

# Обязательные индивидуальные домашние задания

## Задание № 1а

Найдите производные данных функций

1a.1	$y = \frac{2(3x^3 + 4x^2 - x - 2)}{15\sqrt{x+1}}$	1a.2	$y = \frac{(2x^2 - 1)\sqrt{1+x^2}}{3x^3}$
1a.3	$y = \frac{x^4 - 8x^2}{2(x^2 - 4)}$	1a.4	$y = \frac{2x^2 - x - 1}{3\sqrt{2+4x}}$
1a.5	$y = \frac{(1+x^8)\sqrt{1+x^8}}{12x^{12}}$	1a.6	$y = \frac{x^2}{2\sqrt{1-3x^4}}$
1a.7	$y = \frac{(x^2 - 6)\sqrt{(4+x^2)^3}}{120x^5}$	1a.8	$y = \frac{(x^2 - 8)\sqrt{x^2 - 8}}{6x^3}$
1a.9	$y = \frac{4 + 3x^3}{x\sqrt[3]{(2+x^3)^2}}$	1a.10	$y = \sqrt[3]{\frac{(1+x^{3/4})^2}{x^{3/2}}}$
1a.11	$y = \frac{x^6 + x^3 - 2}{\sqrt{1-x^3}}$	1a.12	$y = \frac{(x^2 - 2)\sqrt{4+x^2}}{24x^3}$
1a.13	$y = \frac{1+x^2}{2\sqrt{1+2x^2}}$	1a.14	$y = \frac{\sqrt{x-1}(3x-2)}{4x^2}$
1a.15	$y = \frac{\sqrt{(1+x^2)^3}}{3x^3}$	1a.16	$y = \frac{x^6 + 8x^3 - 128}{\sqrt{8-x^3}}$
1a.17	$y = \frac{\sqrt{2x+3}(x-2)}{x^2}$	1a.18	$y = (1-x^2)\sqrt[5]{x^3 + \frac{1}{x}}$
1a.19	$y = \frac{(2x^2 + 3)\sqrt{x^2 - 3}}{9x^3}$	1a.20	$y = \frac{x-1}{(x^2 + 5)\sqrt{x^2 + 5}}$
1a.21	$y = \frac{(3x-5)\sqrt{x-3x^3}}{2x^2}$	1a.22	$y = 2\sqrt{\frac{1-\sqrt{x}}{1+\sqrt{x}}}$
1a.23	$y = \frac{1}{(x+2)\sqrt{x^2 + 4x + 5}}$	1a.24	$y = \frac{3\sqrt[3]{x^2 + x + 1}}{x+1}$

1a.25	$y = 3 \sqrt[3]{\frac{x+1}{(x-1)^2}}$	1a.26	$y = \frac{x+7}{6 \sqrt{x^2 + 2x + 7}}$
1a.27	$y = \frac{x \sqrt{x+1}}{x^2 + x + 1}$	1a.28	$y = \frac{x^2 + 2}{2 \sqrt{1 - x^4}}$
1a.29	$y = \frac{(x+3) \sqrt{2x-1}}{2x+7}$	1a.30	$y = \frac{3x + \sqrt{x}}{\sqrt{x^2 + 2}}$

### Задание № 16

Найдите производные данных функций

16.1	$y = x - \ln(2 + e^x + 2\sqrt{e^{2x} + e^x + 1})$
16.2	$y = \frac{1}{8}e^{2x}(2 - \sin 2x - \cos 2x)$
16.3	$y = \frac{1}{2} \operatorname{arctg} \frac{e^x - 3}{2}$
16.4	$y = \frac{1}{\ln 4} \ln \frac{1 + 2^x}{1 - 2^x}$
16.5	$y = 2\sqrt{e^x + 1} + \ln \frac{\sqrt{e^x + 1} - 1}{\sqrt{e^x + 1} + 1}$
16.6	$y = \frac{2}{3} \sqrt{(\operatorname{arctg} e^x)^3}$
16.7	$y = \frac{1}{2} \ln(e^{2x} + 1) - 2 \operatorname{arctg} e^x$
16.8	$y = \ln(e^x + 1) + \frac{18e^{2x} + 27e^x + 11}{6(e^x + 1)}$
16.9	$y = \frac{2}{\ln 2} \left( \sqrt{2^x - 1} - \operatorname{arctg} \sqrt{2^x - 1} \right)$
16.10	$y = 2(x - 2)\sqrt{1 + e^x} - 2 \ln \frac{\sqrt{1 + e^x} - 1}{\sqrt{1 + e^x} + 1}$

16.11	$y = \frac{e^{ax}}{a^2 + b^2} (a \sin bx - b \cos bx)$
16.12	$y = \frac{e^{ax}}{a^2 + b^2} (b \sin bx + a \cos bx)$
16.13	$y = e^{ax} \frac{\frac{1}{2}x}{2a} + \frac{a \cos 2bx + 2b \sin 2bx}{2(a^2 + 4b^2)}$
16.14	$y = x + \frac{1}{1 + e^x} - \ln(1 + e^x)$
16.15	$y = x - 3 \ln \frac{x}{(1 + e^6) \sqrt{1 + e^3}} - 3 \operatorname{arctg} \frac{x}{e^6}$
16.16	$y = x + \frac{8}{x + e^{x/4}}$
16.17	$y = \ln(e^x + \sqrt{e^{2x} - 1}) + \sin e^{-x}$
16.18	$y = x - e^{-x} \arcsin e^x - \ln(1 + \sqrt{1 - e^{2x}})$
16.19	$y = x - \ln(1 + e^x) - 2e^{-x/2} \operatorname{arctg} e^{x/2} - (\operatorname{arctg} e^{x/2})^2$
16.20	$y = -\frac{1}{2}e^{-x^2} (x^4 + 2x^2 + 2)$
16.21	$y = 2x - \frac{p}{\cos^2 x} \operatorname{arctg} x \frac{e^{5x}}{p}$
16.22	$y = 3e^{\sqrt[3]{x}} \left( \sqrt[3]{x^2} - 2\sqrt[3]{x} + 2 \right)$
16.23	$y = \arcsin e^x - \sqrt{1 - e^{2x}}$
16.24	$y = e^{\sin x} \frac{\sin x}{\cos x} - \frac{1}{\cos x}$
16.25	$y = \frac{e^x}{2} ((x^2 - 1) \cos x + (x - 1)^2 \sin x)$

16.26	$y = \operatorname{arctg} (e^x - e^{-x})$
16.27	$y = 3e^{\sqrt[3]{x}} \left( \sqrt[3]{x^5} - 5\sqrt[3]{x^4} + 2x - 6\sqrt[3]{x^2} + 12\sqrt[3]{x} - 12 \right)$
16.28	$y = -\frac{e^{3x}}{3sh^3x}$
16.29	$y = \ln \frac{\sqrt{1+e^x+e^{2x}} - e^x - 1}{\sqrt{1+e^x+e^{2x}} - e^x + 1}$
16.30	$y = \frac{e^{x^2}}{1+x^3}$

**Задание № 1в**  
Найдите производные данных функций

1в.1	$y = \sin \sqrt{3} + \frac{1}{3} \frac{\sin^2 3x}{\cos 6x}$	1в.2	$y = \cos \ln 2 - \frac{1}{3} \frac{\cos^2 3x}{\sin 6x}$
1в.3	$y = \operatorname{tg} \ln \frac{1}{3} + \frac{1}{4} \frac{\sin^2 4x}{\cos 8x}$	1в.4	$y = \operatorname{ctg} \sqrt[3]{5} - \frac{1}{8} \frac{\cos^2 4x}{\sin 8x}$
1в.5	$y = \frac{\cos \sin 5 \Psi \sin^2 2x}{2 \cos 4x}$	1в.6	$y = \frac{\sin \cos 3 \Psi \cos^2 2x}{4 \sin 4x}$
1в.7	$y = \frac{\cos \ln 7 \Psi \sin^2 7x}{7 \cos 14x}$	1в.8	$y = \cos \operatorname{ctg} 2 - \frac{1}{16} \frac{\cos^2 8x}{\sin 16x}$
1в.9	$y = \operatorname{ctg} \cos 2 + \frac{1}{6} \frac{\cos^2 10x}{\sin 20x}$	1в.10	$y = \sqrt[3]{\operatorname{ctg} 2} + \frac{1}{6} \frac{\sin^2 6x}{\cos 12x}$
1в.11	$y = \frac{1}{3} \cos \operatorname{tg} \frac{1}{2} + \frac{1}{10} \frac{\sin^2 10x}{\cos 20x}$	1в.12	$y = \ln \sin \frac{1}{2} - \frac{1}{24} \frac{\cos^2 12x}{\sin 24x}$
1в.13	$y = 8 \sin \operatorname{ctg} 3 + \frac{1}{5} \frac{\sin^2 5x}{\cos 10x}$	1в.14	$y = \frac{\cos \operatorname{ctg} 3 \Psi \cos^2 14x}{28 \sin 28x}$
1в.15	$y = \frac{\cos x \operatorname{tg}(1/3) \Psi \cos^2 16x}{32 \sin 32x}$	1в.16	$y = \frac{\operatorname{ctg} \sin(1/3) \Psi \sin^2 17x}{17 \cos 34x}$

1в.17	$y = \frac{\sin \operatorname{tg}(1/7) \cos^2 16x}{32 \sin 32x}$	1в.18	$y = \frac{\sqrt[5]{\operatorname{ctg} 2} \cos^2 18x}{36 \sin 36x}$
1в.19	$y = \frac{\operatorname{tg} \ln 2 \sin^2 19x}{19 \cos 38x}$	1в.20	$y = \operatorname{ctg} \cos 5 - \frac{1}{40} \frac{\cos^2 20x}{\sin 40x}$
1в.21	$y = \sqrt{\operatorname{tg} 4} + \frac{\sin^2 21x}{21 \cos 42x}$	1в.22	$y = \cos \ln 13 - \frac{1}{44} \frac{\cos^2 22x}{\sin 44x}$
1в.23	$y = \ln \cos \frac{1}{3} + \frac{\sin^2 23x}{23 \cos 46x}$	1в.24	$y = \operatorname{ctg} \sin \frac{1}{13} - \frac{1}{48} \frac{\cos^2 24x}{\sin 48x}$
1в.25	$y = \sin \ln \frac{1}{2} + \frac{\sin^2 25x}{25 \cos 50x}$	1в.26	$y = \sqrt[3]{\cos \sqrt{2}} - \frac{1}{52} \frac{\cos^2 26x}{\sin 52x}$
1в.27	$y = \sqrt[7]{\operatorname{tg} \cos 2} + \frac{\sin^2 27x}{27 \cos 54x}$	1в.28	$y = \sin \sqrt[3]{\operatorname{tg} 2} - \frac{\cos^2 28x}{56 \sin 56x}$
1в.29	$y = \cos \sin 3 + \frac{\sin^2 29x}{29 \cos 58x}$	1в.30	$y = \sin^2 \cos 2 - \frac{\cos^2 30x}{60 \sin x 60}$

### Задание № 1г

Найдите производные функций, заданных неявно.

1Г.1	$y \arcsin x - \arccos(y - x) = 0$	1Г.2	$y \operatorname{ctgx} = \cos(x + y)$
1Г.3	$x^3 + y^3 - 3axy = 0$	1Г.4	$y^2 \cos x = a^2 \sin 3x$
1Г.5	$y^3 - 3y + 2ay \sin x = 0$	1Г.6	$y^2 - 2xy + b^2 \cos(xy) = 0$
1Г.7	$x^4 + y^4 = x^2 y^2$	1Г.8	$x^3 + ax^2 y + bxy^2 + y^3 = 0$
1Г.9	$\sin(xy) + \cos(xy) = \operatorname{tg}(x + y)$	1Г.10	$2^x + 2^y = 2^{x+y}$
1Г.11	$2y \ln y = x \arcsin x$	1Г.12	$x - y = y \arcsin x - x \arcsin y$
1Г.13	$x^y = y^x$	1Г.14	$x \cos(xy) = ye^x$
1Г.15	$x^{\frac{1}{2}} + y^{\frac{1}{2}} = a^{\frac{1}{2}}$	1Г.16	$x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$
1Г.17	$y = 1 + xe^y$	1Г.18	$x \sin y - \cos y + \cos 2y = 0$
1Г.19	$\operatorname{tg} \frac{y}{2} = \sqrt{\frac{1-k}{1+k}} \operatorname{tg} \frac{x}{2}$	1Г.20	$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$

1Г.21	$y = x + \operatorname{arctg}(y + e^x)$	1Г.22	$y^2 \arcsin x + 2^y = x$
1Г.23	$\cos x + e^{y \arcsin x} = xy$	1Г.24	$y \ln(x + y) = 2^y \arccos x$
1Г.25	$\operatorname{tg}(x + 5^y) + \operatorname{arctg}(x^y) = 0$	1Г.26	$\cos x + \sqrt{y} = \operatorname{arcctg}(2^x + y^3)$
1Г.27	$\sqrt{x + \arcsin y} + \ln(x - y) = 0$	1Г.28	$\operatorname{ctg}(xy) + \operatorname{tg}(x - y) = 2^y$
1Г.29	$\operatorname{sh}(x - y) + \operatorname{th}(2^x) = e^y$	1Г.30	$e^{2x} + \sqrt[3]{y} + \operatorname{ch}(xy)$

### Задание № 1д

Найдите производные данных функций

1д.1	$y = (\operatorname{cth}3x)^{\arcsin x}$	1д.2	$y = (\cos(x + 2))^{\ln x}$
1д.3	$y = (\sin 3x)^{\arccos x}$	1д.4	$y = (\operatorname{th}5x)^{\arcsin(x+1)}$
1д.5	$y = (\operatorname{sh}(x + 2))^{\arcsin 2x}$	1д.6	$y = (\cos 5x)^{\operatorname{arcctg} \sqrt{x}}$
1д.7	$y = (\sqrt{3x + 2})^{\operatorname{arcctg} 3x}$	1д.8	$y = (\ln(x + 3))^{\sin \sqrt{x}}$
1д.9	$y = (\log_2(x + 4))^{\operatorname{ctg} 7x}$	1д.10	$y = (\operatorname{sh}3x)^{\operatorname{arcctg}(x+2)}$
1д.11	$y = (\operatorname{ch}3x)^{\operatorname{ctg}(1/x)}$	1д.12	$y = (\arcsin 5x)^{\operatorname{tg} \sqrt{x}}$
1д.13	$y = (\arccos 5x)^{\ln(x-3)}$	1д.14	$y = (\arccos 2x)^{3\operatorname{arcctg} x}$
1д.15	$y = (\ln(x + 7))^{\operatorname{ctg} 2x}$	1д.16	$y = (\operatorname{ctg}(7x + 4))^{\sqrt{x+3}}$
1д.17	$y = (\operatorname{th}\sqrt{x+1})^{\operatorname{arcctg} 2x}$	1д.18	$y = (\operatorname{cth}(1/x))^{\arcsin 7x}$
1д.19	$y = (\cos(x + 5))^{\arcsin 3x}$	1д.20	$y = (\sqrt{x+6})^{\arccos 3x}$
1д.21	$y = (\sin 4x)^{\operatorname{arcctg}(1/x)}$	1д.22	$y = (\operatorname{tg} 3x^4)^{\sqrt{x+3}}$
1д.23	$y = (\operatorname{ctg} 2x^3)^{\sin \sqrt{x}}$	1д.24	$y = (\operatorname{tg} 7x^5)^{\sqrt{x+2}}$
1д.25	$y = (\arccos x)^{\sqrt{\cos x}}$	1д.26	$y = (\operatorname{ctg} 7x)^{\operatorname{sh}(x+3)}$
1д.27	$y = (\operatorname{sh}5x)^{\operatorname{arcctg}(x+4)}$	1д.28	$y = (\operatorname{arcctg} x)^{\operatorname{th}(3x+1)}$
1д.29	$y = (\operatorname{cth}\sqrt{x})^{\sin(x+3)}$	1д.30	$y = (\operatorname{sh}3x)^{\operatorname{arcctg} 2x}$

