

Individual task 3

Fredholm integral equations. Part II

Case 1

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= x + s + 1; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= 1 + 3xs; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x + s) \varphi(s) ds = 1.$$

$$2.2. \varphi(x) - \lambda \int_0^1 (2x - s) \varphi(s) ds = \frac{x}{6}$$

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Case 2

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= 4xs - x^2; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= e^{x-s}; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x) \cos(s) \varphi(s) ds = \cos(2x).$$

$$2.2. \varphi(x) + \int_0^1 e^{x-s} \varphi(s) ds = e^x.$$

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Case 3

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= x + s + 1; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= \sin(x + s); & 0 \leq x \leq 2\pi, & 0 \leq s \leq 2\pi. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) + \int_0^1 e^{x-s} \varphi(s) ds = e^x.$$

$$2.2. \varphi(x) - \lambda \int_0^1 (4xs - x^2) \varphi(s) ds = x.$$

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Case 4

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= 2x - s; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= \sin(x) \cos(s) & 0 \leq x \leq 2\pi, & 0 \leq s \leq 2\pi. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x+s) \varphi(s) ds = 1.$$

$$2.2. \varphi(x) - \lambda \int_0^1 (4xs - x^2) \varphi(s) ds = x.$$

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Case 5

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= 1 + 3xs; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= e^{x-s}; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^1 (2x - s) \varphi(s) ds = \frac{x}{6}.$$

$$2.2. \varphi(x) + \int_0^1 e^{x-s} \varphi(s) ds = e^x.$$

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Case 6

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= x + s + 1; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= x^2 s - x s^2; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x+s) \varphi(s) ds = 1.$$

$$2.2. \varphi(x) + \int_0^1 e^{x-s} \varphi(s) ds = e^x.$$

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Case 7

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$1.1. K(x, s) = \sin(x) - \sin(s) \quad 0 \leq x \leq 2\pi, \quad 0 \leq s \leq 2\pi.$$

$$1.2. K(x, s) = 1 + 3xs; \quad 0 \leq x \leq 1, \quad 0 \leq s \leq 1.$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x) \cos(s) \varphi(s) ds = \cos(2x).$$

$$2.2. \varphi(x) - \lambda \int_0^1 (4xs - x^2) \varphi(s) ds = x.$$

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Case 8

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$1.1. K(x, s) = x \cdot s; \quad 0 \leq x \leq 1, \quad 0 \leq s \leq 1.$$

$$1.2. K(x, s) = e^{x-s}; \quad -1 \leq x \leq 1, \quad -1 \leq s \leq 1.$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^1 (2x - s) \varphi(s) ds = \frac{x}{6}$$

$$2.2. \varphi(x) - \lambda \int_0^1 (4xs - x^2) \varphi(s) ds = x.$$

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Case 9

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$1.1. K(x, s) = 4xs - x^2; \quad -1 \leq x \leq 1, \quad -1 \leq s \leq 1.$$

$$1.2. K(x, s) = e^{x-s}; \quad -1 \leq x \leq 1, \quad -1 \leq s \leq 1.$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x + s) \varphi(s) ds = 1.$$

$$2.2. \varphi(x) + \int_0^1 e^{x-s} \varphi(s) ds = e^x.$$

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Case 10

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= 4xs - x^2; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= e^{x-s}; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x) \cos(s) \varphi(s) ds = \cos(2x).$$

$$2.2. \varphi(x) - \lambda \int_0^1 (4xs - x^2) \varphi(s) ds = x.$$

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Case 11

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= x \cdot s + s^2; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= e^{x-s}; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x) \cos(s) \varphi(s) ds = \cos(2x).$$

$$2.2. \varphi(x) - \lambda \int_0^1 (4xs - x^2) \varphi(s) ds = x.$$

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Case 12

1. Using the Fredholm determinants method with help of recurrence relations

$B_n(x, s) = C_n K(x, s) - n \int_a^b K(x, t) B_{n-1}(t, s) dt$ и $C_n = \int_a^b B_{n-1}(t, t) dt$, find the resolvent for kernels:

$$\begin{aligned} 1.1. \quad K(x, s) &= 1 + 3xs; & 0 \leq x \leq 1, & 0 \leq s \leq 1. \\ 1.2. \quad K(x, s) &= 4xs - x^2; & -1 \leq x \leq 1, & -1 \leq s \leq 1. \end{aligned}$$

2. Solve the integral equations with help of resolvent:

$$2.1. \varphi(x) - \lambda \int_0^{2\pi} \sin(x) \cos(s) \varphi(s) ds = \cos(2x).$$

$$2.2. \varphi(x) + \int_0^1 e^{x-s} \varphi(s) ds = e^x.$$