm	b , mm	c , mm	V_p , mm^3	Δa , mm	Δb mm	Δc mm	ΔV_p , mm^3
1								
2								
3								
4								
5								
Average								

The values of _____ are measured by a vernier caliper with accuracy _____ mm, and the values of _____ are measured by a micrometer caliper with accuracy _____ mm.

Table 2

No.	D , mm	h , mm	V_C , mm^3	ΔD , mm	Δh , mm	ΔV_C , mm^3
1						
2						
3						
Average						

Error analysis

Errors in direct measurements

1. Calculate the average value of a (the number of measurements $n = 5$)

$\bar{a} =$

2. Calculate the standard deviation for these measurements

$\sigma_{\bar{a}} =$

3. Calculate the random error $\Delta\bar{a}_r =$

where $\alpha =$ _____ $t_{\alpha,n}$ _____

Find $t_{\alpha,n}$ from the table of Student's coefficients

with $\alpha = 0.95$ and $n = 5$ $t_{\alpha,n} =$

4. Calculate the error of individual measurement

$\Delta\bar{a}_{i.m} =$ _____ where ℓ_a

The value of \bar{a} is _____ so $\ell_a =$ _____ mm.

In a similar manner, calculate averages of $b, C, D,$ and h .

Error in individual measurement

b

1. The average for $n = 5$ is

$$\bar{b} =$$

2. The standard deviation is

$$\sigma_{\bar{b}} =$$

3. The random error is

$$\Delta\bar{b}_r =$$

$$\alpha =$$

$$t_{\alpha,n} =$$

4. The error in individual measurement

is $\Delta\bar{b}_{i.m} =$

where $\ell_{\bar{b}} =$

\bar{b} is measured by _____,

hence $\ell_{\bar{b}} =$ _____ mm.

5. The total error is

$$\Delta\bar{b} =$$

D

1. The average for $n = 3$ is

$$\bar{D} =$$

2. The standard deviation is

$$\sigma_{\bar{D}} =$$

3. The random error is

$$\Delta\bar{D}_r =$$

$$\alpha =$$

$$t_{\alpha,n} =$$

4. The error in individual measurement

is $\Delta\bar{D}_{i.m} =$

where $\ell_{\bar{D}} =$

\bar{D} is measured by _____,

hence $\ell_{\bar{D}} =$ _____ mm.

5. The total error is

$$\Delta\bar{D} =$$

C

1. The average for $n = 5$ is

$$\bar{C} =$$

2. The standard deviation is

$$\sigma_{\bar{C}} =$$

h

1. The average for $n = 3$ is

$$\bar{h} =$$

2. The standard deviation is

$$\sigma_{\bar{h}} =$$

3. The random error is

$$\Delta \bar{C}_r =$$

$$\alpha =$$

$$t_{\alpha, n} =$$

4. The error in individual measurement

$$\text{is } \Delta \bar{C}_{i.m} =$$

$$\text{where } \ell_{\bar{C}} =$$

\bar{C} is measured by _____,

$$\text{hence } \ell_{\bar{C}} = \text{_____ mm.}$$

5. The total error is

$$\Delta \bar{C} =$$

3. The random error is

$$\Delta \bar{h}_r =$$

$$\alpha =$$

$$t_{\alpha, n} =$$

4. The error in individual measurement

$$\text{is } \Delta \bar{h}_{i.m} =$$

$$\text{where } \ell_{\bar{h}} =$$

\bar{h} is measured by _____,

$$\text{hence } \ell_{\bar{h}} = \text{_____ mm.}$$

5. The total error is

$$\Delta \bar{h} =$$

Relative error

(according to tutor's instruction)

Parallelepiped

$$\frac{\Delta \bar{V}_p}{\bar{V}_p} = \sqrt{\left(\frac{\Delta \bar{a}}{\bar{a}}\right)^2 + \left(\frac{\Delta \bar{b}}{\bar{b}}\right)^2 + \left(\frac{\Delta \bar{c}}{\bar{c}}\right)^2}, \text{ where}$$

$\Delta \bar{a}$, $\Delta \bar{b}$, and $\Delta \bar{c}$ are the total errors in direct measurements of \bar{a} , \bar{b} , and \bar{c}

$$\Delta \bar{a} = \text{_____ mm with } \alpha = \text{_____}$$

$$t_{\alpha, n} = \text{_____}$$

$$\Delta \bar{b} = \text{_____ mm with } \alpha = \text{_____}$$

$$t_{\alpha, n} = \text{_____}$$

$$\Delta \bar{c} = \text{_____ mm with } \alpha = \text{_____}$$

$$t_{\alpha, n} = \text{_____}$$

$$\varepsilon = \frac{\Delta \bar{V}_p}{\bar{V}_p}$$

$$\Delta \bar{V}_p =$$

Cylinder

$$\frac{\Delta \bar{V}_c}{\bar{V}_c} = \sqrt{\left(\frac{2\Delta \bar{D}}{\bar{D}}\right)^2 + \left(\frac{\Delta \bar{h}}{\bar{h}}\right)^2}, \text{ where}$$