### Задание № 1e

Вычислите производную  $y'$  от функций, заданных параметрически

1e.1 $x = \frac{3t^2 + 1}{3t^2}$ $y = \sin(t^3/3 + t)$	1e.2 $x = \sqrt{2t - t^2}$ $y = \frac{1}{\sqrt[3]{(t - 1)^2}}$
1e.3 $x = \sqrt{1 - t^2}$ $y = \operatorname{tg} \sqrt{1 + t}$	1e.4 $x = \arcsin(\sin t)$ $y = \arccos(\cos t)$
1e.5 $x = \ln(t + \sqrt{t^2 + 1})$ $y = t\sqrt{t^2 + 1}$	1e.6 $x = \sqrt{2t - t^2}$ $y = \arcsin(t - 1)$
1e.7 $x = \operatorname{ctg}(2e^t)$ $y = \ln \operatorname{tg} e^t$	1e.8 $x = \ln \operatorname{ctg} t$ $y = 1/\cos^2 t$
1e.9 $x = \operatorname{arctg} e^{t/2}$ $y = \sqrt{e^t + 1}$	1e.10 $x = \ln \sqrt{\frac{1-t}{1+t}}$ $y = \sqrt{1 - t^2}$
1e.11 $x = \ln \frac{1}{\sqrt{1 - t^4}}$ $y = \arcsin \frac{1 - t^2}{1 + t^2}$	1e.12 $x = \sqrt{1 - t^2}$ $y = \frac{t}{\sqrt{1 - t^2}}$
1e.13 $x = \arcsin \sqrt{1 - t^2}$ $y = \arccos^2 t$	1e.14 $x = (1 + \cos^2 t)^2$ $y = \cos t / \sin^2 t$
1e.15 $x = \frac{t}{\sqrt{1 - t^2}}$ $y = \frac{\ln(1 + \sqrt{1 - t^2})}{t}$	1e.16 $x = \ln \frac{1 - t}{1 + t}$ $y = \sqrt{1 - t^2}$
1e.17 $x = \arccos \frac{1}{t}$ $y = \sqrt{t^2 - 1} + \arcsin \frac{1}{t}$	1e.18 $x = \frac{1}{\ln t}$ $y = \ln \frac{1 + \sqrt{1 - t^2}}{t}$

1e.19	$\begin{aligned}x &= \arcsin \sqrt{t} \\y &= \sqrt{1 + \sqrt{t}}\end{aligned}$	1e.20	$\begin{aligned}x &= \arcsin^2 t \\y &= t / \sqrt{1 - t^2}\end{aligned}$
1e.21	$\begin{aligned}x &= t \sqrt{t^2 + 1} \\y &= \ln \frac{1 + \sqrt{1 + t^2}}{t}\end{aligned}$	1e.22	$\begin{aligned}x &= \operatorname{arctg} t \\y &= \ln \frac{\sqrt{1 + t^2}}{t + 1}\end{aligned}$
1e.23	$\begin{aligned}x &= \ln(1 - t^2) \\y &= \arcsin \sqrt{1 - t^2}\end{aligned}$	1e.24	$\begin{aligned}x &= \operatorname{arctg}((t + 1)/(t - 1)) \\y &= \arcsin \sqrt{1 - t^2}\end{aligned}$
1e.25	$\begin{aligned}x &= \ln \sqrt{\frac{1 - \sin t}{1 + \sin t}} \\y &= (1/2) \operatorname{tg}^2 t + \ln \cos t\end{aligned}$	1e.26	$\begin{aligned}x &= \sqrt{t - t^2} - \operatorname{arctg} \sqrt{\frac{1 - t}{t}} \\y &= \sqrt{t} - \sqrt{1 - t} \arcsin \sqrt{t}\end{aligned}$
1e.27	$\begin{aligned}x &= \ln \operatorname{tg} t \\y &= \frac{1}{\sin^2 t}\end{aligned}$	1e.28	$\begin{aligned}x &= \frac{t^2 \ln t}{1 - t^2} + \ln \sqrt{1 - t^2} \\y &= \frac{t \arcsin t}{\sqrt{1 - t^2}} + \ln \sqrt{1 - t^2}\end{aligned}$
1e.29	$\begin{aligned}x &= e^{\sec^2 t} \\y &= \operatorname{tg} t \ln \cos t + \operatorname{tg} t - t\end{aligned}$	1e.30	$\begin{aligned}x &= \ln(t + \sqrt{1 + t^2}) \\y &= \sqrt{1 + t^2} - \ln \frac{1 + \sqrt{1 + t^2}}{t}\end{aligned}$

### Задание № 2а

Составьте уравнение нормали и уравнение касательной к данной кривой в точке с абсциссой  $x_0$

2a.1	$y = \frac{4x - x^2}{4}, x_0 = 2$	2a.2	$y = \frac{1 + \sqrt{x}}{1 - \sqrt{x}}, x_0 = 4$
2a.3	$y = 2x^2 + 3x - 1, x_0 = -2$	2a.4	$y = x - x^3, x_0 = -1$
2a.5	$y = x + \sqrt{x^3}, x_0 = 1$	2a.6	$y = \sqrt[3]{x^2} - 20, x_0 = -8$
2a.7	$y = x^2 + 8\sqrt{x} - 32, x_0 = 4$	2a.8	$y = 8\sqrt[4]{x} - 70, x_0 = 16$
2a.9	$y = 2x^3 - 3x + 1, x_0 = 1$	2a.10	$y = 2x^2 + 3, x_0 = -1$

2a.11	$y = \frac{x^2 - 3x + 6}{x^2}, x_0 = 3$	2a.12	$y = \frac{x^3 + 2}{x^3 - 2}, x_0 = 2$
2a.13	$y = \sqrt{x} - 3\sqrt[3]{x}, x_0 = 64$	2a.14	$y = 3(\sqrt[3]{x} - 2\sqrt{x}), x_0 = 1$
2a.15	$y = \frac{3x - 2x^3}{3}, x_0 = 1$	2a.16	$y = \frac{x^{29} + 6}{x^4 + 1}, x_0 = 1$
2a.17	$y = 14\sqrt{x} - 15\sqrt[3]{x} + 2, x_0 = 1$	2a.18	$y = 3\sqrt[4]{x} - \sqrt{x}, x_0 = 1$
2a.19	$y = \frac{2x + 1}{x}, x_0 = 1$	2a.20	$y = \frac{-2(x^8 + 2)}{3(x^4 + 1)}, x_0 = 1$
2a.21	$y = \frac{x^5 + 1}{x^4 + 1}, x_0 = 1$	2a.22	$y = \frac{x^{16} + 9}{1 - 5x^2}, x_0 = 1$
2a.23	$y = \frac{1}{3x + 2}, x_0 = 2$	2a.24	$y = \frac{x}{x^2 + 2}, x_0 = -2$
2a.25	$y = \frac{x^2 - 3x + 3}{3}, x_0 = 3$	2a.26	$y = \frac{2x}{x^2 + 1}, x_0 = 1$
2a.27	$y = \frac{1 + 3x^2}{3 + x^2}, x_0 = 1$	2a.28	$y = \frac{x^2}{10} + 3, x_0 = 2$
2a.29	$y = -2(\sqrt[3]{x} + 3\sqrt{x}), x_0 = 1$	2a.30	$y = \frac{x^2 - 2x - 3}{4}, x_0 = 4$

**Задание № 2 б**  
Найдите угол между линиями.

26.1	$y = \sqrt{2x}; y = \frac{x^2}{2}$	26.2	$y = \frac{1}{x}; y = x$
26.3	$x^2 + y^2 - 4x = 1;$ $x^2 + y^2 - 2y = 9$	26.4	$y = \sin x; y = \cos x;$ $x \in [0; 2\pi]$
26.5	$y = x^2; y = \sqrt{x}$	26.6	$y = \sqrt{1 - x^2}; y = \sqrt{x}$

26.7	$y = x^3 - x; \quad y = \frac{12}{x}$	26.8	$x^2 + y^2 = 8ax; \quad y^2 = \frac{x}{2a - x}$
26.9	$y = x^2; \quad y = x^3$	26.10	$y = (x - 2)^2; \quad y = 4x - x^2 + 4$
26.11	$y = 2x^2 - 5; \quad y = x^2 - 3x + 5$	26.12	$y = 2x^3 - x; \quad x + y = 2$
26.13	$y = x - x^3; \quad y = 5x$	26.14	$y = 1 + \sin x; \quad y = 1$
26.15	$x^2 + y^2 = 5; \quad y^2 = 4x$	26.16	$y = \sqrt{2} \sin x; \quad y = \sqrt{2} \cos x$
26.17	$y = x^3; \quad y = \frac{1}{x^2}$	26.18	$y = \frac{1}{x}; \quad y = \sqrt{x}$
26.19	$y = 8 - x^2; \quad y = x^2$	26.20	$y = 2x^2; \quad y = x^3 + 2x^2 - 1$
26.21	$x^3 + y^3 - xy - 7 = 0;$ $y = x + 1$	26.22	$x^2 + y^2 = 4;$ $x + 2y = 2$
26.23	$y = x^2; \quad y = 5x$	26.24	$y = x^2; \quad x = y^2$
26.25	$y = \ln x; \quad y = \frac{x^2}{2e}$	26.26	$y = \frac{2}{3}x^5 - \frac{1}{9}x^3; \quad x = 1$
26.27	$y = x^2 - 4x + 4;$ $y = -x^2 + 6x - 4$	26.28	$y = 4x^2 + 2x - 8;$ $y = x^3 - x + 10$
26.29	$y = x^2 \ln x; \quad y = 4 - 4x^2$	26.30	$y^2 = 2x^3; \quad 64x - 48y - 11 = 0$

**Задание № 3а**  
Вычислите пределы, используя правило Лопитала

3a.1	$\lim_{x \rightarrow 1} \frac{\ln(x+5)}{\sqrt[4]{x+3}}$	3a.2	$\lim_{x \rightarrow 1} \frac{a^{\ln x} - x}{x - 1}$
3a.3	$\lim_{x \rightarrow 0} \frac{\operatorname{tg} x - x}{x - \sin x}$	3a.4	$\lim_{x \rightarrow 1} \frac{1 - 4 \sin^2(p x / 6)}{1 - x^2}$
3a.5	$\lim_{x \rightarrow a} \arcsin \frac{x-a}{a} \Psi \operatorname{tg}(x-a)$	3a.6	$\lim_{x \rightarrow 1} (p - 2 \operatorname{arctg} x) \ln x$
3a.7	$\lim_{x \rightarrow 1} (a^{1/x} - 1)x$	3a.8	$\lim_{x \rightarrow 1} \frac{\frac{x}{3} \frac{1}{\ln x} - \frac{x}{\ln x} \frac{1}{x}}{\frac{1}{\ln x} - \frac{1}{x}}$

3a.9	$\lim_{x \rightarrow 0} \frac{1 - \cos x^2}{x^2 - \sin x^2}$	3a.10	$\lim_{x \rightarrow 0} \frac{\operatorname{tg} x - x}{2 \sin x + x}$
3a.11	$\lim_{x \rightarrow 1} \frac{e^{1/x^2} - 1}{2 \operatorname{arctg} x^2 - p}$	3a.12	$\lim_{x \rightarrow 1} \frac{x^3 - 2x^2 - x + 2}{x^3 - 7x + 6}$
3a.13	$\lim_{x \rightarrow 0} \frac{x \cos x - \sin x}{x^3}$	3a.14	$\lim_{x \rightarrow 1} \frac{e^x}{x^5}$
3a.15	$\lim_{x \rightarrow 1} \frac{1 - x}{1 - \sin(px/2)}$	3a.16	$\lim_{x \rightarrow 1} \frac{\ln x}{\sqrt[3]{x}}$
3a.17	$\lim_{x \rightarrow 0} \frac{\operatorname{ch} x - 1}{1 - \cos x}$	3a.18	$\lim_{x \rightarrow 0} \frac{p/x}{\operatorname{ctg}(px/2)}$
3a.19	$\lim_{x \rightarrow 0} \frac{\ln(\sin mx)}{\ln(\sin x)}$	3a.20	$\lim_{x \rightarrow p/2} \frac{\operatorname{tg} x}{\operatorname{tg} 5x}$
3a.21	$\lim_{x \rightarrow p/4} \frac{1/\cos^2 x - 2\operatorname{tg} x}{1 + \cos 4x}$	3a.22	$\lim_{x \rightarrow 0} (1 - \cos x) \operatorname{ctg} x$
3a.23	$\lim_{x \rightarrow 1} (1 - x) \operatorname{tg}(px/2)$	3a.24	$\lim_{x \rightarrow 1} x \sin(3/x)$
3a.25	$\lim_{x \rightarrow -1} \frac{\sqrt[3]{1+2x} + 1}{\sqrt{2+x} + x}$	3a.26	$\lim_{x \rightarrow 0} \frac{x \cos x - \sin x}{x^3}$
3a.27	$\lim_{x \rightarrow 1} \frac{1 - x}{1 - \sin(px/2)}$	3a.28	$\lim_{x \rightarrow 0} \frac{\operatorname{tg} x - \sin x}{4x - \sin x}$
3a.29	$\lim_{x \rightarrow p/2} \frac{\operatorname{tg} 3x}{\operatorname{tg} 5x}$	3a.30	$\lim_{x \rightarrow p/4} \frac{\sec^2 - 2\operatorname{tg} x}{1 + \cos 4x}$

### Задание № 36

Вычислите пределы, используя правило Лопитала

36.1	$\lim_{x \rightarrow 0} \frac{1 - \cos 8x}{\operatorname{tg}^2 2x}$	36.2	$\lim_{x \rightarrow 1} x^4 \sin \frac{3\pi - \pi}{4x}$
36.3	$\lim_{x \rightarrow 1} \ln x \operatorname{tg}(x - 1)$	36.4	$\lim_{x \rightarrow p} (p - x) \operatorname{tg}(x/2)$

