## Flows. Variant 1.

1. Find a maximal flow and a minimal cut in the network with the following capacity matrix.

|  | $a$ | $b$ | c | $d$ | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ | 18 | 14 |  |  | 9 |  |
| $a$ |  | 8 | 11 | 7 |  | 13 |
| $b$ |  |  |  | 12 |  | 19 |
| $c$ |  | 10 |  |  | 15 |  |
| $d$ |  |  | 17 |  | 21 |  |
| $e$ |  |  |  |  |  | 14 |
| $t$ |  |  |  |  |  |  |

2. Propose an algorithm to solve the maximal flow problem in a network with several sources and sinks. Give an example.
3. Find a minimal cost flow using the Ford-Falkerson algorithm for the network from the task 1 with the flow value equal to $2 / 3$ of the maximal flow value and with the follow1ng cost matrix.

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ | 3 | 4 |  |  | 8 |  |
| $a$ |  | 2 | 6 | 4 |  | 7 |
| $b$ |  |  |  | 5 |  | 8 |
| c |  | 3 |  |  | 6 |  |
| $d$ |  |  | 5 |  | 9 |  |
| $e$ |  |  |  |  |  | 4 |
| $t$ |  |  |  |  |  |  |

## Flows. Variant 2.

1. Find a maximal flow and a minimal cut in the network with the following capacity matrix.

|  | $a$ | $b$ | c | $d$ | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ | 9 |  | 11 |  | 11 |  |
| $a$ |  | 6 |  | 8 |  | 12 |
| $b$ |  |  |  |  |  | 7 |
| $c$ | 12 |  |  |  | 5 | 5 |
| $d$ |  |  |  |  | 7 |  |
| $e$ |  |  |  |  |  | 9 |
| $t$ |  |  |  |  |  |  |

2. Propose an algorithm of a maximal flow search in a network with capacities of vertices and edges. Give an example.
3. Find a minimal cost flow using negative cost cycles for the network from the task 1 with the flow value equal to $2 / 3$ of the maximal flow value and with the follow1ng cost matrix.

|  | $a$ | $b$ | c | $d$ | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ | 4 |  | 6 |  | 12 |  |
| $a$ |  | 3 |  | 2 |  | 7 |
| $b$ |  |  |  |  |  | 2 |
| $c$ | 3 |  |  |  | 3 | 1 |
| $d$ |  |  |  |  | 2 |  |
| $e$ |  |  |  |  |  | 8 |
| $t$ |  |  |  |  |  |  |

## Flows. Variant 3.

1. Find a maximal flow and a minimal cut in the network with the following capacity matrix.

|  | $a$ | $b$ | c | $d$ | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ | 10 | 5 |  |  | 8 |  |
| $a$ |  |  | 5 | 3 |  | 4 |
| $b$ |  |  | 4 | 5 | 10 |  |
| $c$ |  |  |  | 4 |  | 9 |
| $d$ |  |  |  |  | 5 | 6 |
| $e$ |  |  |  |  |  | 7 |
| $t$ |  |  |  |  |  |  |

2. Propose an algorithm of a maximal flow search in a network with capacities of vertices and edges. Give an example.
3. Find a minimal cost flow using minimal paths for the network from the task 1 with the flow value equal to $2 / 3$ of the maximal flow value and with the follow1ng cost matrix.


## Flows. Variant 4.

1. Find a maximal flow and a minimal cut in the network with the following capacity matrix.

|  | $a$ | $b$ | $c$ | d | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ |  | 5 |  | 15 | 9 |  |
| $a$ |  |  |  | 6 |  | 7 |
| $b$ | 3 |  | 4 |  | 7 |  |
| c |  |  |  |  | 8 | 3 |
| $d$ |  |  |  |  |  | 18 |
| $e$ |  |  |  | 9 |  | 5 |
| $t$ |  |  |  |  |  |  |

2. Propose an algorithm of a flow search in a network with upper and lower bounds of the flow in every edge. Give an example.
3. Find a minimal cost flow using negative cost cycles for the network from the task 1 with the flow value equal to $2 / 3$ of the maximal flow value and with the follow1ng cost matrix.


## Flows. Variant 5.

1. Find a maximal flow and a minimal cut in the network with the following capacity matrix.

|  | $a$ | $b$ | c | $d$ | $e$ | $t$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s$ | 10 |  | 8 |  |  |  |
| $a$ |  | 8 | 12 | 10 |  | 6 |
| $b$ |  |  |  |  | 5 | 11 |
| c |  |  |  | 4 | 12 |  |
| $d$ |  | 5 |  |  |  | 9 |
| $e$ |  |  |  | 6 |  | 7 |
| $t$ |  |  |  |  |  |  |

2. Propose an algorithm of a flow search in a network with upper and lower bounds of the flow in every edge. Give an example.
3. Find a minimal cost flow using minimal paths for the network from the task 1 with the flow value equal to $2 / 3$ of the maximal flow value and with the following cost matrix.