$\Delta \bar{D}$ and $\Delta \bar{h}$ are the total errors in direct measurements of \bar{D} , \bar{h} .

$$\Delta \bar{D} = \text{_____ mm with } \alpha = \text{_____}$$

$$t_{\alpha, n} = \text{_____}$$

$$\Delta \bar{h} = \text{_____ mm with } \alpha = \text{_____}$$

$$t_{\alpha, n} = \text{_____}$$

$$\varepsilon = \frac{\Delta \bar{V}_c}{\bar{V}_c}$$

$$\Delta \bar{V}_c =$$

The final result with confidence level $\alpha = 0.95$

(by the rule of rounding off)

$$\bar{V}_p \pm \Delta \bar{V}_p =$$

$$\text{mm}^3$$

$$\bar{V}_c \pm \Delta \bar{V}_c =$$

$$\text{mm}^3$$

Conclusions

Test questions

1. What errors are called systematic? Give some examples.
2. What errors are called the calibration ones?
3. Give the definition of uniform distribution parameter l_x for a physical quantity x .
4. Indicate possible sources of random errors. Can these errors be eliminated while performing an individual measurement?
5. Write the formula of a normal distribution and explain the meaning of all its parameters. How can these parameters be evaluated?
6. Indicate conditions at which the end points of confidence interval measurement errors are specified with the help of the Student distribution.
7. Give the general formula that expresses the error in indirect measurements of a certain quantity $Z(y_1, \dots, y_m)$ in terms of errors in direct measurements of quantities y_1, \dots, y_m .
8. Describe the procedure of measuring with a vernier caliper.
9. Describe the procedure of measuring with a micrometer caliper.

Report on laboratory experiment No. 2 Measuring the free fall acceleration

The **objective** is to measure the acceleration due to gravity g_φ in Tomsk, to calculate g_0 , and to compare it with the theoretical estimate.