36.5	$\lim_{x \rightarrow 3} \frac{\frac{1}{\sqrt[3]{x}} - \frac{5}{x^2} - \frac{1}{x-6}}{x-3}$	36.6	$\lim_{x \rightarrow 1} \frac{\frac{1}{\sqrt[3]{2(1-\sqrt{x})}} - \frac{1}{3(1-\sqrt[3]{x})}}{x-1}$
36.7	$\lim_{x \rightarrow 0} \frac{e^{ax} - e^{bx}}{\sin x}$	36.8	$\lim_{x \rightarrow p/2} \frac{\frac{x}{\sqrt[3]{\operatorname{ctg} x}} - \frac{p}{2 \cos x}}{x-p/2}$
36.9	$\lim_{x \rightarrow 0} \frac{x - \operatorname{arctg} x}{x^3}$	36.10	$\lim_{x \rightarrow p/(2a)} \frac{1 - \sin ax}{(2ax - p)^2}$
36.11	$\lim_{x \rightarrow p/6} \frac{1 - 2 \sin x}{\cos 3x}$	36.12	$\lim_{x \rightarrow 0} \frac{e^{2x} - 1}{\ln(1+2x)}$
36.13	$\lim_{x \rightarrow 0} \frac{a^x - 1}{c^x - 1}$	36.14	$\lim_{x \rightarrow 1} \frac{\ln x}{1 - x^3}$
36.15	$\lim_{x \rightarrow 1} \frac{\ln x}{\operatorname{ctg} x}$	36.16	$\lim_{x \rightarrow 0} \frac{1 - \cos ax}{1 - \cos bx}$
36.17	$\lim_{x \rightarrow a} \frac{x - a}{x^n - a^n}$	36.18	$\lim_{x \rightarrow 0} \frac{e^x - 1}{\sin 2x}$
36.19	$\lim_{x \rightarrow 0} (x \ln x)$	36.20	$\lim_{x \rightarrow 0} (1 - e^{2x}) \operatorname{ctg} x$
36.21	$\lim_{x \rightarrow 0} \frac{\frac{1}{\sqrt[3]{x \sin x}} - \frac{1}{x^2}}{x-0}$	36.22	$\lim_{x \rightarrow 0} \frac{a^x - b^x}{x \sqrt{1-x}}$
36.23	$\lim_{x \rightarrow 0} \frac{e^{x^3} - 1 - x^3}{\sin^2 2x}$	36.24	$\lim_{x \rightarrow 0} \frac{e^{a\sqrt{x}} - 1}{\sqrt{\sin bx}}$
36.25	$\lim_{x \rightarrow 0} \frac{\ln(1+x^2)}{\cos 3x - e^{-x}}$	36.26	$\lim_{x \rightarrow 1} \frac{e^x}{x^5}$
36.27	$\lim_{x \rightarrow +\infty} \frac{\ln(x+7)}{\sqrt[7]{x-3}}$	36.28	$\lim_{x \rightarrow 0} \frac{p/x}{\operatorname{ctg}(5x/2)}$
36.29	$\lim_{x \rightarrow 0} (1 - \cos 2x) \operatorname{ctg} 4x$	36.30	$\lim_{x \rightarrow 1} (x^2 \sin b/x)$

### Задание № 3в

Вычислите пределы, используя правило Лопиталля

3в.1	$\lim_{x \rightarrow 0} \frac{\arcsin 4x}{5 - 5e^{-3x}}$	3в.2	$\lim_{x \rightarrow 0} \frac{\ln \cos x}{x}$
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3B.3	$\lim_{x \rightarrow 0} \frac{e^{x^2} - 1}{\cos x - 1}$	3B.4	$\lim_{x \rightarrow 0} \frac{e^x - x^2/2 - x - 1}{\cos x - x^2/2 - 1}$
3B.5	$\lim_{x \rightarrow 0} \frac{e^{tgx} - 1}{tgx - x}$	3B.6	$\lim_{x \rightarrow 1} \frac{\ln(1-x) + tg(px/2)}{ctgp x}$
3B.7	$\lim_{x \rightarrow a} \frac{\cos x \ln(x-a)}{\ln(e^x - e^a)}$	3B.8	$\lim_{x \rightarrow 1} \frac{1}{\cos(px/2) \ln(1-x)}$
3B.9	$\lim_{x \rightarrow 0} \frac{e^{ax} - \cos bx}{e^{bx} - \cos bx}$	3B.10	$\lim_{x \rightarrow 0} \frac{\cos(e^{x^2} - 1)}{\cos x - 1}$
3B.11	$\lim_{x \rightarrow a} \frac{x^m - a^m}{x^n - a^n}$	3B.12	$\lim_{x \rightarrow 1} x \sin \frac{a}{6x}$
3B.13	$\lim_{x \rightarrow 0} \frac{3tg4x - 12tgx}{3\sin 4x - 12\sin x}$	3B.14	$\lim_{x \rightarrow p/4} \frac{\sqrt{tgx} - 1}{2\sin^2 x - 1}$
3B.15	$\lim_{x \rightarrow 0} \frac{x(e^x + 1) - 2(e^x - 1)}{x^3}$	3B.16	$\lim_{x \rightarrow 0} \frac{\arcsin 2x - 2\arcsin x}{x^3}$
3B.17	$\lim_{x \rightarrow 0} \frac{a^x - a^{\sin x}}{x^3}$	3B.18	$\lim_{x \rightarrow p/4} (tgx)^{tg 2x}$
3B.19	$\lim_{x \rightarrow 0} \frac{\ln(\cos ax)}{\ln(\cos bx)}$	3B.20	$\lim_{x \rightarrow p/4} \frac{\sqrt[3]{tgx} - 1}{2\sin^2 x - 1}$
3B.21	$\lim_{x \rightarrow 0} \frac{\frac{1}{3}x^3 - \frac{1}{e^x - 1} \frac{1}{2}x^2}{x^3}$	3B.22	$\lim_{x \rightarrow 0} \frac{\ln(1 + xe^x)}{\ln(x + \sqrt{1 + x^2})}$
3B.23	$\lim_{x \rightarrow 1} x^2 e^{-0,01x}$	3B.24	$\lim_{x \rightarrow 1} (1-x)^{\log_2 x}$
3B.25	$\lim_{x \rightarrow 1} \frac{e^{4/x^2} - 1}{2\arctg x^2 - p}$	3B.26	$\lim_{x \rightarrow 1/2} \frac{\frac{1}{3}x^3 - \frac{1}{\ln 3x - 1} \frac{1}{2}x^2}{x^3}$
3B.27	$\lim_{x \rightarrow 1/2} \ln 2x \ln(2x-1)$	3B.28	$\lim_{x \rightarrow 0} \arcsin x \ln g x$
3B.29	$\lim_{x \rightarrow 1} (x^3 e^{-x})$	3B.30	$\lim_{x \rightarrow 1} (x-1)^{x-1}$

### Задание № 3г

Вычислите пределы, используя правило Лопиталя

3Г.1	$\lim_{x \rightarrow 0} (1 - \sin 2x)^{ctgx}$	3Г.2	$\lim_{x \rightarrow 0} (\ln(1/x))^x$
3Г.3	$\lim_{x \rightarrow 0} (\cos x)^{ctg^2 x}$	3Г.4	$\lim_{x \rightarrow 0} x^x$
3Г.5	$\lim_{x \rightarrow 1} (\ln 2x)^{1/\ln x}$	3Г.6	$\lim_{x \rightarrow 0} (1 + \sin^2 x)^{1/tg^2 x}$
3Г.7	$\lim_{x \rightarrow 1} (1 - x)^{\ln x}$	3Г.8	$\lim_{x \rightarrow 0} (\ln(x + e))^{1/x}$
3Г.9	$\lim_{x \rightarrow 0} (\sin x)^{gx}$	3Г.10	$\lim_{x \rightarrow 1} \sqrt[x]{x}$
3Г.11	$\lim_{x \rightarrow 0} x^{\sin x}$	3Г.12	$\lim_{x \rightarrow 1} (1 - x)^{\cos(px/2)}$
3Г.13	$\lim_{x \rightarrow 0} (1 + x^2)^{1/x}$	3Г.14	$\lim_{x \rightarrow 1} x^{1/(x-1)}$
3Г.15	$\lim_{x \rightarrow 1} \frac{\frac{x}{3} \operatorname{tg} \frac{px}{4}}{\frac{1}{4}}$	3Г.16	$\lim_{x \rightarrow 1} \frac{\frac{x}{3} \operatorname{ctg} \frac{px}{4}}{\frac{1}{4}}$
3Г.17	$\lim_{x \rightarrow 0} \frac{\frac{x}{3} \operatorname{tg} x}{\frac{1}{4} x}$	3Г.18	$\lim_{x \rightarrow 1} \frac{\frac{x}{3} - \frac{4}{3} x}{\frac{1}{4} x + \frac{3}{4}}$
3Г.19	$\lim_{x \rightarrow 0} (\operatorname{ctgx})^{\sin x}$	3Г.20	$\lim_{x \rightarrow 1} (\ln x)^{1/x}$
3Г.21	$\lim_{x \rightarrow 1} x^{6/(1+2\ln x)}$	3Г.22	$\lim_{x \rightarrow 1} (1 - e^x)^{1/x}$
3Г.23	$\lim_{x \rightarrow 1} (x - 1)^{1/\ln(2(x-1))}$	3Г.24	$\lim_{x \rightarrow 1} \frac{\frac{x}{3} \cos \frac{m}{x}}{\frac{1}{x}}$
3Г.25	$\lim_{x \rightarrow 0} (\operatorname{ctg} 2x)^{1/\ln x}$	3Г.26	$\lim_{x \rightarrow 1} x^2 \sin(a/x)$
3Г.27	$\lim_{x \rightarrow 5} \frac{\frac{1}{3} \frac{1}{x-5}}{\frac{5}{x^2 - x - 20}}$	3Г.28	$\lim_{x \rightarrow 1} \frac{\frac{1}{3} \frac{1}{2(1-\sqrt{x})}}{\frac{1}{3(1-\sqrt[3]{x})}}$
3Г.29	$\lim_{x \rightarrow 1} (1 - x)^{\cos(px/2)}$	3Г.30	$\lim_{x \rightarrow 0} (\operatorname{ctgx})^{\sin x}$

### Задание № 4а

Найдите наименьшее и наибольшее значения функции  $y = f(x)$   
на отрезке  $[a; b]$

4a.1	$y = \ln(x^2 - 2x + 2)$ , $[0; 3]$	4a.2	$y = (x + 2)e^{1-x}$ , $[-2; 2]$
4a.3	$y = \frac{2x-1}{(x-1)^2}$ , $[-1/2; 0]$	4a.4	$y = \frac{3x}{x^2 + 1}$ , $[0; 5]$
4a.5	$y = \ln(x^2 - 2x + 4)$ , $[-1; 3/2]$	4a.6	$y = \sqrt{x - x^3}$ , $[-2; 2]$
4a.7	$y = \frac{x^3}{x^2 - x + 1}$ , $[-1; 1]$	4a.8	$y = \frac{3x+1}{x}$ , $[1; 2]$
4a.9	$y = 4 - e^{-x^2}$ , $[0; 1]$	4a.10	$y = xe^x$ , $[-2; 0]$
4a.11	$y = \frac{x^3 + 4}{x^2}$ , $[1; 2]$	4a.12	$y = \frac{x}{9 - x^2}$ , $[-2; 2]$
4a.13	$y = (x - 2)e^x$ , $[-2; 1]$	4a.14	$y = (x - 1)e^{-x}$ , $[0; 3]$
4a.15	$y = \frac{1 + \ln x}{x}$ , $[1/e; e]$	4a.16	$y = \frac{x^5 - 8}{x^4}$ , $[-3; -1]$
4a.17	$y = e^{4x - x^2}$ , $[1; 3]$	4a.18	$y = x \ln x$ , $\frac{1}{e}/e^2; 1\frac{1}{e}$
4a.19	$y = \frac{e^{2x} + 1}{e^x}$ , $[-1; 2]$	4a.20	$y = \frac{x^2 - 2x + 2}{x - 1}$ , $[-1; 3]$
4a.21	$y = x^3 e^{x+1}$ , $[-4; 0]$	4a.22	$y = (x+1)\sqrt[3]{x^2}$ , $[-4/5; 3]$
4a.23	$y = e^{6x - x^2}$ , $[-3; 3]$	4a.24	$y = 3x^4 - 16x^3 + 2$ , $[-3; 1]$
4a.25	$y = \frac{\ln x}{x}$ , $[1; 4]$	4a.26	$y = \frac{x^4}{4} - 6x^3 + 7$ , $[16; 20]$
4a.27	$y = x^5 - 5x^4 + 5x^3 + 1$ , $[-1; 2]$	4a.28	$y = (3 - x)e^{-x}$ , $[0; 5]$
4a.29	$y = 3/2 + \cos x$ , $[0; p/2]$	4a.30	$y = 108x - x^4$ , $[-1; 4]$

### Задание № 5а

Найдите производную указанного порядка

5a.1	$y = (2x^2 - 7)\ln(x - 1)$ , $y^V = ?$	5a.2	$y = (3 - x^2)\ln^2 x$ , $y^{III} = ?$
5a.3	$y = x \cos x^2$ , $y^{III} = ?$	5a.4	$y = (4x^3 + 5)e^{2x+1}$ , $y^V = ?$
5a.5	$y = \frac{\ln(x - 1)}{\sqrt{x - 1}}$ , $y^{III} = ?$	5a.6	$y = \frac{\log_2 x}{x^3}$ , $y^{III} = ?$
5a.7	$y = x^2 \sin(5x - 3)$ , $y^{III} = ?$	5a.8	$y = (2x + 3)\ln^2 x$ , $y^{III} = ?$
5a.9	$y = \frac{\ln x}{x^2}$ , $y^{IV} = ?$	5a.10	$y = \frac{\ln x}{x^3}$ , $y^{IV} = ?$
5a.11	$y = (1 + x^2) \operatorname{arctg} x$ , $y^{III} = ?$	5a.12	$y = (4x + 3)2^{-x}$ , $y^V = ?$
5a.13	$y = e^{1-2x} \sin(2 + 3x)$ , $y^{IV} = ?$	5a.14	$y = (x^2 + 3)\ln(x - 3)$ , $y^{IV} = ?$
5a.15	$y = (1 - x - x^2)e^{\frac{x-1}{2}}$ , $y^{IV} = ?$	5a.16	$y = \frac{\ln(3 + x)}{3 + x}$ , $y^{III} = ?$
5a.17	$y = (2x^3 + 1)\cos x$ , $y^V = ?$	5a.18	$y = (1/x)\sin 2x$ , $y^{III} = ?$
5a.19	$y = (x + 7)\ln(x + 4)$ , $y^V = ?$	5a.20	$y = (3x - 7)3^{-x}$ , $y^{IV} = ?$
5a.21	$y = \frac{\ln(2x + 5)}{2x + 5}$ , $y^{III} = ?$	5a.22	$y = \frac{\ln x}{x^5}$ , $y^{III} = ?$
5a.23	$y = e^{x/2} \sin 2x$ , $y^{IV} = ?$	5a.24	$y = x \ln(1 - 3x)$ , $y^{IV} = ?$
5a.25	$y = (x^2 + 3x + 1)e^{3x}$ , $y^V = ?$	5a.26	$y = (5x - 8)2^{-x}$ , $y^{IV} = ?$
5a.27	$y = \frac{\ln(x - 2)}{x - 2}$ , $y^V = ?$	5a.28	$y = \frac{\log_3 x}{x^2}$ , $y^{IV} = ?$
5a.29	$y = (5x - 1)\ln^2 x$ , $y^{III} = ?$	5a.30	$y = (x^3 + 2)e^{4x+3}$ , $y^{IV} = ?$

### Задание № 5б

Вычислите производные  $\dot{y}$  и  $\ddot{y}$  от функций, заданных параметрически

