1. Find the diameter, the radius and centers of the given graph.
2. Find the vertex connectivity and the edge connectivity.
3. Find a minimum vertex cut for vertices $b, h$.
4. Find a maximum set of vertex-independent paths $\langle b, h\rangle$.

|  |  | $b$ | c | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  |  |  |  | 1 |  | 1 | 1 |
| $b$ |  |  | 1 |  | 1 |  | 1 |  |
| c |  | 1 |  | 1 | 1 |  |  |  |
| $d$ |  |  | 1 |  |  | 1 |  |  |
| $e$ | 1 | 1 | 1 |  |  |  | 1 |  |
| $f$ |  |  |  | 1 |  |  |  | 1 |
| $g$ | 1 | 1 |  |  | 1 |  |  | 1 |
| $h$ | 1 |  |  |  |  | 1 | 1 |  |

5. Construct the quotient graph for the given graph and determine its type of connectivity.

|  | $a$ | $b$ | c | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  |  | 1 | 1 |  |  |  | 1 |
| $b$ |  |  | 1 |  |  |  | 1 |  |
| c | 1 |  |  |  |  |  |  |  |
| $d$ |  |  |  |  |  |  | 1 |  |
| $e$ | 1 |  |  |  |  | 1 |  | 1 |
| $f$ |  | 1 |  |  | 1 |  |  |  |
| $g$ |  |  |  | 1 |  |  |  |  |
| $h$ |  |  |  |  |  |  |  |  |

6. By using operations with Boolean matrices find all pairs of vertices connected by paths of the length 3 .
7. By using Warshall algorithm find all pairs of vertices connected by paths going only through vertices $\{b, c, e\}$.


## Connectivity. Variant 2.

1. Find the diameter, the radius and centers of the given graph.
2. Find the vertex connectivity and the edge connectivity.
3. Find a minimum vertex cut for vertices $c, f$.
4. Find a maximum set of vertex-independent paths $\langle c, f\rangle$.

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  | 1 | 1 |  |  |  | 1 |  |
| $b$ | 1 |  |  |  | 1 |  | 1 | 1 |
| c | 1 |  |  |  |  |  |  |  |
| $d$ |  |  |  |  |  | 1 | 1 |  |
| $e$ |  | 1 |  |  |  |  | 1 |  |
| $f$ |  |  |  | 1 |  |  |  | 1 |
| $g$ | 1 | 1 |  | 1 | 1 |  |  | 1 |
| $h$ |  | 1 |  |  |  | 1 | 1 |  |

5. Construct the quotient graph for the given graph and determine its type of connectivity.

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  | 1 |  | 1 |  |  |  | 1 |
| $b$ |  |  |  |  | 1 |  | 1 |  |
| c |  |  |  | 1 |  |  |  |  |
| $d$ |  |  |  |  |  |  |  |  |
| $e$ | 1 |  | 1 |  |  | 1 |  |  |
| $f$ |  |  |  |  |  |  |  | 1 |
| $g$ |  |  |  | 1 |  |  |  |  |
| $h$ |  |  |  |  |  |  | 1 |  |

6. By using operations with Boolean matrices find all pairs of vertices connected by paths of the length 3 .
7. By using Warshall algorithm find all pairs of vertices connected by paths going only through vertices $\{b, d, e\}$.

| $a$ |  |  |  |  | $b$ |  |  |  |  | $c$ | $d$ | $e$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 1 |  |  |  |  |  |  |  |  |  |

## Connectivity. Variant 3.

1. Find the diameter, the radius and centers of the given graph.
2. Find the vertex connectivity and the edge connectivity.
3. Find a minimum vertex cut for vertices $a, d$.
4. Find a maximum set of vertex-independent paths $\langle a, d\rangle$.

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  | 1 | 1 |  |  |  | 1 | 1 |
| $b$ | 1 |  | 1 |  |  |  |  | 1 |
| c | 1 | 1 |  |  | 1 | 1 |  |  |
| $d$ |  |  |  |  |  |  | 1 | 1 |
| $e$ |  |  | 1 |  |  |  |  |  |
| $f$ |  |  | 1 |  |  |  |  | 1 |
| $g$ | 1 |  |  | 1 |  |  |  |  |
| $h$ | 1 | 1 |  | 1 |  | 1 |  |  |

5. Construct the quotient graph for the given graph and determine its type of connectivity.

|  | $a$ | $b$ | c | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  |  |  |  |  |  | 1 |  |
| $b$ | 1 |  |  |  | 1 |  | 1 |  |
| c |  |  |  |  |  | 1 |  |  |
| $d$ |  |  |  |  |  |  |  |  |
| $e$ |  | 1 | 1 |  |  | 1 |  | 1 |
| $f$ |  | 1 |  |  |  |  |  | 1 |
| $g$ |  |  |  | 1 |  |  |  |  |
| $h$ |  |  |  | 1 |  |  |  |  |

6. By using operations with Boolean matrices find all pairs of vertices connected by paths of the length 3 .
7. By using Warshall algorithm find all pairs of vertices connected by paths going only through vertices $\{a, c, d\}$.

|  | $a$ | $b$ | c | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  | 1 |  | 1 |  |
| $b$ |  |  | 1 |  |  |
| c |  |  |  | 1 | 1 |
| $d$ | 1 |  | 1 |  |  |
| $e$ |  | 1 |  | 1 |  |

1. Find the diameter, the radius and centers of the given graph.
2. Find the vertex connectivity and the edge connectivity.
3. Find a minimum vertex cut for vertices $a, h$.
4. Find a maximum set of vertex-independent paths $\langle a, h\rangle$.

|  | $a$ | $b$ | c | $d$ | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  | 1 |  |  |  | 1 | 1 |  |
| $b$ | 1 |  |  |  | 1 | 1 |  | 1 |
| c |  |  |  | 1 | 1 |  |  |  |
| $d$ |  |  | 1 |  |  | 1 |  |  |
| $e$ |  | 1 | 1 |  |  |  | 1 |  |
| $f$ | 1 | 1 |  | 1 |  |  | 1 | 1 |
| $g$ | 1 |  |  |  | 1 | 1 |  | 1 |
| $h$ |  | 1 |  |  |  | 1 | 1 |  |

5. Construct the quotient graph for the given graph and determine its type of connectivity.

|  | $a$ | $b$ | c | d | $e$ | $f$ | $g$ | $h$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  | 1 | 1 | 1 |  |  | 1 |  |
| $b$ |  |  |  |  | 1 | 1 |  |  |
| c |  |  |  |  |  |  |  | 1 |
| $d$ |  | 1 | 1 |  |  |  |  |  |
| $e$ |  |  |  |  |  |  |  |  |
| $f$ | 1 |  |  |  |  |  |  | 1 |
| $g$ |  |  |  | 1 | 1 |  |  |  |
| $h$ |  |  |  |  |  |  | 1 |  |

6. By using operations with Boolean matrices find all pairs of vertices connected by paths of the length 3 .
7. By using Warshall algorithm find all pairs of vertices connected by paths going only through vertices $\{b, c, d\}$.

|  | $a$ | $b$ | c | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ |  |  |  | 1 | 1 |
| $b$ |  |  | 1 |  |  |
| c | 1 |  |  |  |  |
| $d$ |  |  | 1 |  | 1 |
| $e$ | 1 | 1 |  |  |  |