THEORY

A reference frame is _____

Noninertial reference frames are called _____

A laboratory system is _____

The net force that acts on a body in a laboratory coordinate system is _____

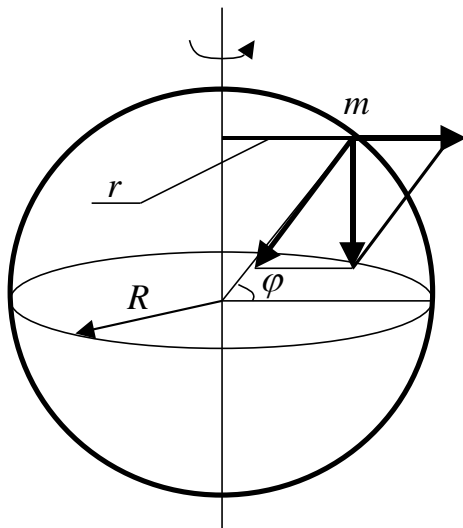
where

$F_{gr} =$ _____ is the force of _____

$F_{cp} =$ _____ is the force of _____

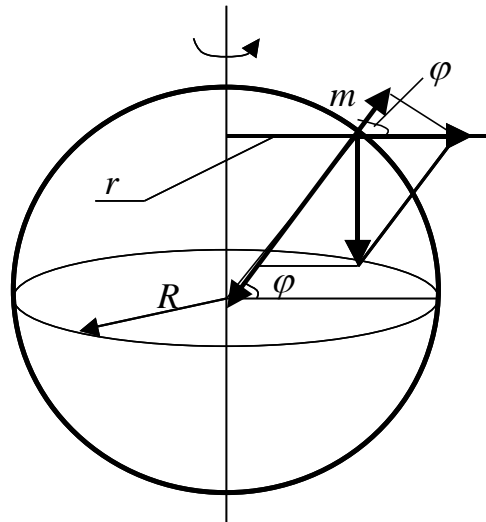
$F_{cor} =$ _____ is the force of _____

Forces acting on a body in a noninertial reference frame at latitude φ



The axis of the Earth's rotation

The acceleration of a body on the Earth's surface at latitude φ



The axis of the Earth's rotation

$$mg_{\varphi} =$$

where _____

$$g_{\varphi} - g_0 =$$

$$a_{cp} = \omega r =$$

$$g_{\varphi} =$$

Calculation formulas

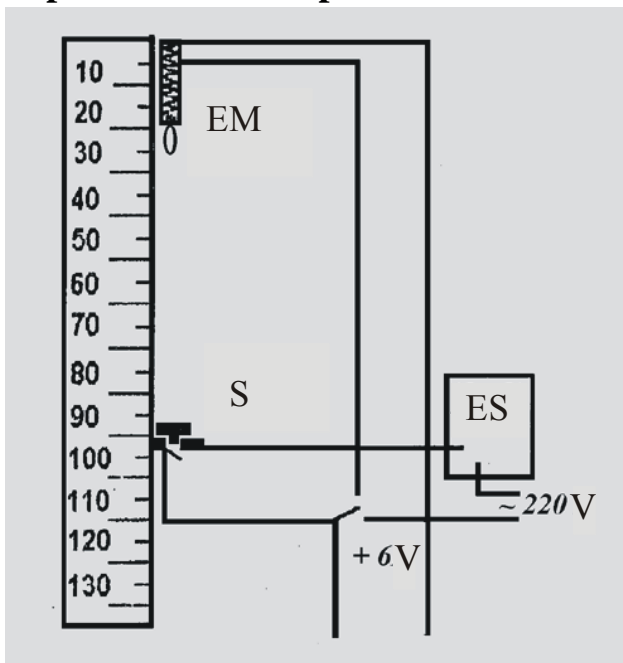
$$g_{\varphi} =$$

where _____

$$g_0 =$$

where _____

Experimental Setup



EM _____

S _____

ESW _____

Data of measurements

h, m	Time t, s															t _{av} , s	g _φ , m/s			
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15					

CALCULATIONS

Evaluation of the free fall acceleration from the experimental data

$$g_{\varphi} =$$

Calculation of the theoretical value

Report on laboratory experiment No. 3

Determining the coefficient of sliding friction

The objective is to evaluate the coefficient of sliding friction k .

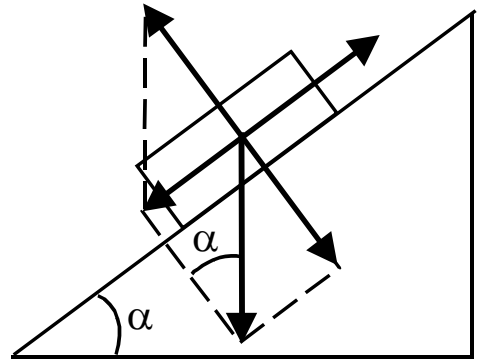
THEORY

The types of friction are _____

The force of sliding friction acts if _____

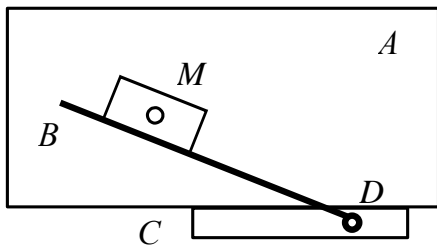
The friction coefficient depends on _____

The method of limiting angle is used to evaluate k . The method is based on the following physical phenomenon: _____



The force of sliding friction F_{sl} (for homogeneous solid materials in contact) is approximately equal to the maximum static frictional force $F_{sl} = kN$

$k =$ _____



Experimental Setup

Here

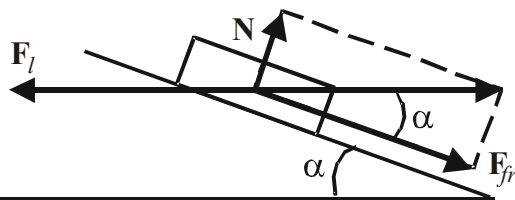
- A _____
- B _____
- C _____
- D _____

Diagram of the experiment

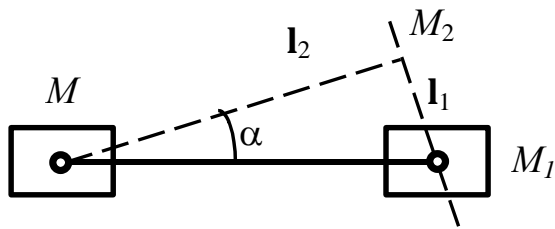
Here

- N _____
- F_{sl} _____
- F_l _____

Directions of forces N and F_{fr} are fixed, but the direction of F_l is variable and



depends on _____



Here

M _____

M_1 _____

M_1M_2 _____

MM_2 _____

MM_1 _____

Calculation formulas

The coefficient of sliding friction is $k =$

where

l_1 _____

l_2 _____

The average coefficient of sliding friction is $\bar{k} =$

Data of measurements

Table 1

Materials in contact	No.	Mass of the load, kg	α , deg	l_1 , cm	l_2 , cm	k	\bar{k}
Duralumin-brass	1		45				
	2						
	3						
	4						
	5						
	1	0.2	45				
	2						
	3						
	4						
	5						
Duralumin-rubber	1		50				
	2						
	3						
	4						
	5						
	1	0.2	50				
	2						
	3						
	4						
	5						

Conclusions

Error analysis

Calculate the absolute and relative errors in measuring the coefficient of sliding friction k for materials in contact by the formulas

$$\sigma_{\bar{k}} = \sqrt{\frac{\sum_{i=1}^n (\bar{k} - k_i)^2}{n(n-1)}} =$$

$$\Delta \bar{k}_r = t_{\alpha, n} \cdot \sigma_{\bar{k}}$$

where $t_{\alpha, n} = 2.26$ at $\alpha = 0.95$ and $n = 10$ (from the table).