56.1	$\begin{array}{l} \overset{\text{М}}{\text{H}} x = (2t + 3) \cos t \\ \overset{\text{Н}}{\text{H}} y = 3t^3 \end{array}$	56.2	$\begin{array}{l} \overset{\text{М}}{\text{H}} x = 2 \cos^2 t \\ \overset{\text{Н}}{\text{H}} y = 3 \sin^2 t \end{array}$
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56.3	$\begin{aligned}x &= 6\cos^3 t \\y &= 2\sin^3 t\end{aligned}$	56.4	$\begin{aligned}x &= 1/(t + 2) \\y &= (t/(t + 2))^2\end{aligned}$
56.5	$\begin{aligned}x &= e^{-2t} \\y &= e^{4t}\end{aligned}$	56.6	$\begin{aligned}x &= \sqrt{t} \\y &= \sqrt[5]{t}\end{aligned}$
56.7	$\begin{aligned}x &= 2t/(1+t^3) \\y &= t^2/(1+t^2)\end{aligned}$	56.8	$\begin{aligned}x &= \sqrt{t^2 - 1} \\y &= (t+1)/\sqrt{t^2 - 1}\end{aligned}$
56.9	$\begin{aligned}x &= 4t + 2t^2 \\y &= 5t^3 - 3t^2\end{aligned}$	56.10	$\begin{aligned}x &= (\ln t)/t \\y &= t \ln t\end{aligned}$
56.11	$\begin{aligned}x &= e^{t \cos t} \\y &= e^t \sin t\end{aligned}$	56.12	$\begin{aligned}x &= t^4 \\y &= \ln t\end{aligned}$
56.13	$\begin{aligned}x &= 5 \cos t \\y &= 4 \sin t\end{aligned}$	56.14	$\begin{aligned}x &= 5 \cos^2 t \\y &= 3 \sin^2 t\end{aligned}$
56.15	$\begin{aligned}x &= \arctan t \\y &= \ln(1+t^2)\end{aligned}$	56.16	$\begin{aligned}x &= \arcsin t \\y &= \sqrt{1-t^2}\end{aligned}$
56.17	$\begin{aligned}x &= 3(t - \sin t) \\y &= 3(1 - \cos t)\end{aligned}$	56.18	$\begin{aligned}x &= 3(\sin t - t \cos t) \\y &= 3(\cos t + t \sin t)\end{aligned}$
56.19	$\begin{aligned}x &= \sin 2t \\y &= \cos^2 t\end{aligned}$	56.20	$\begin{aligned}x &= e^{3t} \\y &= e^{-3t}\end{aligned}$
56.21	$\begin{aligned}x &= (\ln t/t) \\y &= t^2 \ln t\end{aligned}$	56.22	$\begin{aligned}x &= \arccos t \\y &= \sqrt{1-t^2}\end{aligned}$
56.23	$\begin{aligned}x &= 1/(t+1) \\y &= (t/(t+1))\end{aligned}$	56.24	$\begin{aligned}x &= 5 \sin^3 t \\y &= 3 \cos^3 t\end{aligned}$
56.25	$\begin{aligned}x &= e^{-3t} \\y &= e^{8t}\end{aligned}$	56.26	$\begin{aligned}x &= \sqrt[3]{(t-1)^2} \\y &= \sqrt{t-1}\end{aligned}$
56.27	$\begin{aligned}x &= \ln^2 t \\y &= t + \ln t\end{aligned}$	56.28	$\begin{aligned}x &= te^t \\y &= t/e^t\end{aligned}$

56.29 $\frac{M}{H} x = 6t^2 - 4$ $\frac{H}{D} y = 3t^5$	56.30 $\frac{M}{H} x = \arcsin t$ $\frac{H}{D} y = \ln t$
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### Задание № 5в

Разложите полином по степеням  $(x - x_0)$ , сделайте проверку, либо раскрыв скобки в разложении, либо разделив данный многочлен на  $(x - x_0)$ .

5в.1	$P_3(x) = x^3; x_0 = 1$
5в.2	$P_4(x) = x^4 + 8x^3 + 24x^2 + 23x + 17; x_0 = -2$
5в.3	$P_3(x) = 1 + x^2 + x^3; x_0 = -1$
5в.4	$P_6(x) = (x^3 - 8)^2; x_0 = 2$
5в.5	$P_3(x) = 2x^3 - 3x^2 + 5x + 1; x_0 = -1$
5в.6	$P_4(x) = 2x^4 - 5x^3 - 3x^2 + 8x + 4; x_0 = 2$
5в.7	$P_4(x) = x^4 - 2x^3 + 7x - 4; x_0 = 1$
5в.8	$P_6(x) = (x^2 - 2x + 3)^3; x_0 = 0$
5в.9	$P_3(x) = 4x^3 - 2x^2 + 5x - 1; x_0 = 1$
5в.10	$P_4(x) = 6x^4 + 5x^2 - 12; x_0 = -1$
5в.11	$P_6(x) = (3x^2 - 2x + 1)^3; x_0 = 0$
5в.12	$P_5(x) = 2x^5 - 10x^4 - 3x + 5; x_0 = 1$
5в.13	$P_4(x) = 8x^4 - 3x^2 + 2; x_0 = -2$
5в.14	$P_3(x) = 9x^3 + 12x^2 - 4; x_0 = 3$
5в.15	$P_4(x) = x^4 - 5x^3 + 3x^2 - 7x + 2; x_0 = -1$
5в.16	$P_6(x) = (11x^2 - 5x + 4)^3; x_0 = 0$
5в.17	$P_3(x) = 2x^3 + 3x^2 - 5x + 10; x_0 = -3$
5в.18	$P_6(x) = x^6; x_0 = 5$
5в.19	$P_6(x) = (3x^2 - x + 5)^3; x_0 = 0$

5в.20	$P_4(x) = 2x^4 - 3x^3 + 2x^2 + x - 1; \quad x_0 = 4$
5в.21	$P_3(x) = 24x^3 + 15x^2 - 11x - 3; \quad x_0 = -4$
5в.22	$P_5(x) = 2x^5 - 3x^2 + 10; \quad x_0 = -1$
5в.23	$P_4(x) = 3x^4 - 2x^2 + 1; \quad x_0 = 2$
5в.24	$P_3(x) = 5x^3 + x^2 - 20; \quad x_0 = -5$
5в.25	$P_6(x) = (2x^3 + 3x^2 - 1)^2; \quad x_0 = 0$
5в.26	$P_4(x) = x^4 - 2x^3 + 3x^2 - 10; \quad x_0 = 6$
5в.27	$P_5(x) = x^5 + 6x^4 - 4x^3 + 3x^2 + 2; \quad x_0 = -1$
5в.28	$P_4(x) = (2x^2 + 3x - 4)^2; \quad x_0 = 1$
5в.29	$P_5(x) = 3x^5 - 11x^3 + 9; \quad x_0 = -7$
5в.30	$P_3(x) = 4x^3 - 3x^2 + x - 1; \quad x_0 = 7$

### Задание № 5г

Разложите по формуле Маклорена заданные функции  $f(x)$  до  $o(x^n)$ .

5Г.1	$f(x) = e^{5x-1}$	5Г.2	$f(x) = \sin(2x+3)$
5Г.3	$f(x) = \cos(\frac{x}{2} + 2)$	5Г.4	$f(x) = \ln(ex+2)$
5Г.5	$f(x) = \frac{1}{1-2x}$	5Г.6	$f(x) = \frac{1}{3x+4}$
5Г.7	$f(x) = \frac{1}{\sqrt{1+4x}}$	5Г.8	$f(x) = \frac{1}{(1-x)^2}$
5Г.9	$f(x) = 3^{2-x}$	5Г.10	$f(x) = (x-1)e^{x/2}$
5Г.11	$f(x) = (x^2 - x)e^{-x}$	5Г.12	$f(x) = (2x+1)\sqrt{1-x}$
5Г.13	$f(x) = \frac{x^2 + 3x}{e^{2x}}$	5Г.14	$f(x) = \ln \frac{1+2x}{1-x}$
5Г.15	$f(x) = (2x-3)\ln(5x+6)$	5Г.16	$f(x) = \ln(x^2 + 3x + 2)$
5Г.17	$f(x) = \ln(2+x-x^2)$	5Г.18	$f(x) = ch(\sin x), \quad \text{до } o(x^2)$

5Г.19	$f(x) = \ln \frac{2 - 3x}{3 + 2x}$	5Г.20	$f(x) = e^{tgx}, \text{ до } o(x^2)$
5Г.21	$f(x) = e^{\sqrt{1+2x}}, \text{ до } o(x^2)$	5Г.22	$f(x) = \cos(sh \frac{x}{\sqrt{5}}), \text{ до } o(x^2)$
5Г.23	$f(x) = (1 - x + x^2)^3, \text{ до } o(x^2)$	5Г.24	$f(x) = \ln \cos x, \text{ до } o(x^2)$
5Г.25	$f(x) = arctg(\sin x), \text{ до } o(x^3)$	5Г.26	$f(x) = e^{\sin x}, \text{ до } o(x^3)$
5Г.27	$f(x) = \ln^3(1 - x/2), \text{ до } o(x^3)$	5Г.28	$f(x) = \sqrt[3]{1 + 3 \sin x}, \text{ до } o(x^3)$
5Г.29	$f(x) = \ln(1 + \arcsin x) \text{ до } o(x^3)$	5Г.30	$f(x) = \sqrt[3]{1 - 3 \cos 2x}, \text{ до } o(x^3)$

**Задание № 6а**  
Найдите дифференциал  $dy$

6a.1	$y = x \arcsin \frac{1}{x} - \ln \left  x + \sqrt{x^2 - 1} \right , x > 0$
6a.2	$y = tg(2 \arccos \sqrt{1 - 2x^2}), x > 0$
6a.3	$y = \sqrt{1 + 2x} - \ln(x + \sqrt{1 + 2x})$
6a.4	$y = x^2 arctg \sqrt{x^2 - 1} - \sqrt{x^2 - 1}$
6a.5	$y = \arccos(1/\sqrt{1 + 2x^2}), x > 0$
6a.6	$y = x \ln \left  x + \sqrt{x^2 + 3} \right  - \sqrt{x^2 + 3}$
6a.7	$y = arctg(shx) + shx \ln(chx)$
6a.8	$y = \arccos((x^2 - 1)/(x^2 \sqrt{2}))$
6a.9	$y = \ln(\cos^2 x + \sqrt{1 + \cos^4 x})$
6a.10	$y = \ln(x + \sqrt{1 + x^2}) - \sqrt{1 + x^2} arctgx$
6a.11	$y = \ln(e^x + \sqrt{e^{2x} - 1}) + \arcsin e^{-x}$
6a.12	$y = \frac{\ln x }{1 + x^2} - \frac{1}{2} \ln \frac{x^2}{1 + x^2}$

6a.13	$y = x\sqrt{4 - x^2} + 4\arcsin(x/2)$
6a.14	$y = \ln \operatorname{tg} \frac{\frac{x}{3}}{\frac{1}{2}} - \frac{x}{\sin x}$
6a.15	$y = 2x + \ln \sin x + 2\cos x $
6a.16	$y = \sqrt{ctgx} - \sqrt{\operatorname{tg}^3(x/3)}$
6a.17	$y = \ln \left  \frac{x + \sqrt{x^2 + 1}}{2x} \right $
6a.18	$y = \sqrt[3]{\frac{x+2}{x-2}}$
6a.19	$y = \operatorname{arctg} \frac{x^2 - 1}{x}$
6a.20	$y = \ln x^2 - 1  - \frac{1}{x^2 - 1}$
6a.21	$y = \operatorname{arctg} \frac{\frac{x}{3}}{\frac{1}{2}} + 1$
6a.22	$y = \ln 2x + 2\sqrt{x^2 + x} + 1 $
6a.23	$y = \ln \cos \sqrt{x}  + \sqrt{x} \operatorname{tg} \sqrt{x}$
6a.24	$y = e^x (\cos 2x + 2\sin 2x)$
6a.25	$y = x(\sin \ln x - \cos \ln x)$
6a.26	$y = \frac{\frac{x}{3}\sqrt{x-1}}{\frac{1}{2}} - \frac{1}{2}e^{2\sqrt{x-1}}$
6a.27	$y = \cos x \operatorname{tg} x - \ln \operatorname{tg} \frac{x}{2}$
6a.28	$y = \sqrt{3 + x^2} - x \ln x + \sqrt{3 + x^2} $
6a.29	$y = \sqrt{x} - (1+x) \operatorname{arctg} \sqrt{x}$
6a.30	$y = x \operatorname{arctg} x - \ln \sqrt{1 + x^2}$

### Задание № 6 б

С помощью дифференциала приближенно вычислите данные величины и оцените допущенную относительную погрешность (с точностью до двух знаков после запятой)

66.1	$\sqrt[5]{34}$	66.2	$\sqrt[3]{26,19}$
66.3	$\sqrt[4]{16,64}$	66.4	$\sqrt{8,76}$
66.5	$\sqrt[5]{31}$	66.6	$\sqrt[3]{70}$
66.7	$(2,01)^3 + (2,01)^2$	66.8	$\sqrt[3]{65}$
66.9	$\sqrt{\frac{(2,037)^2 - 3}{(2,037)^2 + 5}}$	66.10	$\sqrt{\frac{4 - 3,02}{1 + 3,02}}$
66.11	$\sqrt[4]{15,8}$	66.12	$\sqrt[3]{10}$
66.13	$\sqrt[5]{200}$	66.14	$(3,03)^5$
66.15	$2,9 / \sqrt{(2,9)^2 + 16}$	66.16	$\sqrt[7]{130}$
66.17	$\sqrt[3]{27,5}$	66.18	$\sqrt{17}$
66.19	$\sqrt{640}$	66.20	$\sqrt{1,2}$
66.21	$\sqrt[10]{1025}$	66.22	$(3,02)^4 + (3,02)^3$
66.23	$(5,07)^3$	66.24	$(4,01)^{1,5}$
66.25	$\sqrt[3]{1,02}$	66.26	$\cos 151^\circ$
66.27	$\arctg 1,05$	66.28	$\cos 61^\circ$
66.29	$\tg 44^\circ$	66.30	$\arctg 0,98$

### Задание № 7а

Постройте графики функций с помощью производной первого порядка.

7a.1	$y = 2x^3 - 9x^2 + 12x - 9$	7a.2	$y = 3x - x^2$
7a.3	$y = x^2(x - 2)^2$	7a.4	$y = 2 - 3x^2 - x^3$
7a.5	$y = (x + 1)^2(x - 1)^2$	7a.6	$y = 2x^3 - 3x^2 - 4$

7a.7	$y = 3x^2 - 2 - x^3$	7a.8	$y = (x - 1)^2(x - 3)^2$
7a.9	$y = \frac{x^3 + 3x^2}{4} - 5$	7a.10	$y = \frac{x^3 - 9x^2}{4} + 6x - 9$
7a.11	$y = 6x - 8x^3$	7a.12	$y = 16x^2(x - 1)^2$
7a.13	$y = 2x^3 + 3x^2 - 5$	7a.14	$y = 2 - 12x^2 - 8x^3$
7a.15	$y = (2x + 1)^2(2x - 1)^2$	7a.16	$y = 2x^3 + 9x^2 + 12x$
7a.17	$y = 12x^2 - 8x^3 - 2$	7a.18	$y = (2x - 1)^2(2x - 3)^2$
7a.19	$y = \frac{27(x^3 - x^2)}{4} - 4$	7a.20	$y = \frac{x(12 - x^2)}{8}$
7a.21	$y = \frac{x^2(x - 4)^2}{16}$	7a.22	$y = \frac{27(x^3 - x^2)}{4} - 5$
7a.23	$y = \frac{16 - 6x^2 - x^3}{8}$	7a.24	$y = -\frac{(x - 4)^2}{16}$
7a.25	$y = 16x^3 - 36x^2 + 24x - 9$	7a.26	$y = \frac{6x^2 - x^3 - 16}{8}$
7a.27	$y = -\frac{1}{16}(x - 2)^2(x - 6)^2$	7a.28	$y = \frac{11 + 9x - 3x^2 - x^3}{8}$
7a.29	$y = 16x^3 - 12x^2 - 4$	7a.30	$y = -\frac{(x + 1)^2(x - 3)^2}{16}$

### Задание № 76

Постройте графики функций с помощью производной первого порядка.

76.1	$y = 1 - \sqrt[3]{x^2 - 2x}$	76.2	$y = 2x - \sqrt[3]{x^2}$
76.3	$y = \frac{12\sqrt[3]{6(x - 2)^2}}{x^2 + 8}$	76.4	$y = -\frac{12\sqrt[3]{6(x - 1)^2}}{x^2 + 2x + 9}$
76.5	$y = 1 - \sqrt[3]{x^2 + 2x}$	76.6	$y = 2x + 6 - 3\sqrt[3]{(x + 3)^2}$
76.7	$y = \frac{6\sqrt[3]{6(x - 3)^2}}{x^2 - 2x + 9}$	76.8	$y = -\frac{6\sqrt[3]{6x^2}}{x^2 + 4x + 12}$
76.9	$y = 1 - \sqrt[3]{x^2 + 4x + 3}$	76.10	$y = 3\sqrt[3]{(x - 3)^2} - 2x + 6$
76.11	$y = 4x + 8 - 6\sqrt[3]{(x + 2)^2}$	76.12	$y = \sqrt[3]{x(x + 2)}$

76.13	$y = \frac{3\sqrt[3]{6(x-4)^2}}{x^2 - 4x + 12}$	76.14	$y = -\frac{3\sqrt[3]{6(x+1)^2}}{x^2 + 6x + 17}$
76.15	$y = \sqrt[3]{x^2 + 4x + 3}$	76.16	$y = 6\sqrt[3]{(x-2)^2} - 4x + 8$
76.17	$y = \frac{3\sqrt[3]{6(x-5)^2}}{x^2 - 6x + 17}$	76.18	$y = -\frac{3\sqrt[3]{6(x+2)^2}}{x^2 + 8x + 24}$
76.19	$y = 2 + \sqrt[3]{8x(x+2)}$	76.20	$y = 6x - 6 - 9\sqrt[3]{(x-1)^2}$
76.21	$y = \sqrt[3]{x^2 + 6x + 8}$	76.22	$y = \sqrt[3]{4x(x-1)}$
76.23	$y = \sqrt[3]{x(x-2)}$	76.24	$y = 1 - \sqrt[3]{x^2 - 4x + 3}$
76.25	$y = 9\sqrt[3]{(x+1)^2} - 6x - 6$	76.26	$y = 8x - 16 - 12\sqrt[3]{(x-2)^2}$
76.27	$y = \frac{6\sqrt[3]{6(x+3)^2}}{x^2 + 10x + 33}$	76.28	$y = -\frac{6\sqrt[3]{6(x-6)^2}}{x^2 - 8x + 24}$
76.29	$y = 12\sqrt[3]{(x+2)^2} - 2x - 8$	76.30	$y = 3\sqrt[3]{(x+4)^2} - 2x - 8$

### Задание № 7в

Исследуйте поведение функций в окрестностях заданных точек с помощью производных высших порядков.

7в.1	$y = x^2 - 4x - (x-2)\ln(x-1),$ $x_0 = 2$	7в.2	$y = 4x - x^2 - 2\cos(x-2),$ $x_0 = 2$
7в.3	$y = 6e^{x-2} - x^3 + 3x^2 - 6x,$ $x_0 = 2$	7в.4	$y = 2\ln(x+1) - 2x + x^2 + 1,$ $x_0 = 0$
7в.5	$y = 2x - x^2 - 2\cos(x-1),$ $x_0 = 1$	17в.6	$y = \cos^2(x+1) + x^2 + 2x,$ $x_0 = -1$
7в.7	$y = 2\ln x + x^2 - 4x + 3,$ $x_0 = 1$	7в.8	$y = 1 - 2x - x^2 - 2\cos(x+1),$ $x_0 = -1$

7в.9	$y = x^2 + 6x + 8 - 2e^{x+2}$ , $x_0 = -2$	7в.10	$y = 4x + x^2 - 2e^{x+1}$ , $x_0 = -1$
7в.11	$y = (x+1)\sin(x+1) - 2x - x^2$ , $x_0 = -1$	7в.12	$y = 6e^{x-1} - 3x - x^3$ , $x_0 = 1$
7в.13	$y = 2x + x^2 - (x+1)\ln(2+x)$ , $x_0 = -1$	7в.14	$y = \sin^2(x+1) - 2x - x^2$ $x_0 = -1$
7в.15	$y = x^2 + 4x + \cos^2(x+2)$ , $x_0 = -2$	7в.16	$y = x^2 + 2\ln(x+2)$ , $x_0 = -1$
7в.17	$y = 4x - x^2 + (x-2)\sin(x-2)$ , $x_0 = 2$	7в.18	$y = 6e^x - x^3 - 3x^2 - 6x - 5$ , $x_0 = 0$
7в.19	$y = x^2 - 2x - 2e^{x-2}$ , $x_0 = 2$	7в.20	$y = \sin^2(x+2) - x^2 - 4x - 4$ , $x_0 = -2$
7в.21	$y = \cos^2(x-1) + x^2 - 2x$ , $x_0 = 1$	7в.22	$y = x^2 - 2x - (x-1)\ln x$ , $x_0 = 1$
7в.23	$y = (x-1)\sin(x-1) + 2x - x^2$ , $x_0 = 1$	7в.24	$y = x^2 - 4x + \cos^2(x-2)$ , $x_0 = 2$
7в.25	$y = x^4 + 4x^3 + 12x^2 + 24(x+1 - e^x)$ , $x_0 = 0$	7в.26	$y = \sin^2(x-2) - x^2 + 4x - 4$ , $x_0 = 2$
7в.27	$y = 6e^{x+1} - x^3 - 6x^2 - 15x - 16$ , $x_0 = -1$	7в.28	$y = \sin x + sh x - 2x$ , $x_0 = 0$
7в.29	$y = \sin^2(x-1) - x^2 + 2x$ , $x_0 = 1$	7в.30	$y = \cos x + ch x$ , $x_0 = 0$

### Задание № 8а

Найдите интервалы выпуклости и вогнутости функций.

8а.1	$y = x^4 - 2x^3 + 6x - 4$	8а.2	$y = x^3 - 6x^2 + 2x - 6$
8а.3	$y = x^4 - 2x^3 - 12x^2 + 24x + 8$	8а.4	$y = 2x^4 - 3x^2 + x - 1$

8a.5	$y = x^5 - 10x^2 + 3x$	8a.6	$y = \sqrt[3]{x + 3}$
8a.7	$y = \frac{1}{1 - x^2}$	8a.8	$y = \frac{x^3}{12 + x^2}$
8a.9	$y = \frac{\sqrt{x}}{x + 1}$	8a.10	$y = \frac{x}{\sqrt[3]{x^2 - 1}}$
8a.11	$y = \sqrt[3]{4x^3 - 12x}$	8a.12	$y = x + \sin x$
8a.13	$y = e^{-x^2}$	8a.14	$y = e^{1/x}$
8a.15	$y = \frac{10}{x} \ln \frac{x}{10}$	8a.16	$y = \frac{x^2}{(x - 1)^3}$
8a.17	$y = x \sin \ln x$	8a.18	$y = x^4 - 6x^2 + 5x$
8a.19	$y = \operatorname{arctg} \frac{1}{x}$	8a.20	$y = 4x^3 + \frac{1}{x}$
8a.21	$y = x^4 - 12x^3 + 48x^2$	8a.22	$y = 2x^4 + 2x^3 + 3x^2 + 3x + 1$
8a.23	$y = (x^2 - 1)^3$	8a.24	$y = 36x(x - 1)^3$
8a.25	$y = x + 36x^2 - 2x^3 - x^4$	8a.26	$y = e^{\operatorname{arctg} x}$
8a.27	$y = 1 + x^2 - \frac{x^4}{2}$	8a.28	$y = \frac{x^5}{20} - x^4 + 8x^3 - 32x^2$
8a.29	$y = \sqrt[3]{x^2} - \sqrt[3]{x^2 - 4}$	8a.30	$y =  x - 1 /x^2$

### Задание № 9а

Найдите асимптоты и постройте графики функций.

9a.1	$y = \frac{17 - x^2}{4x - 5}$	9a.2	$y = \frac{x^2 + 1}{\sqrt{4x^2 - 3}}$
9a.3	$y = \frac{x^3 - 4x}{3x^2 - 4}$	9a.4	$y = \frac{4x^2 + 9}{4x + 8}$

9a.5	$y = \frac{4x^3 + 3x^2 - 8x - 2}{2 - 3x^2}$	9a.6	$y = \frac{x^2 - 3}{\sqrt{3x^2 - 2}}$
9a.7	$y = \frac{2x^2 - 6}{x - 2}$	9a.8	$y = \frac{2x^3 + 2x^2 - 3x - 1}{2 - 4x^2}$
9a.9	$y = \frac{x^3 - 5x}{5 - 3x^2}$	9a.10	$y = \frac{x^2 - 6x + 4}{3x - 2}$
9a.11	$y = \frac{2 - x^2}{\sqrt{9x^2 - 4}}$	9a.12	$y = \frac{4x^3 - 3x}{4x^2 - 1}$
9a.13	$y = \frac{3x^2 - 7}{2x + 1}$	9a.14	$y = \frac{x^2 + 16}{\sqrt{9x^2 - 8}}$
9a.15	$y = \frac{x^3 + 3x^2 - 2x - 2}{2 - 3x^2}$	9a.16	$y = \frac{21 - x^2}{7x + 9}$
9a.17	$y = \frac{2x^2 - 1}{\sqrt{x^2 - 2}}$	9a.18	$y = \frac{2x^3 - 3x^2 - 2x + 1}{1 - 3x^2}$
9a.19	$y = \frac{x^2 - 11}{4x - 3}$	9a.20	$y = \frac{2x^2 - 9}{\sqrt{x^2 - 1}}$
9a.21	$y = \frac{x^3 - 2x^2 - 3x + 2}{1 - x^2}$	9a.22	$y = \frac{x^2 + 2x - 1}{2x + 1}$
9a.23	$y = \frac{x^3 + x^2 - 3x - 1}{2x^2 - 2}$	9a.24	$y = \frac{x^2 + 6x + 9}{x + 4}$
9a.25	$y = \frac{3x^2 - 10}{\sqrt{4x^2 - 1}}$	9a.26	$y = \frac{x^2 - 2x + 2}{x + 3}$
9a.27	$y = \frac{2x^3 + 2x^2 - 9x - 3}{2x^2 - 3}$	9a.28	$y = \frac{3x^2 - 10}{3 - 2x}$
9a.29	$y = \frac{-x^2 - 4x + 13}{4x + 3}$	9a.30	$y = \frac{-8 - x^2}{\sqrt{x^2 - 4}}$

### Задание № 10а

Проведите полное исследование функций и постройте их графики.

10a.1	$y = (2x + 3)e^{-2(x+1)}$	10a.2	$y = (3 - x)e^{x-2}$
10a.3	$y = \frac{e^{2(x+1)}}{2(x+1)}$	10a.4	$y = 3 \ln \frac{x}{x-3} - 1$
10a.5	$y = \frac{e^{2-x}}{2-x}$	10a.6	$y = \ln \frac{x}{x+2} + 1$
10a.7	$y = (x-2)e^{3-x}$	10a.8	$y = -(2x+1)e^{2(x+1)}$
10a.9	$y = \frac{e^{2(x-1)}}{2(x-1)}$	10a.10	$y = 3 - 3 \ln \frac{x}{x+4}$
10a.11	$y = \frac{e^{2(x+2)}}{2(x+2)}$	10a.12	$y = \ln \frac{x}{x-2} - 2$
10a.13	$y = (2x+5)e^{-2(x+2)}$	10a.14	$y = (4-x)e^{x-3}$
10a.15	$y = \frac{e^{3-x}}{3-x}$	10a.16	$y = 2 \ln \frac{x}{x+1} - 1$
10a.17	$y = -\frac{e^{-2(x+2)}}{2(x+2)}$	10a.18	$y = 2 \ln \frac{x+3}{x} - 3$
10a.19	$y = (2x-1)e^{2(1-x)}$	10a.20	$y = -(x+1)e^{x+2}$
10a.21	$y = -\frac{e^{-(x+2)}}{x+2}$	10a.22	$y = 2 \ln \frac{x}{x-4} - 3$
10a.23	$y = \frac{e^{x+3}}{x+3}$	10a.24	$y = \ln \frac{x}{x+5} - 1$
10a.25	$y = -(2x+3)e^{2(x+2)}$	10a.26	$y = (x+4)e^{-(x+3)}$
10a.27	$y = -\frac{e^{-2(x-1)}}{2(x-1)}$	10a.28	$y = \ln \frac{x-5}{x} + 2$
10a.29	$y = \frac{e^{x-3}}{x-3}$	10a.30	$y = 2 \ln \frac{4x-2}{x} + 1$

# Упражнения по технике дифференцирования

## функции одного аргумента

### Задание № 11

Найдите производные данных функций

11.1	$y = 2x^5 - \frac{4}{x^3} + \frac{1}{x} + 3\sqrt{x}$	11.2	$y = \frac{3}{x} + \sqrt[5]{x^2} - 4x^3 + \frac{2}{x^4}$
11.3	$y = 3x^4 + \sqrt[3]{x^5} - \frac{2}{x} - \frac{4}{x^2}$	11.4	$y = 7\sqrt{x} - \frac{2}{x^5} - 3x^2 + \frac{4}{x}$
11.5	$y = 7x + \frac{5}{x^2} - \sqrt[7]{x^4} + \frac{6}{x}$	11.6	$y = 5x^2 - \sqrt[3]{x^4} + \frac{4}{x} - \frac{5}{x}$
11.7	$y = 3x^5 - \frac{3}{x} - \sqrt{x^3} + \frac{10}{x^5}$	11.8	$y = \sqrt[3]{x^7} + \frac{3}{x} - 4x^6 + \frac{4}{x^5}$
11.9	$y = 8x^2 + \sqrt[3]{x^4} - \frac{4}{x} - \frac{2}{x^3}$	11.10	$y = 4x^6 + \frac{5}{x} - \sqrt[3]{x^7} - \frac{7}{x^4}$
11.11	$y = 2\sqrt{x^3} - \frac{7}{x} + 3x^2 - \frac{2}{x^5}$	11.12	$y = 4x^3 - \frac{3}{x} - \sqrt[5]{x^2} + \frac{6}{x^2}$
11.13	$y = 5x^3 - \frac{8}{x^2} + 4\sqrt{x} + \frac{1}{x}$	11.14	$y = \frac{9}{x^3} + \sqrt[3]{x^4} - \frac{2}{x} + 5x^4$
11.15	$y = \frac{4}{x^5} - \frac{9}{x} + \sqrt[5]{x^2} - 7x^3$	11.16	$y = \frac{8}{x^3} + \frac{3}{x} - 4\sqrt{x^3} + 2x^7$
11.17	$y = 5x^2 + \frac{4}{x} - \sqrt[3]{x^7} - 2x^6$	11.18	$y = 10x^2 + 3\sqrt{x^5} - \frac{4}{x} - \frac{5}{x^4}$
11.19	$y = \sqrt{x^5} - \frac{3}{x} + \frac{4}{x^3} - 3x^3$	11.20	$y = 9x^4 + \frac{5}{x} - \frac{7}{x^3} + \sqrt[3]{x^7}$
11.21	$y = 3\sqrt{x} + \frac{4}{x^5} + \sqrt[3]{x^2} - \frac{7}{x}$	11.22	$y = \sqrt{x^3} + \frac{2}{x} - \frac{4}{x^5} - 5x^3$
11.23	$y = 7x^2 + \frac{3}{x} - \sqrt[5]{x^4} + \frac{8}{x^3}$	11.24	$y = 8x^3 - \frac{4}{x} - \frac{7}{x^4} + \sqrt[7]{x^2}$
11.25	$y = 8x - \frac{5}{x^4} + \frac{1}{x} - \sqrt[5]{x^4}$	11.26	$y = \sqrt[4]{x^3} - \frac{5}{x} + \frac{4}{x^5} + 3x$
11.27	$y = 4x^5 + \frac{3}{x} - \sqrt[3]{x^5} - \frac{3}{x^4}$	11.28	$y = 4x^5 - \frac{5}{x} - \sqrt{x^3} + \frac{2}{x}$
11.29	$y = \frac{7}{x} + \frac{4}{x^3} - \sqrt[5]{x^3} - 2x^6$	11.30	$y = \frac{6}{x^4} - \frac{3}{x} + 3x^3 - \sqrt{x^7}$