$$\bar{k} \pm \Delta \bar{k}_r = \quad \text{with confidence level } \alpha = 0.95.$$

$$\varepsilon_{\bar{k}} = \frac{\Delta \bar{k}_r}{\bar{k}} =$$

Test questions

1. What factors determine the magnitude of friction force?
 2. What is the direction of friction force?
 3. What physical parameters can affect the force of sliding friction?
 4. Compare the coefficient of sliding friction with that of static friction.
 5. Why two specimens having surfaces machined in equal quantity have different coefficients of dry sliding friction?
 6. When does the rolling friction force act?
 7. What is the static and sliding friction?
 8. What is the mechanism of energy losses in friction?
 9. When does the empirical law of dry friction ($F = kN$) violate?
-
-

Report on laboratory experiment No. 4 Studying the distribution function of random variables

The objective is _____

THEORY

Very often random variables are distributed according to the Gauss law

Here the average \tilde{x} is evaluated by the formula

where n is _____

The standard deviation is

The confidence level $\Delta\tilde{x}$ is _____

Here $t_{\alpha,n}$ is called _____ which depends on

and

In our case, $n = 150$ and $t_{\alpha,n} =$ _____ with confidence level $\alpha =$ _____.

Data of measurements and calculations

1. Try to record the time interval $x = 1$ s by an electric timer. The number of measurements is $n = 150$. Taking into consideration that 1 revolution of the timer arm equals 1 s or 100 timer scale divisions, put the data in Table 1 in units of scale divisions.

2. Calculate \tilde{x} , $(x_i - \tilde{x})^2$, and σ and put them in Table 1.

Table 1

n	X_i	$(x_i - \tilde{x})^2$	N	x_i	$(x_i - \tilde{x})^2$
1			76		
2			77		
3			78		
4			79		
5			80		
6			81		
7			82		
8			83		
9			84		
10			95		
11			86		
12			87		
13			88		

14			89		
15			90		
16			91		
17			92		
18			93		
19			94		
20			95		
21			96		
22			97		
23			98		
24			99		
25			100		
26			101		
27			102		
28			103		
29			104		
30			105		
31			106		
32			107		
33			108		
34			109		
35			110		
36			111		
37			112		
38			113		
39			114		
40			115		
41			116		
42			117		
43			118		
44			119		
45			120		
46			121		
47			122		
48			123		
49			124		
50			125		
51			126		
52			127		
53			128		
54			129		
55			130		
56			131		
57			132		

58			133		
59			134		
60			135		
61			136		
62			137		
63			138		
64			139		
56			140		
66			141		
67			142		
68			143		
69			144		
70			145		
71			146		
72			147		
73			148		
74			149		
75			150		
				$\tilde{x} =$	$\sigma =$

2. Divide the total range of x_i variables into 10 arbitrary intervals and count the number of data N_i in each subinterval. Here Δx is the length of the intervals, and \bar{x}_i are their centers.

3. Calculate the probability density $f_i = \frac{N_i}{n\Delta x}$.

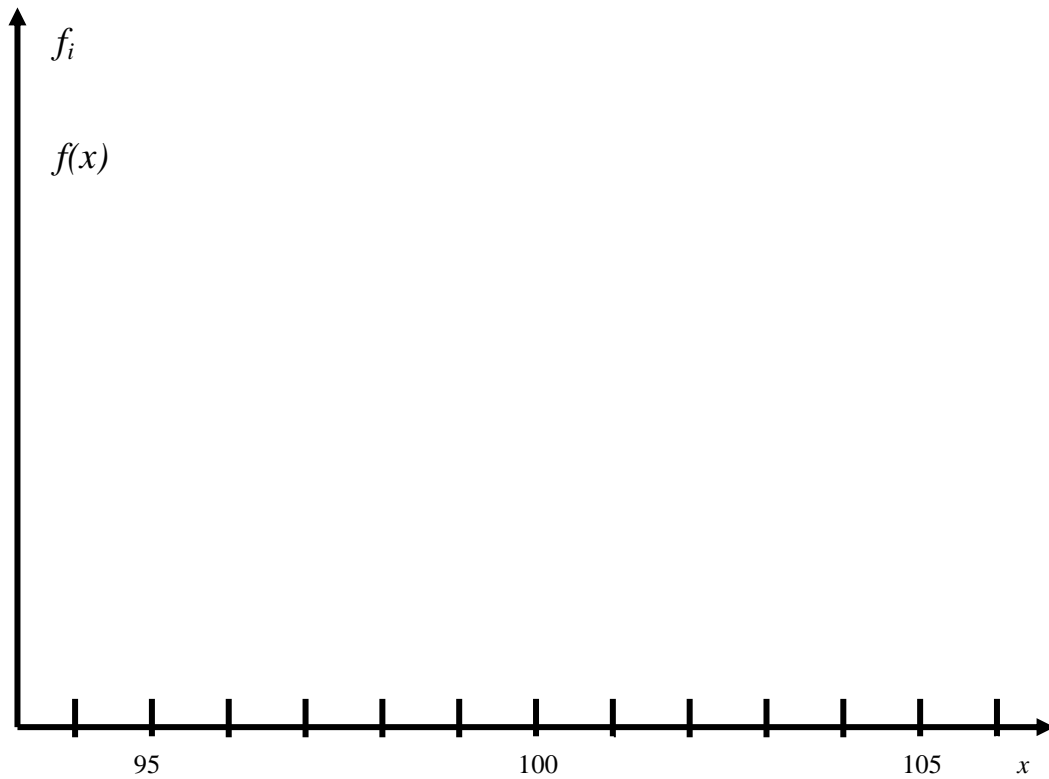
4. Evaluate the parameters of the Gauss distribution $f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(\bar{x}-x_i)^2}{2\sigma^2}}$ for the points \bar{x}_i .