**Задание № 12**  
Найдите производные данных функций

12.1	$y = \sqrt[3]{3x^4 + 2x - 5} + \frac{4}{(x - 2)^5}$	12.2	$y = \sqrt[3]{(x - 3)^4} - \frac{3}{2x^3 - 3x + 1}$
12.3	$y = \sqrt{(x - 4)^5} + \frac{5}{(2x^2 + 4x - 1)^2}$	12.4	$y = \sqrt[5]{7x^2 - 3x + 5} - \frac{5}{(x - 1)^3}$
12.5	$y = \sqrt[4]{3x^2 - x + 5} - \frac{3}{(x - 5)^4}$	12.6	$y = \sqrt{3x^4 - 2x^3 + x} - \frac{4}{(x + 2)^3}$
12.7	$y = \sqrt[3]{(x - 7)^5} + \frac{5}{4x^2 + 3x - 5}$	12.8	$y = \sqrt[5]{(x + 4)^6} - \frac{2}{2x^2 - 3x + 7}$
12.9	$y = \frac{3}{(x - 4)^7} - \sqrt{5x^2 - 4x + 3}$	12.10	$y = \sqrt[3]{4x^2 - 3x - 4} - \frac{2}{(x - 3)^5}$
12.11	$y = \frac{7}{(x - 1)^3} + \sqrt{8x - 3 + x^2}$	12.12	$y = \sqrt[5]{3x^2 + 4x - 5} + \frac{4}{(x - 4)^4}$
12.13	$y = \sqrt[3]{5x^4 - 2x + 1} + \frac{8}{(x - 5)^2}$	12.14	$y = \frac{3}{(x + 2)^5} - \sqrt[7]{5x - 7x^2 - 3}$
12.15	$y = \sqrt[4]{(x - 1)^5} - \frac{4}{7x^2 - 3x + 2}$	12.16	$y = \sqrt[5]{(x - 2)^6} - \frac{3}{7x^3 - x^2 - 4}$
12.17	$y = \frac{3}{(x + 4)^2} - \sqrt[3]{4 + 3x - x^4}$	12.18	$y = \frac{2}{(x - 1)^3} - \frac{8}{6x^2 + 3x - 7}$
12.19	$y = \sqrt{1 + 5x - 2x^2} + \frac{3}{(9x - 3)^4}$	12.20	$y = \sqrt[3]{5 + 4x - x^2} - \frac{5}{(x + 1)^3}$
12.21	$y = \sqrt[4]{5x^2 - 4x + 1} - \frac{7}{(x - 5)^2}$	12.22	$y = \sqrt[5]{3 - 7x + x^2} - \frac{4}{(x - 7)^5}$
12.23	$y = \sqrt{(x - 3)^7} + \frac{9}{7x^2 - 5x - 8}$	12.24	$y = \sqrt[3]{(x - 8)^4} - \frac{2}{1 + 3x - 4x^2}$
12.25	$y = \frac{3}{4x - 3x^2 + 1} - \sqrt{(x - 1)^5}$	12.26	$y = \frac{3}{x - 4} + \sqrt[6]{(2x^2 - 3x + 1)^5}$
12.27	$y = \frac{4}{(x - 7)^3} - \sqrt[3]{(3x^2 - x + 1)^4}$	12.28	$y = \sqrt{(x - 4)^7} - \frac{10}{(3x^2 - 5x + 1)^4}$
12.29	$y = \frac{7}{(x + 2)^5} - \sqrt{8 - 5x + 2x^2}$	12.30	$y = \sqrt[3]{(x - 1)^5} + \frac{5}{2x^2 - 4x + 7}$

**Задание № 13**  
Найдите производные данных функций

13.1	$y = \sin^3 2x \operatorname{cos} 8x^5$	13.2	$y = \cos^5 3x \operatorname{tg}(4x + 1)^3$
13.3	$y = \operatorname{tg}^4 x \operatorname{arcsin} 4x^5$	11.4	$y = \operatorname{ctg} 3x \operatorname{arccos} 3x^2$
13.5	$y = \operatorname{arcsin}^3 2x \operatorname{tg} 7x^4$	13.6	$y = \operatorname{arccos}^2 4x \operatorname{ln}(x - 3)$
13.7	$y = \ln^5 x \operatorname{arctg} 7x^4$	13.8	$y = \operatorname{arctg}^3 4x \operatorname{B}^{\sin x}$
13.9	$y = 2^{\cos x} \operatorname{arcctg} 5x^3$	13.10	$y = 4^{-x} \operatorname{ln}^5(x - 2)$
13.11	$y = 3^{\operatorname{tg} x} \operatorname{arcsin} 7x^4$	13.12	$y = 5^{x^2} \operatorname{arccos} 2x^5$
13.13	$y = \sin^4 3x \operatorname{arctg} 2x^3$	13.14	$y = \cos^3 4x \operatorname{arcctg} \sqrt{x}$
13.15	$y = \operatorname{tg}^3 2x \operatorname{arccos} 2x^3$	13.16	$y = \operatorname{ctg}^7 x \operatorname{arcsin} x^5$
13.17	$y = e^{-\sin x} \operatorname{tg} 7x^6$	13.18	$y = e^{\cos x} \operatorname{ctg} 8x^3$
13.19	$y = \cos^5 x \operatorname{arccos} 4x$	13.20	$y = \sin^3 7x \operatorname{arcctg} 5x^2$
13.21	$y = \sin^2 3x \operatorname{arcctg} 3x^5$	13.22	$y = \cos \sqrt[5]{x} \operatorname{arctgx}^4$
13.23	$y = \operatorname{tg}^6 2x \operatorname{cos} 7x^2$	13.24	$y = \operatorname{ctg}^3 4x \operatorname{arcsin} \sqrt{x}$
13.25	$y = \operatorname{ctg} \frac{1}{x} \operatorname{arccos} x^4$	13.26	$y = \operatorname{tg} \frac{1}{\sqrt{x}} \operatorname{arcctg} 3x^5$
13.27	$y = \operatorname{tg}^3 2x \operatorname{arccos} 2x^3$	13.28	$y = 2^{\operatorname{tg} x} \operatorname{arctg}^5 3x$
13.29	$y = \sin^5 3x \operatorname{arctg} \sqrt{x}$	13.30	$y = \cos^4 3x \operatorname{arcsin} 3x^2$

**Задание № 14**  
Найдите производные данных функций

14.1	$y = \operatorname{arcctg}^2 5x \operatorname{ln}(x - 4)$	14.2	$y = \operatorname{arctg}^3 2x \operatorname{ln}(x + 5)$
14.3	$y = \operatorname{arccos}^4 x \operatorname{ln}(x^2 + x - 1)$	14.4	$y = \sqrt{\operatorname{arccos} 2x} \operatorname{B}^{-x}$
14.5	$y = \operatorname{tg}^4 3x \operatorname{arcctg} 7x^2$	14.6	$y = 5^{-x^2} \operatorname{arcsin} 3x^3$
14.7	$y = \operatorname{arctg}^5 x \operatorname{log}_2(x - 2)$	14.8	$y = \log_3(x + 5) \operatorname{arccos} 3x$
14.9	$y = e^{-x} \operatorname{arcsin}^2 5x$	14.10	$y = \log_4(x - 1) \operatorname{arcsin}^4 x$
14.11	$y = (x - 4)^5 \operatorname{arcctg} 3x^2$	14.12	$y = \operatorname{ctg}^3 4x \operatorname{arctg} 2x^3$

14.13	$y = e^{-\cos x} \operatorname{arctg} 7x^5$	14.14	$y = (x+1)^4 \operatorname{arccos} 4x^6$
14.15	$y = 2^{\sin x} \operatorname{arcctg} 5x^4$	14.16	$y = 3^{-x^3} \operatorname{arctg} 2x^5$
14.17	$y = 3^{\cos x} \operatorname{arcsin}^2 3x$	14.18	$y = \ln(x-10) \operatorname{arccos}^2 4x$
14.19	$y = \lg(x-2) \operatorname{arcsin}^5 3x$	14.20	$y = \log_3(5x-2) \operatorname{arctg}^5 7x$
14.21	$y = \ln(x+5) \operatorname{arcctg}^3 2x$	14.22	$y = \lg(7x+9) \operatorname{arccos}^2 4x$
14.23	$y = 4^{-\sin x} \operatorname{arctg} 3x$	14.24	$y = 2^{\cos x} \operatorname{arcctg}^2 4x$
14.25	$y = \log_5(2x-5) \operatorname{arcsin}^2 5x$	14.26	$y = \log_3(2x-9) \operatorname{arccos}^2 x$
14.27	$y = 2^{-x} \operatorname{arctg}^3 4x$	14.28	$y = \ln(x-4) \operatorname{arcctg}^4 3x$
14.29	$y = \lg(3x+4) \operatorname{arcctg}^3 2x$	14.30	$y = \log_5(3x+1) \operatorname{arctg}^5 x^3$

### Задание № 15

Найдите производные данных функций

15.1	$y = \operatorname{tg}^4 3x \operatorname{arcsin} 2x^3$	15.2	$y = (x-2)^4 \operatorname{arcsin} 5x^4$
15.3	$y = 2^{-x^3} \operatorname{arctg} 7x^4$	15.4	$y = (x+6)^5 \operatorname{arcctg} 3x^5$
15.5	$y = 3^{\cos x} \ln(x^2 - 3x + 7)$	15.6	$y = \log_2(x-7) \operatorname{arctg} \sqrt{x}$
15.7	$y = \operatorname{arccos}^5 3x \operatorname{tg} x^4$	15.8	$y = (x-5)^7 \operatorname{arcctg} 7x^3$
15.9	$y = \operatorname{arccos} x^2 \operatorname{ctg} 7x^3$	15.10	$y = 5^{-x^2} \operatorname{arccos} 5x^4$
15.11	$y = \operatorname{arcctg}^4 x \operatorname{cos} 7x^4$	15.12	$y = 4(x-6)^7 \operatorname{arcsin} 3x^5$
15.13	$y = (x+5)^2 \operatorname{arccos}^3 5x$	15.14	$y = (x+2)^7 \operatorname{arccos} \sqrt{x}$
15.15	$y = 2^{-\sin x} \operatorname{arcsin}^3 2x$	15.16	$y = (x-7)^5 \operatorname{arcsin} 7x^4$
15.17	$y = \ln(x-3) \operatorname{arccos} 3x^4$	15.18	$y = \log_2(x-4) \operatorname{arctg}^3 4x$
15.19	$y = (x-7)^4 \operatorname{arcctg}^2 7x$	15.20	$y = \sqrt[3]{x-5} \operatorname{arccos}^4 2x$
15.21	$y = \sqrt[4]{2x-5} \operatorname{arcsin}^4 5x$	15.22	$y = (3x-4)^5 \operatorname{arccos} 3x^6$
15.23	$y = \sqrt{(5x-3)^5} \operatorname{arcsin} 2x^3$	15.24	$y = \sqrt[2]{(x+1)^2} \operatorname{arccos} 3x$
15.25	$y = \operatorname{tg}^3 5x \operatorname{arcctg} 3x$	15.26	$y = \sqrt{(3x-2)^3} \operatorname{arctg} (7x-1)$
15.27	$y = \sqrt[5]{(3x-4)^3} \operatorname{arcsin} 7x^2$	15.28	$y = \operatorname{arcsin}^3 4x \operatorname{tg} 3x$
15.29	$y = e^{-\cos x} \operatorname{arcsin} 5x$	15.30	$y = 5\sqrt{(3x+5)^3} \operatorname{arccos}^4 x$

**Задание № 16**  
Найдите производные данных функций

16.1	$y = (x - 3)^4 \arccos 5x^3$	16.2	$y = (3x - 4)^3 \arccos 3x^2$
16.3	$y = sh^3 4x \operatorname{arcos} \sqrt{x}$	16.4	$y = th^2 \sqrt{x} \operatorname{arcctg} 3x^2$
16.5	$y = cth^3 5x \operatorname{arcsin} 3x^2$	16.6	$y = ch \frac{1}{x} \operatorname{arctg} (7x + 2)$
16.7	$y = ch^3 4x \operatorname{arcos} 4x^2$	16.8	$y = sh^3 3x \operatorname{arcctg} 5x^2$
16.9	$y = th^5 3x \operatorname{arcsin} \sqrt{x}$	16.10	$y = cth^2(x + 1) \operatorname{arcos} \frac{1}{x}$
16.11	$y = sh^4 2x \operatorname{arcos} x^2$	16.12	$y = ch^3(3x + 2) \operatorname{arctg} 3x$
16.13	$y = th^3 4x \operatorname{arcctg} 3x^4$	16.14	$y = cth^4 7x \operatorname{arcsin} \sqrt{x}$
16.15	$y = sh^3 2x \operatorname{arcsin} 7x^2$	16.16	$y = th^5 4x \operatorname{arcos} 3x^4$
16.17	$y = ch^2 5x \operatorname{arctg} \sqrt{x}$	16.18	$y = cth^4 2x \operatorname{arctgx}^3$
16.19	$y = sh^4 5x \operatorname{arcos} 3x^2$	16.20	$y = ch^3 9x \operatorname{arctg} (5x - 4)$
16.21	$y = th^4 3x \operatorname{arcctg} \frac{1}{x}$	16.22	$y = cth^3 4x \operatorname{arcsin}(3x - 1)$
16.23	$y = ch^5 2x \operatorname{arctgx}^4$	16.24	$y = th^4 7x \operatorname{arcos} x^3$
16.25	$y = cth 4x^5 \operatorname{arcos} 2x$	16.26	$y = cth 3x \operatorname{arcsin}^4 2x$
16.27	$y = th^5 3x \operatorname{arcctg} \sqrt{x}$	16.28	$y = sh^4 3x \operatorname{arcos} 5x^4$
16.29	$y = cth^2 4x \operatorname{arcsin} x^3$	16.30	$y = th^3 5x \operatorname{arcctg} (2x - 5)$

**Задание № 17**  
Найдите производные данных функций

17.1	$y = \frac{e^{\arccos^3 x}}{\sqrt{x+5}}$	17.2	$y = \frac{(x - 4)^2}{e^{\operatorname{arcctgx}}}$
17.3	$y = \frac{e^{-x^2}}{\sqrt{x^2 + 5x - 1}}$	17.4	$y = \frac{e^{-\operatorname{ctg} 5x}}{3x^2 - 4x + 2}$

17.5	$y = \frac{\sqrt{7x^3 - 5x + 2}}{e^{\cos x}}$	17.6	$y = \frac{e^{tg 3x}}{\sqrt{3x^2 - x + 4}}$
17.7	$y = \frac{e^{\sin x}}{(3x - 5)^7}$	17.8	$y = \frac{\sqrt[3]{2x^2 - 3x + 1}}{e^{-x}}$
17.9	$y = \frac{\sqrt{x^3 + 4x - 5}}{e^{x^3}}$	17.10	$y = \frac{e^{ctg 5x}}{(2x + 4)^3}$
17.11	$y = \frac{\sqrt{3 + 2x - x^2}}{e^x}$	17.12	$y = \frac{e^{3x}}{\sqrt{3x^2 - 4x - 7}}$
17.13	$y = \frac{e^{-\sin 2x}}{(3x + 5)^4}$	17.14	$y = \frac{e^{\cos 5x}}{\sqrt{x^2 - 5x - 2}}$
17.15	$y = \frac{(2x + 5)^3}{e^{ctgx}}$	17.16	$y = \frac{e^{-tg 3x}}{4x^2 - 3x + 5}$
17.17	$y = \frac{e^{-\sin 4x}}{(3x - 5)^6}$	17.18	$y = \frac{3x^2 - 5x + 10}{e^{-x^4}}$
17.19	$y = \frac{e^{-x}}{(2x^2 - x + 4)^2}$	17.20	$y = \frac{e^{4x}}{(3x + 5)^3}$
17.21	$y = \frac{e^{ctg 5x}}{(3x - 5)^4}$	17.22	$y = \frac{(2x - 3)^7}{e^{-2x}}$
17.23	$y = \frac{(3x + 1)^4}{e^{4x}}$	17.24	$y = \frac{5x^2 + 4x - 2}{e^{-x}}$
17.25	$y = \frac{\sqrt{5x^2 - x + 1}}{e^{3x}}$	17.26	$y = \frac{e^{-x^2}}{(2x - 5)^7}$
17.27	$y = \frac{e^{\cos 3x}}{(2x + 4)^5}$	17.28	$y = \frac{e^{\sin 5x}}{(3x - 2)^2}$
17.29	$y = \frac{\sqrt{x^2 - 3x - 7}}{e^{-x^3}}$	17.30	$y = \frac{e^{-tg x}}{4x^2 + 7x - 5}$

**Задание № 18**  
Найдите производные данных функций

18.1	$y = \frac{\log_5(3x - 7)}{ctg 7x^3}$	18.2	$y = \frac{\ln(5x - 3)}{4tg 3x^4}$
18.3	$y = \frac{\ln(7x + 2)}{5\cos^3 4x}$	18.4	$y = \frac{\sin^3 5x}{\ln(2x - 3)}$
18.5	$y = \frac{\cos^2 3x}{\lg(3x - 4)}$	18.6	$y = \frac{tg^3 2x}{\lg(5x + 1)}$
18.7	$y = \frac{\log_3(4x + 5)}{2ctg \sqrt{x}}$	18.8	$y = \frac{\ln(7x - 3)}{3tg^2 4x}$
18.9	$y = \frac{\lg(11x + 3)}{\cos^2 5x}$	18.10	$y = \frac{ctg^2 5x}{\ln(7x - 2)}$
18.11	$y = \frac{tg^2(x - 2)}{\lg(x + 3)}$	18.12	$y = \frac{\sin^3(5x + 1)}{\lg(3x - 2)}$
18.13	$y = \frac{\cos^3(7x - 1)}{\lg(x + 5)}$	18.14	$y = \frac{\sin^3(4x + 3)}{\ln(7x + 1)}$
18.15	$y = \frac{ctg^3(2x - 3)}{\log_3(x + 2)}$	18.16	$y = \frac{\lg^3 x}{\sin 5x^2}$
18.17	$y = \frac{\ln^2(x + 1)}{\cos 3x^4}$	18.18	$y = \frac{\log_2(7x - 5)}{tg \sqrt{x}}$
18.19	$y = \frac{\log_3(4x - 2)}{ctg^3 2x}$	18.20	$y = \frac{\ln^3(x - 5)}{tg(1/x)}$
18.21	$y = \frac{\lg(x + 2)}{\sin 2x^5}$	18.22	$y = \frac{tg^3 7x}{\ln(3x + 2)}$
18.23	$y = \frac{ctg \sqrt{2x - 3}}{\lg(3x + 4)}$	18.24	$y = \frac{tg(3x - 5)}{\ln^2(x + 3)}$
18.25	$y = \frac{\cos^2 x}{\lg(x^2 - 2x + 1)}$	18.26	$y = \frac{\log_2(3x - 7)}{tg 3x}$
18.27	$y = \frac{\ln^3(x - 3)}{ctg(x - 3)}$	18.28	$y = \frac{tg^4 5x}{\ln(x + 7)}$
18.29	$y = \frac{\log_3(2x - 1)}{\cos^5 x}$	18.30	$y = \frac{tg^4 3x}{\lg(x^2 - x + 4)}$

### Задание № 19

Найдите производные данных функций

19.1	$y = \frac{\operatorname{arcctg}^4 5x}{\operatorname{sh} \sqrt{x}}$	19.2	$y = \frac{\operatorname{arctg}^3 2x}{\operatorname{ch}(1/x)}$
19.3	$y = \frac{\operatorname{arccos} 3x^4}{\operatorname{th}^2 x}$	19.4	$y = \frac{\operatorname{arcsin} 5x^3}{\operatorname{ch} \sqrt{x}}$
19.5	$y = \frac{\operatorname{cth}^3(x+1)}{\operatorname{arccos} 2x}$	19.6	$y = \frac{\operatorname{th} 3x^5}{\operatorname{arctg}^2 3x}$
19.7	$y = \frac{\operatorname{arccos}^7 2x}{\operatorname{th} x^5}$	19.8	$y = \frac{\operatorname{arcsin}^3 5x}{\operatorname{sh}(3x+1)}$
19.9	$y = \frac{\operatorname{th}^4(2x+5)}{\operatorname{arccos} 3x}$	19.10	$y = \frac{\sqrt[3]{\operatorname{arctg} 2x}}{\operatorname{sh}^2 x}$
19.11	$y = \frac{\operatorname{arcsin}^2 4x}{\operatorname{th}(5x-3)}$	19.12	$y = \frac{\operatorname{ch}^2(4x+2)}{\operatorname{arctg} x^3}$
19.13	$y = \frac{\operatorname{arcsin} 4x^5}{\operatorname{th}^3 x}$	19.14	$y = \frac{\operatorname{arctg}^3(2x+1)}{\operatorname{ch} \sqrt{x}}$
19.15	$y = \frac{\operatorname{arccos} 4x^3}{\operatorname{sh}^4 x}$	19.16	$y = \frac{\operatorname{cth}^2(x-2)}{\operatorname{arccos} 3x}$
19.17	$y = \frac{\operatorname{th}^2(2x+2)}{\operatorname{arcsin} 5x}$	19.18	$y = \frac{\operatorname{cth}^2(3x-1)}{\operatorname{arccos} x^2}$
19.19	$y = \frac{\operatorname{sh}^5 x}{\operatorname{arccos} 4x}$	19.20	$y = \frac{\sqrt{\operatorname{ch}^3 x}}{\operatorname{arctg} 5x}$
19.21	$y = \frac{\operatorname{th}^2(x+3)}{\operatorname{arcctg} \sqrt{x}}$	19.22	$y = \frac{\operatorname{arcsin}^3 3x}{\operatorname{ch}(x-5)}$
19.23	$y = \frac{\operatorname{arcctg}^3 x}{\operatorname{sh}(2x-5)}$	19.24	$y = \frac{\operatorname{arccos}^3 5x}{\operatorname{th}(x-2)}$
19.25	$y = \frac{\sqrt{\operatorname{arccos} 3x}}{\operatorname{sh}^2 x}$	19.26	$y = \frac{\operatorname{arcsin}^2 3x}{\sqrt{\operatorname{th} x}}$
19.27	$y = \frac{\operatorname{arctg}^2 5x}{\sqrt[3]{\operatorname{cth} x}}$	19.28	$y = \frac{\operatorname{arctg}^2 5x}{\operatorname{th}(x+3)}$
19.29	$y = \frac{\sqrt{\operatorname{sh}^3 x}}{\operatorname{arcctg} 5x}$	19.30	$y = \frac{\sqrt[5]{\operatorname{ch} 3x}}{\operatorname{arctg}(x+2)}$

**Задание № 20**  
Найдите производные данных функций

20.1	$y = \frac{9 \operatorname{arctg}(x+7)}{(x-1)^2}$	20.2	$y = \frac{8 \operatorname{arctg}(2x+3)}{(x+1)^3}$
20.3	$y = \frac{7 \operatorname{arccos}(4x-1)}{(x+2)^4}$	20.4	$y = \frac{6 \operatorname{arcsin}(x+5)}{(x-2)^5}$
20.5	$y = \frac{3 \operatorname{arcctg}(2x-5)}{(x+1)^4}$	20.6	$y = \frac{2 \operatorname{arctg}(3x+2)}{(x-3)^2}$
20.7	$y = \frac{4 \operatorname{arccos} 3x}{(x+2)^5}$	20.8	$y = \frac{\operatorname{arcsin}(3x+8)}{(x-7)^3}$
20.9	$y = \frac{7 \operatorname{arctg}(4x+1)}{(x-4)^4}$	20.10	$y = \frac{3 \operatorname{arcsin}(2x-7)}{(x+2)^4}$
20.11	$y = \frac{2 \lg(4x+5)}{(x+6)^4}$	20.12	$y = \frac{5 \ln(5x+7)}{(x-7)^2}$
20.13	$y = \frac{4 \log_3(3x+1)}{(x+1)^2}$	20.14	$y = \frac{7 \log_4(2x-5)}{(x-1)^5}$
20.15	$y = \frac{\ln(7x+2)}{(x-6)^4}$	20.16	$y = \frac{4 \lg(3x+7)}{(x+1)^7}$
20.17	$y = \frac{5 \log_2(x^2+1)}{(x-3)^4}$	20.18	$y = \frac{6 \log_3(2x+9)}{(x+4)^2}$
20.19	$y = \frac{3 \log_2(5x-4)}{(x-3)^5}$	20.20	$y = \frac{7 \log_5(x^2+x)}{(x+3)^3}$
20.21	$y = \frac{\log_7(2x^2+5)}{(x-4)^2}$	20.22	$y = \frac{2 \ln(3x-10)}{(x+5)^7}$
20.23	$y = \frac{2 \log_3(4x-7)}{(x+3)^4}$	20.24	$y = \frac{8 \lg(4x+5)}{(x-1)^5}$
20.25	$y = \frac{3 \log_4(2x+9)}{(x-7)^2}$	20.26	$y = \frac{\lg(x^2-2x)}{(x+8)^4}$
20.27	$y = \frac{3 \ln(x^2+5)}{(x-7)^3}$	20.28	$y = \frac{4 \log_2(3x-5)}{(x-2)^2}$
20.29	$y = \frac{2 \ln(2x^2-3)}{(x-5)^5}$	20.30	$y = \frac{4 \lg(3x+7)}{(x-7)^3}$

**Задание № 21**  
Найдите производные данных функций

21.1	$y = \sqrt{\frac{2x+1}{2x-1}} \log_2(x - 3x^2)$	21.2	$y = \sqrt[3]{\frac{2x-5}{2x+3}} \lg(4x+7)$
21.3	$y = \sqrt[4]{\frac{x+3}{x-3}} \ln(5x^2 - 2x + 1)$	21.4	$y = \sqrt[5]{\frac{x+1}{x-1}} \log_3(x^2 + 2 + 4)$
21.5	$y = \sqrt[6]{\frac{7x-4}{7x+4}} \log_5(3x^2 + 2x)$	21.6	$y = \sqrt[7]{\frac{2x-3}{2x+1}} \lg(7x - 10)$
21.7	$y = \sqrt[8]{\frac{5x+1}{5x-1}} \ln(3x - x^2)$	21.8	$y = \sqrt[9]{\frac{x+3}{x-3}} \log_5(2x - 3)$
21.9	$y = \sqrt{\frac{6x+5}{6x-5}} \lg(4x+7)$	21.10	$y = \sqrt[3]{\frac{4x-1}{4x+1}} \ln(2x^3 - 3)$
21.11	$y = \sqrt[4]{\frac{x+6}{x-6}} \sin(3x^2 + 1)$	21.12	$y = \sqrt[5]{\frac{x-7}{x+7}} \cos(2x^3 + x)$
21.13	$y = \sqrt[6]{\frac{x-9}{x+9}} \operatorname{tg}(3x^2 - 4x + 1)$	21.14	$y = \sqrt[7]{\frac{x-4}{x+4}} \operatorname{ctg}(2x + 5)$
21.15	$y = \sqrt[8]{\frac{x-2}{x+2}} \sin(4x^2 - 7x + 2)$	21.16	$y = \sqrt[9]{\frac{x+3}{x-3}} \cos(x^2 - 3x + 2)$
21.17	$y = \sqrt{\frac{3x-2}{3x+2}} \operatorname{tg}(2x^2 - 9)$	21.18	$y = \sqrt{\frac{2x+3}{2x-3}} \operatorname{ctg}(3x^2 + 5)$
21.19	$y = \sqrt[4]{\frac{x+5}{x-5}} \sin(3x^2 - x + 4)$	21.20	$y = \sqrt[5]{\frac{x-6}{x+6}} \cos(7x + 2)$
21.21	$y = \sqrt[6]{\frac{x-7}{x+7}} \arcsin(2x + 3)$	21.22	$y = \sqrt[7]{\frac{x-8}{x+8}} \arccos(3x - 5)$
21.23	$y = \sqrt[8]{\frac{x-4}{x+4}} \operatorname{arctg}(5x + 1)$	21.24	$y = \sqrt[9]{\frac{x-1}{x+1}} \operatorname{arcctg}(7x + 2)$
21.25	$y = \sqrt{\frac{7x-4}{7x+4}} \arcsin(x^2 + 1)$	21.26	$y = \sqrt[3]{\frac{8x-3}{8x+3}} \arccos(x^2 - 5)$
21.27	$y = \sqrt[4]{\frac{2x-5}{2x+5}} \operatorname{arctg}(3x + 2)$	21.28	$y = \sqrt[5]{\frac{3x-4}{3x+4}} \operatorname{arcctg}(2x + 5)$
21.29	$y = \sqrt[6]{\frac{x^2-1}{x^2+1}} \arcsin 2x$	21.30	$y = \sqrt[7]{\frac{x^2+3}{x^2-3}} \arccos 4x$

**Задание № 22**  
Найдите производные данных функций

22.1	$y = (\arccos(x+2))^{tg^3x}$	22.2	$y = (\arcsin 2x)^{ctg(x+1)}$
22.3	$y = (arctg(x+7))^{\cos 2x}$	22.4	$y = (arcctg(x-3))^{\sin 4x}$
22.5	$y = (ctg(3x-2))^{\arcsin 3x}$	22.6	$y = (tg(4x-3))^{\arcsin 3x}$
22.7	$y = (\cos(2x-5))^{arcctg 5x}$	22.8	$y = (\sin(7x+4))^{arcctgx}$
22.9	$y = (\arcsin 2x)^{\ln(x+3)}$	22.10	$y = (\arccos 3x)^{\lg(5x-1)}$
22.11	$y = (arctg 5x)^{\log_2(x+4)}$	22.12	$y = (arctg 7x)^{\lg(x+1)}$
22.13	$y = (\log_4(2x+3))^{\arcsin x}$	22.14	$y = (\log_5(3x+2))^{\arccos x}$
22.15	$y = (\ln(5x-4))^{arcctgx}$	22.16	$y = (\log_2(6x+5))^{\arcsin 2x}$
22.17	$y = (\lg(7x-5))^{arctg 2x}$	22.18	$y = (\lg(4x-3))^{arccos 4x}$
22.19	$y = (\ln(7x-3))^{arctg 5x}$	22.20	$y = (\log_5(2x+5))^{arctgx}$
22.21	$y = (\sin(8x-7))^{cth(x+3)}$	22.22	$y = (\cos(3x+8))^{th(x-7)}$
22.23	$y = (tg(9x+2))^{ch(2x-1)}$	22.24	$y = (ctg(7x+5))^{sh 3x}$
22.25	$y = (sh(3x-7))^{\cos(x+4)}$	22.26	$y = (ch(2x-3))^{tg(x+5)}$
22.27	$y = (th(7x-5))^{\sin(x+2)}$	22.28	$y = (ch(3x+2))^{\cos(x+4)}$
22.29	$y = (\ln(7x+4))^{tg x}$	22.30	$y = (\lg(8x+3))^{tg 5x}$