Put all the calculated values in Table 2.

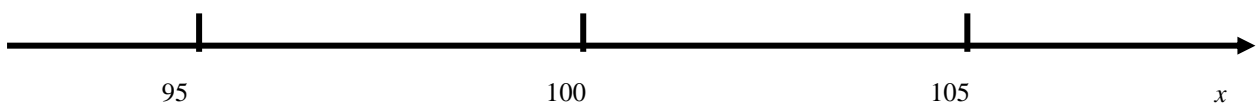
Table 2

Serial No. of interval	Δx	N_i	f_i	$f(x)$
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

5. Using the data of Table 2, construct the histogram and the Gauss distribution.



6. Take arbitrarily 3, 5, and 10 successive measurements. (Three times for each series in different parts of the distribution.) Evaluate \tilde{x} and the confidence level $\Delta\tilde{x}$. Compare these values with those for $n=150$.



Conclusions _____

Test questions

1. What random physical variables do you know?
2. What is the mathematical meaning of the distribution function?
3. Write the Gauss distribution function and explain the meaning of its parameters σ , x , and \tilde{x} .
4. Find the width of the Gauss distribution function (the distance between the points at opposite edges at half maximum). Express this quantity in terms of σ .
5. What can you conclude while looking at the rectangles $x = \bar{x} \pm \Delta x$ found in the experiment?

Report on laboratory experiment No. 5 Elastic and inelastic collisions of balls

The objective of the experiment is _____

THEORY

The impact in mechanics is _____

The impact is called a) central when _____

b) completely elastic when _____

The head-on central impact is called perfectly inelastic when _____

The coefficient of restitution is _____

When one ball is initially at rest, the law of conservation of momentum has the form

Calculation formulas

Speed of the moving ball before impact is $v_1 =$
where

Speeds of balls after impact are

$u_1 =$ _____ where _____

$u_2 =$ _____ where _____

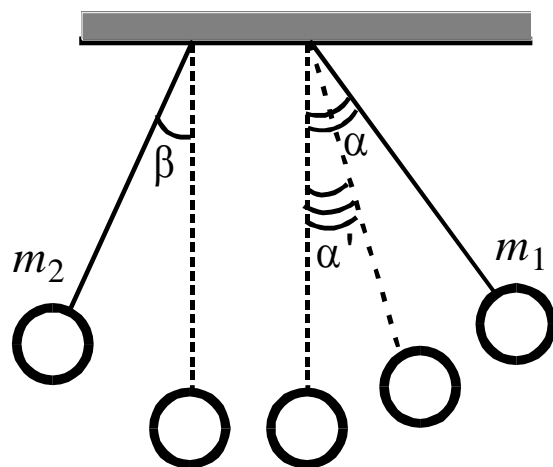
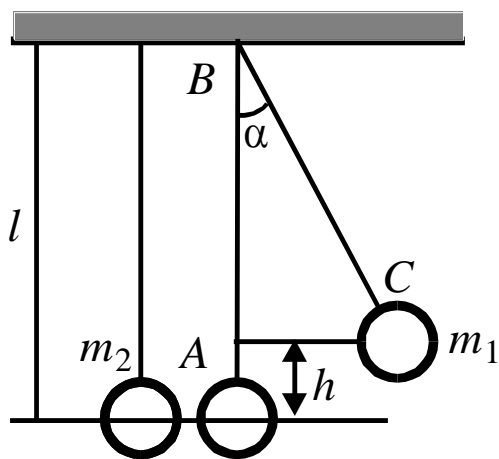
The coefficient of restitution is $k =$

To check the validity of the law of conservation of momentum, the following relations must be tested:

_____ for an elastic impact

_____ for an inelastic impact

Experimental Setup



$h =$ _____

$l =$ _____

$\alpha =$ _____

$\beta =$ _____

$\alpha =$ _____

$\alpha' =$ _____

$\beta =$ _____

Data of measurements

1) For the first pair of balls

$m_1 =$

$m_2 =$

Table 1

No.	α	$\sin \frac{\alpha}{2}$	$\sin^2 \frac{\alpha}{2}$	α'	$\sin \frac{\alpha'}{2}$	$\sin^2 \frac{\alpha'}{2}$	β	$\sin \frac{\beta}{2}$	$\sin^2 \frac{\beta}{2}$	k
1										
2										
3										
4										
5										
6										
7										
8										
9										
10										
Average										

Checking of the law of conservation of momentum

$$m_1 \sin \frac{\alpha}{2} = -m_1 \sin \frac{\alpha'}{2} + m_2 \sin \frac{\beta}{2} \quad (1)$$

Conclusions

2) For the second pair of balls

$$m_1 = \underline{\hspace{2cm}} \quad m_2 = \underline{\hspace{2cm}}$$

Table 2

No.	α	$\sin \frac{\alpha}{2}$	$\sin^2 \frac{\alpha}{2}$	α'	$\sin \frac{\alpha'}{2}$	$\sin^2 \frac{\alpha'}{2}$	β	$\sin \frac{\beta}{2}$	$\sin^2 \frac{\beta}{2}$	k
1										
2										
3										
4										

5										
6										
7										
8										
9										
10										
Average										

Checking of the law of conservation of momentum

$$m_1 \sin \frac{\alpha}{2} = -m_1 \sin \frac{\alpha'}{2} + m_2 \sin \frac{\beta}{2} \quad (2)$$

Conclusions

3) For the third pair of balls (inelastic collision)

$m_1 =$ _____

$m_2 =$ _____

Table 3

No.	α	$\sin \frac{\alpha}{2}$	β	$\sin \frac{\beta}{2}$
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				
Average				

Checking of the law of conservation of momentum

$$m_1 \sin \frac{\alpha}{2} = (m_1 + m_2) \sin \frac{\beta}{2} \quad (3)$$

Conclusions

Error analysis

Calculate the random error in measuring the coefficient of restitution k from the data in Tables 1 and 2 (according to tutor's instruction).

1. Calculate the average value of k

$$\bar{k} =$$

2. Calculate the standard deviation of \bar{k}

$$\sigma_{\bar{k}} =$$

3. Calculate the random error

$$\Delta \bar{k}_r = t_{\alpha, n} \cdot \sigma_{\bar{k}} =$$

where $\alpha =$

$$t_{\alpha, n} = \quad \text{(from the table)}$$

$$\bar{k} \pm \Delta \bar{k}_r = \quad \text{with confidence level } \alpha = 0.95.$$

The relative measurement error is

$$\varepsilon_k = \frac{\Delta \bar{k}_r}{\bar{k}} =$$

Test questions

1. What types of impacts do you know?
2. How do you understand the terms absolutely elastic collision, elastic collision, inelastic collision, and perfectly inelastic collision?
3. Why is it necessary to center the balls?
4. What is the elasticity coefficient?
5. Does this coefficient depend on collision angles?
6. What factors determine the values of the elasticity coefficient?
7. How do Eqs. (1) and (2) change when the collision is perfectly inelastic?
8. Describe the process of collision. What forces do act in this process? What is the elastic deformation?
9. Formulate the law of conservation of energy for the perfectly inelastic collision.
10. What is your opinion concerning Eq. (3)? Is it correct or not?

Report on laboratory experiment No. 6 Studying dynamics laws with Athwood's machine

The objective of the experiments is _____

THEORY

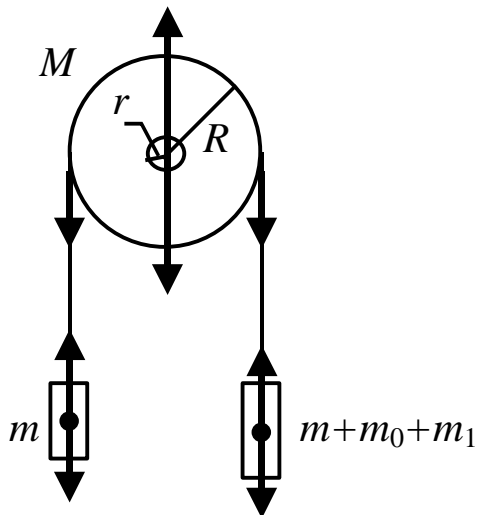
The fundamental laws used in this work are _____

The acceleration is _____

The force is _____

Newton's second law (for translational motion) _____

The basic law of rotational motion is _____



Draw the diagram of forces acting upon the bodies shown in the figure and analyze their motion.

1) For uniform motion of bodies, equations have the form

The torque produced by the friction force is _____

2) For uniformly accelerated motion of bodies, the equation of motion has the form

The friction force is _____ when _____

The acceleration of bodies is _____

3) On the other hand, using the laws of kinematics, the acceleration can be found if

_____ and _____ are specified, i.e., _____

Calculation formulas

(explain the physical meaning of every quantity)

Problem 1

Compare the magnitude of acceleration calculated in accordance with laws of kinematics from the formula

$$a = \frac{2S}{t^2}, \text{ where } S \text{ _____}$$

$$t \text{ _____}$$

and that calculated in accordance with the law of dynamics from the formula

$$a = \frac{m_1 g}{2m + \frac{M}{2}}, \text{ where } m_1 \text{ is _____}$$

$$m \text{ is _____}$$

$$M_p \text{ _____}$$

Problem 2

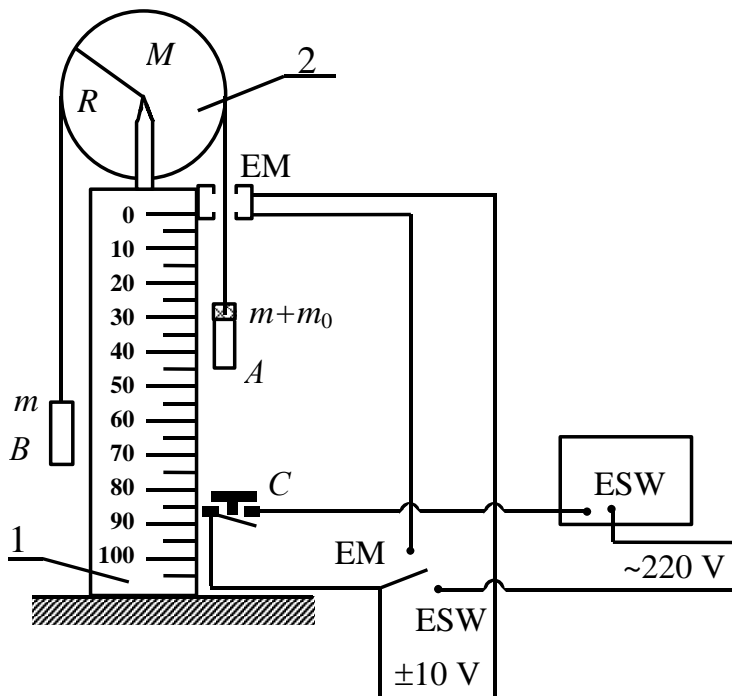
Check the relation

$$\frac{a_1}{a_2} = \frac{F_1}{F_2}, \text{ where } a_1 \text{ is _____}$$

$$a_2 \text{ is _____}$$

$$F_1 = P_2 - P_1 = (m_2 - m_1)g, \text{ where } m_1 \text{ is _____}$$

$$F_2 = P_2 + P_1 = (m_2 + m_1)g, \text{ where } m_2 \text{ is _____}$$



Experimental Setup

where

A is _____

C is _____

B is _____

ESW is _____

EM is _____

1 is _____

2 is _____

Experimental data

Problem 1

Table 1

No.	m ₁ , g	2m, g	M _p , g	S, cm	t, s	t _{av} , s	a = $\frac{2S}{t^2}$, cm/s ²	a = $\frac{m_1 g}{2m + \frac{M}{2}}$ cm/s ²
1								
2								
3								
4								
5								
1								
2								
3								
4								
5								

Calculations

- 1) Calculate the acceleration in accordance with the laws of kinematics from the formula

$$a = \frac{2S}{t^2}, \quad a =$$

Calculate the acceleration in accordance with the laws of dynamics from the formula

$$a = \frac{m_1 g}{2m + \frac{M}{2}}, \quad m_1 = \quad a =$$

Compare the results obtained.

Conclusions

- 2) For the second extra mass $m_1 =$

$$a = \frac{2S}{t^2}, \quad a =$$

$$a = \frac{m_1 g}{2m + \frac{M}{2}}, \quad a =$$

Conclusions

Problem 2

Table 2

No.	m ₁ , g	m ₂ , g	k ₁ = $\frac{F_1}{F_2}$	S, cm	t ₁ , S	t _{1av} , S	t ₂ , S	t _{2av} , S	k ₂ = $\frac{a_1}{a_2}$
1									
2									
3									
4									
5									

Calculations

Find the ratio of forces

$$k_1 = \frac{F_1}{F_2} = \frac{m_2 - m_1}{m_2 + m_1}, \quad k_1 =$$

Find accelerations a₁, a₂ and their ratio

$$a_1 = \frac{2S}{t_{1av}^2}, \quad a_1 =$$

$$a_2 = \frac{2S}{t_{2av}^2}, \quad a_2 =$$

$$k_2 = \frac{a_1}{a_2}, \quad k_2 =$$

Compare k₁ and k₂ k₁ =

$$k_2 =$$

Conclusions

Test questions

1. How does the rotation friction force depend on the masses attached to each end of the cord?
2. What should be done to overcome the rotational friction force?
3. Under what conditions does the torque produced by the rotational friction force equal to that produced by tension in the cord?
4. Write the formula for the magnitude of rotational friction torque. On what quantities does the friction coefficient depend?
5. What conditions are needed to neglect the rotational friction force?
6. Write the equation of motion of bodies when $a \ll g$, $m_1 \ll m$, and $m_0 \ll m$.
7. Write the equation describing the motion of masses.
8. How can we verify that the motion of bodies is uniform or uniformly accelerated?
9. Write the kinematics equation of motion of bodies.
10. What is the magnitude of rotational friction force when the bodies move with acceleration?