**Задание № 23**  
Найдите производные данных функций

23.1	$y = \frac{\sqrt{x+7}(x-3)^4}{(x+2)^5}$	23.2	$y = \frac{(x-3)^5(x+2)^3}{\sqrt{(x-1)^3}}$
23.3	$y = \frac{(x-2)^3 \sqrt{(x+1)^5}}{(x-4)^2}$	23.4	$y = \frac{(x+1)^3 \sqrt[5]{(x-2)^2}}{(x+1)^7}$

23.5	$y = \frac{(x+2)^7(x-3)^3}{\sqrt[3]{(x-4)^2}}$	23.6	$y = \frac{(x-1)^4(x+2)^5}{\sqrt[3]{(x-4)^2}}$
23.7	$y = \frac{(x-7)^{10}\sqrt{3x-1}}{(x+3)^5}$	23.8	$y = \frac{(x-3)^2\sqrt{x+4}}{(x+2)^7}$
23.9	$y = \frac{(x+1)^8(x-3)^2}{\sqrt{(x+2)^5}}$	23.10	$y = \frac{(x+2)(x-7)^4}{\sqrt[3]{(x-1)^4}}$
23.11	$y = \frac{\sqrt[5]{(x+4)^3}}{(x-1)^2(x+3)^5}$	23.12	$y = \frac{\sqrt[3]{(x-1)^7}}{(x+1)^5(x-7)^3}$
23.13	$y = \frac{\sqrt{(x+2)^3}(x-1)^4}{(x+2)^7}$	23.14	$y = \frac{\sqrt[3]{(x-2)^5}(x+3)^2}{(x-7)^3}$
23.15	$y = \frac{\sqrt[4]{x-8}(x+2)^6}{(x-1)^5}$	23.16	$y = \frac{\sqrt[5]{x+1}(x-3)^7}{(x+8)^3}$
23.17	$y = \frac{\sqrt[7]{(x-2)^4}}{(x+1)^2(x-6)^5}$	23.18	$y = \frac{\sqrt[5]{(x+1)^2}}{(x-3)^4(x-5)^3}$
23.19	$y = \frac{\sqrt{x^2+2x-3}}{(x+3)^7(x-4)^2}$	23.20	$y = \frac{\sqrt[3]{(x-2)^4}}{(x-5)^3(x+1)^7}$
23.21	$y = \frac{(x+4)^3(x-2)^4}{\sqrt[3]{(x-2)^5}}$	23.22	$y = \frac{(x-1)^6(x+2)^3}{\sqrt[5]{(x+3)^2}}$
23.23	$y = \frac{(x-1)^4(x-7)^2}{\sqrt{(x+2)^5}}$	23.24	$y = \frac{(x+7)^2(x-3)^5}{\sqrt{x^2+3x-1}}$
23.25	$y = \frac{\sqrt[3]{x-3}(x+7)^5}{(x-4)^4}$	23.26	$y = \frac{\sqrt{x+10}(x-8)^3}{(x-1)^5}$
23.27	$y = \frac{\sqrt[5]{(x-2)^3}(x-1)}{(x+3)^4}$	23.28	$y = \frac{\sqrt[4]{(x+1)^3}(x-2)^5}{(x-3)^2}$
23.29	$y = \frac{\sqrt[6]{(x-1)^5}}{(x+2)^4(x-5)^7}$	23.30	$y = \frac{\sqrt[5]{(x+2)^3}}{(x-1)^4(x-3)^5}$

**Задание № 24**  
Найдите производные данных функций

24.1	$y = \sqrt{x} \ln(\sqrt{x} + \sqrt{x+a}) - x$	24.2	$y = \ln(x + \sqrt{x^2 + a^2})$
24.3	$y = 2\sqrt{x} - 4 \ln(2 + \sqrt{x})$	24.4	$y = \ln(\sqrt{x} + \sqrt{x+1})$
24.5	$y = \ln \frac{a^2 + x^2}{a^2 - x^2}$	24.6	$y = \ln \frac{x^2}{\sqrt{1 - ax^4}}$
24.7	$y = \ln^2(x + \cos x)$	24.8	$y = \ln^3(1 + \cos x)$
24.9	$y = \ln \frac{x^2}{1 - x^2}$	24.10	$y = \ln \operatorname{tg} \frac{\frac{\pi}{3}}{4} + \frac{x}{2}$
24.11	$y = \ln \sqrt[4]{\frac{1+2x}{1-2x}}$	24.12	$y = x + \frac{1}{\sqrt{2}} \ln \frac{\frac{\pi}{3}x - \sqrt{2}}{\frac{\pi}{3}x + \sqrt{2}} + a^{p^{\sqrt{2}}}$
24.13	$y = \ln \sin \frac{2x+4}{x+1}$	24.14	$y = \ln \cos \frac{2x+3}{2x+1}$
24.15	$y = \log_4 \log_2 \operatorname{tg} x$	24.16	$y = x(\cos x \ln x + \sin \ln x)/2$
24.17	$y = \log_{16} \log_5 \operatorname{tg} x$	24.18	$y = \lg \ln \operatorname{ctg} x$
24.19	$y = \log_a \frac{1}{\sqrt{1-x^4}}$	24.20	$y = \frac{1}{\sqrt{2}} \ln(\sqrt{2} \operatorname{tg} x + \sqrt{1 + \operatorname{tg}^2 x})$
24.21	$y = \ln \arcsin \sqrt{1 - e^{2x}}$	24.22	$y = \ln \arccos \sqrt{1 - e^{4x}}$
24.23	$y = \ln(bx + \sqrt{a^2 + b^2 x^2})$	24.24	$y = \ln(e^x + \sqrt{1 + e^{2x}})$
24.25	$y = \ln \operatorname{arccos} \frac{1}{\sqrt{x}}$	24.26	$y = \ln \frac{\sqrt{x^2 + 1} + x\sqrt{2}}{\sqrt{x^2 + 1} - x\sqrt{2}}$
24.27	$y = \ln \frac{\sqrt{5} + \operatorname{tg}(x/2)}{\sqrt{5} - \operatorname{tg}(x/2)}$	24.28	$y = \ln \frac{\ln x}{\sin(1/x)}$
24.29	$y = \ln \ln \sin(1 + 1/x)$	24.30	$y = \ln \ln^3 \ln^2 x$

**Задание № 25**  
Найдите производные данных функций

25.1	$y = \frac{2\sqrt{1-x}\arcsin\sqrt{x}}{x} + \frac{2}{\sqrt{x}}$	25.2	$y = \arctg \frac{\operatorname{tg}x - \operatorname{ctg}x}{\sqrt{2}} + \sqrt{6x^3}$
25.3	$y = \arcsin \frac{\sqrt{x}-2}{\sqrt{5x}} - \frac{4\sqrt{x^3}}{\sqrt{5x}}$	25.4	$y = \frac{2x-1}{4}\sqrt{2+x-x^2}$
25.5	$y = \arctg \frac{\sqrt{1+x^2}-1}{x}$	25.6	$y = \arccos \frac{x^2-4}{\sqrt{x^4+16}}$
25.7	$y = \sqrt{\frac{2}{3}}\arctg \frac{3x-1}{\sqrt{6x}}$	25.8	$y = \frac{1}{4}\ln \frac{x-1}{x+1} - \frac{1}{2}\arctgx$
25.9	$y = \frac{x-4}{\sqrt{8x-x^2+7}} - \operatorname{ctg} \frac{x-1}{2}$	25.10	$y = \frac{\operatorname{arcctg}\sqrt{x}}{x^2} + \frac{1}{3x\sqrt{x}}$
25.11	$y = \frac{x^3}{3}\arccos x + \frac{2+x^2}{\sqrt{1-x^2}}$	25.12	$y = \frac{x}{2\sqrt{x+1}} + \frac{1+x}{2x}\arctg\sqrt{x}$
25.13	$y = \frac{3+x}{\sqrt{x(x+2)}} + 3\arccos\sqrt{\frac{x}{2}}$	25.14	$y = \frac{4+x^4}{x^3}\arctg \frac{x^2}{2} + \frac{4}{x}$
25.15	$y = \arcsin \sqrt{\frac{x}{x+1}} + \arctg\sqrt{x}$	25.16	$y = \frac{1}{2}\sqrt{\frac{1}{x^2}-1} - \frac{\arccos x}{2x^2}$
25.17	$y = 6\arcsin \frac{\sqrt{x}}{2} - \frac{6+x}{2\sqrt{x}}$	25.18	$y = \frac{x-3}{\sqrt{6x-x^2}} + \arcsin \sqrt{\frac{x}{2}-1}$
25.19	$y = \frac{(1+x)\arctg\sqrt{x}-\sqrt{x}}{x}$	25.20	$y = \frac{2x-5}{\sqrt{5x-x^2}} + \arcsin \sqrt{\frac{x-1}{3}}$
25.21	$y = \arctg \frac{x}{3} + \frac{5}{6}\ln \frac{x^2+1}{x^2+4}$	25.22	$y = \arcsin \frac{3x-5}{(x-1)\sqrt{5}}$
25.23	$y = \sqrt{1-x^2} - \frac{x}{3}\arcsin\sqrt{1-x^2}$	25.24	$y = \operatorname{arcctg} \frac{\sqrt{x}}{3} - \frac{8}{3}\arctg \frac{2}{\sqrt{x}}$
25.25	$y = \arctg \frac{\sqrt{1-x}}{1-\sqrt{x}} + \operatorname{ctg} \frac{x}{3}$	25.26	$y = (2x^2+5x)\arctg \frac{x+1}{x+2} - x$

5.27	$y = \frac{x \arcsin 2x}{2\sqrt{1-4x^2}} + \frac{1}{8} \ln(1-4x^2)$	5.28	$y = (x^2 - 1) \operatorname{arctg} \frac{x^2 - 1}{x\sqrt{3}} - e^{\sqrt{x}}$
5.29	$y = 2x \operatorname{arcctg} \frac{\sqrt{x}}{\sqrt{x}+2} - \sqrt[3]{3x}$	5.30	$y = -x^2 \arccos \frac{x\sqrt{2}}{1+x} - \sqrt{2} \ln x$

### Задание № 26

Найдите производные данных функций

26.1	$y = \frac{1}{4\sqrt{5}} \ln \frac{2+\sqrt{5}thx}{2-\sqrt{5}thx}$	26.2	$y = \frac{shx}{4ch^4 x} + \frac{3}{8} \operatorname{arctg} shx$
26.3	$y = \frac{1}{2} \ln \frac{1+\sqrt{thx}}{1-\sqrt{thx}} - \operatorname{arctg} \sqrt{thx}$	26.4	$y = \ln \frac{\sqrt{2}+thx}{\sqrt{2}-thx} - \frac{thx}{4(2-th^2 x)}$
26.5	$y = \frac{1}{2} thx + \frac{1}{4\sqrt{2}} \frac{1+\sqrt{2}thx}{1-\sqrt{2}thx}$	26.6	$y = -\frac{1}{2} \ln th \frac{x}{2} - \frac{chx}{2sh^2 x}$
26.7	$y = \frac{2 \ln ch \sqrt{5x}}{sh^3 x} - \operatorname{arcsin} cthx$	26.8	$y = \frac{\sqrt{3} \operatorname{arctg} thx}{\ln sh^2 x} - sh^2 2x$
26.9	$y = \operatorname{arctg} \frac{\sqrt{shx}}{chx - shx}$	26.10	$y = \frac{1}{6} \ln \frac{1-shx}{2+shx}$
26.11	$y = \sqrt[4]{\frac{1+thx}{1-thx}}$	26.12	$y = \frac{\sqrt{7} sh^3 x}{1+chx}$
26.13	$y = \frac{ch^5 3x}{\sqrt{shx}}$	26.14	$y = \frac{\sqrt{3} th^3 x}{\sqrt{ch6x}}$
26.15	$y = \frac{1+8ch^2 x \ln chx}{2ch^2 x}$	26.16	$y = -\frac{12sh^2 x + 1}{3sh^3 x}$
26.17	$y = -\frac{shx}{2ch^2 x} + \frac{3}{2} \operatorname{arcsin}(thx)$	26.18	$y = \frac{1}{\sqrt{8}} \operatorname{arcsin} \frac{3+chx}{1+3chx}$
26.19	$y = \frac{1}{\sqrt{8}} \ln \frac{4+\sqrt{8}th(x/2)}{4-\sqrt{8}th(x/2)}$	26.20	$y = \frac{1}{4} \ln th \frac{x}{2} - \frac{1}{4} \ln \frac{3+chx}{shx}$

26.21	$y = -\frac{1}{4} \arcsin \frac{5+3chx}{3+5chx}$	26.22	$y = \frac{1-8ch^2x}{4ch^4x}$
26.23	$y = \frac{2}{shx} - \frac{shx}{2ch^2x} + \frac{5}{2} \operatorname{arctg} shx$	26.24	$y = \frac{8}{3} \operatorname{cth} 2x - \frac{1}{3chx sh^3x}$
26.25	$y = \frac{1}{2} \operatorname{arctg}(shx) - \frac{shx}{2ch^3x}$	26.26	$y = \frac{3}{2} \ln th \frac{x}{2} + chx - \frac{chx}{sh^2x}$
26.27	$y = \frac{shx}{2ch^2x} - \frac{1}{shx} - \frac{3}{2} \operatorname{arctg} shx$	26.28	$y = \frac{shx}{2\sqrt{chx}} + \frac{1}{2} \operatorname{arcctg}(shx)$
26.29	$y = \frac{1-2shx}{(1+chx)^2} + \sin^2 shx$	26.30	$y = \frac{3}{2} \cos^3(ch^2x) + \frac{1}{2} \ln thx^2$

**Задание № 27**  
Найдите производные данных функций

27.1	$y = (\operatorname{arctgx})^{(1/2) \ln \operatorname{arctgx}}$	27.2	$y = (\sin \sqrt{x})^{\ln \sin \sqrt{x}}$
27.3	$y = (\sin x)^{5e^x}$	27.4	$y = (\arcsin x)^{e^x}$
27.5	$y = (\ln x)^{3^x}$	27.6	$y = x^{\arcsin x}$
27.7	$y = (\operatorname{ctg} 3x)^{2e^x}$	27.8	$y = x^{e^{tgx}}$
27.9	$y = (\operatorname{tgx})^{4e^x}$	27.10	$y = (\cos 5x)^{e^x}$
27.11	$y = (x \sin x)^{8 \ln(x \sin x)}$	27.12	$y = (x-5)^{chx}$
27.13	$y = (x^3 + 4)^{tgx}$	27.14	$y = (x+1)^{\sin x^3}$
27.15	$y = (x^2 - 1)^{shx}$	27.16	$y = (x^4 + 5)^{ctg x}$
27.17	$y = (\sin x)^{5^{x/2}}$	27.18	$y = (x^2 + 1)^{\cos x}$