Report on laboratory experiment No. 7 Determining the mean free path and the effective diameter of a molecule

The objective of the experiments is _____

THEORY

Transport phenomena are _____

The mean free path is _____

The effective diameter of a molecule is _____

Calculation formulas

The mean free path is $\bar{\lambda} =$

where _____

The pressure difference along the pipe is $\Delta P =$

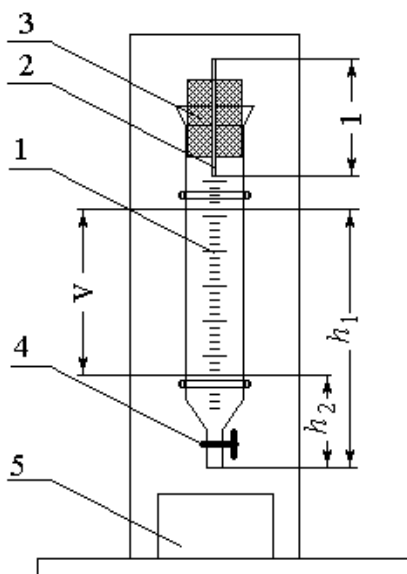
where h_1 _____

h_2 _____

r is the radius of a capillary, $r =$

The effective molecule diameter $D_{eff} =$

where _____



Experimental Setup

Where

1 _____

2 _____

3 _____

4 _____

5 _____

l _____

h_1 (measured) _____

h_2 (measured) _____

V (measured) _____

Data of measurements

1) Estimation of the accuracy of the microscope and calculation of the capillary radius.

Table 1

	1	2	3	ΔN_{av}
N_1				
N_2				
$\Delta N = N_2 - N_1$				

The accuracy of the microscope is

$$x = \frac{2 \text{ mm}}{\Delta N_{av}},$$

$x =$

Table 2

	1	2	3	$\Delta N'_{av}$
N'_1				
N'_2				
$\Delta N' = N'_2 - N'_1$				

The capillary diameter is

$$d = \Delta N'_{av} \cdot x$$

and its radius $r = \frac{d}{2}$.

$d =$

$r =$

Put the data in Table 3

Table 3

No	$h_1, \text{ m}$	$t, \text{ s}$	$h_2, \text{ m}$	$l, \text{ m}$	$\Delta P, \text{ Pa}$	$V, \text{ m}^3$	$T, \text{ K}$	$P, \text{ Pa}$	$r, \text{ m}$	$\lambda, \text{ m}$	$D, \text{ m}$
1											
2											
3											

Reference data for calculations

$$R = 8.31 \text{ J/mol}\cdot\text{K}, \quad \mu = 0.029 \text{ kg/mol}, \quad K = 1.38 \cdot 10^{-23} \text{ J/K},$$

$$1 \text{ mm Hg} = 133.3 \text{ Pa}, \quad g = 9.8 \text{ m/s}^2, \quad \rho_{\text{water}} = 10^3 \text{ kg/m}^3.$$

CALCULATIONS

Calculate the mean free path $\bar{\lambda}$

$$\lambda_1 =$$

$$\lambda_2 =$$

$$\lambda_3 =$$

$$\bar{\lambda} = \frac{\lambda_1 + \lambda_2 + \lambda_3}{3} =$$

Calculate the effective diameter of an air molecule

$$D_{\text{eff}} =$$

Compare the measured and theoretical values.

Theoretical value

for air under standard conditions

$$\bar{\lambda} \cong 6.95 \cdot 10^{-8} \text{ m}$$

$$D_{\text{eff}} \cong 0.35 \text{ nm} = 3.5 \cdot 10^{-10} \text{ m}$$

Measured value

$$\bar{\lambda} =$$

$$D_{\text{eff}} =$$

Conclusions

Calculate the error in measuring $\bar{\lambda}$ by the method of evaluating the indirect measurement error.

Derive the formula for calculating

$$\frac{\Delta\bar{\lambda}}{\bar{\lambda}} =$$

Error analysis

$$\bar{\lambda} \pm \Delta\bar{\lambda} =$$

with confidence level $\alpha = 0.95$.

The relative error is

$$\delta_{\bar{\lambda}} = \frac{\Delta\bar{\lambda}}{\bar{\lambda}} =$$

Test questions

1. What are the causes of transport phenomena?
2. What transport phenomena do you know?
3. Why the transport phenomena are rather “slow”?
4. What is D_{eff} ?
5. What physical phenomenon provides the basis for experimental determination of $\bar{\lambda}$ and D_{eff} ?
6. Give the relation between $\bar{\lambda}$ and D_{eff} .

