

# «Solution»

Lector is an Associate Professor

**Machekhina Ksenia Igorevna**

**(Мачехина К.И.)**

**E-mail:** [machekhinaKsu@tpu.ru](mailto:machekhinaKsu@tpu.ru)

# \* Lecture plan

1. Basic concepts
2. Methods for expressing the concentration of solutions
3. Theory of solutions
4. Thermodynamics of dissolution and solubility
5. Non-electrolytes solutions
6. Electrolyte solutions
7. The solubility products.
8. Constant of water ionization or ion product of water  $K_w$ .

# 1. Basic concepts

A dispersed system (DS) is a system in which one substance (**dispersed phase**) is evenly distributed in another (**dispersion medium**).

# 1. Basic concepts

## Types of dispersed systems

1. Spray

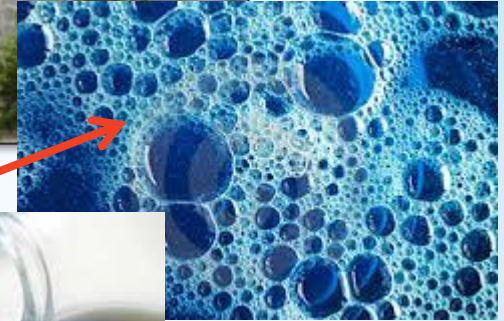
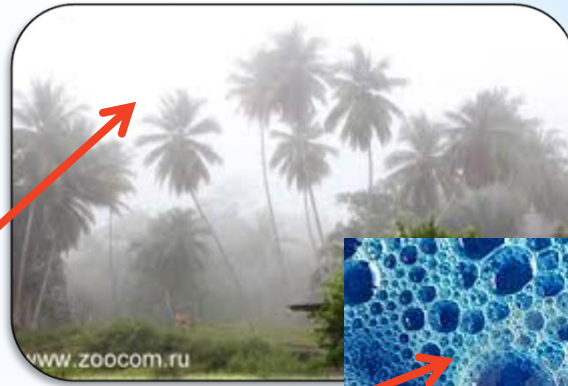
2. Foam

3. Emulsion

4. Sol

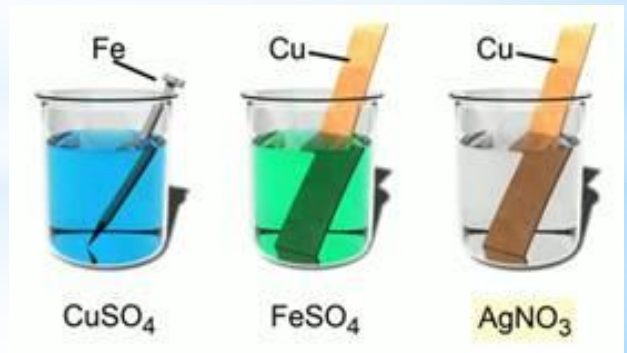
5. Solid emulsion

6. Gel



# 1. Basic concepts

- |                               |                           |
|-------------------------------|---------------------------|
| 1. Coarsely dispersed systems | $10^{-3} \div 10^{-5}$ cm |
| 2. Colloid systems            | $10^{-5} \div 10^{-7}$ cm |
| 3. True Solutions             | $10^{-7} \div 10^{-8}$ cm |





**«What solutions do you see in the picture?»**



# 1. Basic concepts

**Solution** is a single-phase, multi-component system of variable composition.

**Solvent** is a component that does not change the composition, taken in excess and in the same state of aggregation as the solution itself.

**Solute** is a component taken in deficiency and evenly distributed in a solvent.

# 1. Basic concepts

## 1. According to aggregate state

Solid



Liquid



Gaseous



## 2. According to the electrolytic dissociation of a solute

Electrolytes

Non-electrolytes



## 2. Methods for expressing the concentration of solutions

**Concentration** is the content of a solute per unit mass or volume of a solution or solvent.

**Mass share ( $\omega$ ), [%]** shows how many grams of solute B are contained in 100 g of solution.

$$\omega = \frac{m(B)}{m_p} \cdot 100\%$$

$m(B)$  is a mass of solute, g.

$m_{\text{solution}}$  is a mass of solution, g.

$$m_{\text{solution}} = V_{\text{solution}} \cdot \rho$$

## 2. Methods for expressing the concentration of solutions

**Molar concentration (C, C<sub>M</sub>, M), [mol/l]** shows how many moles of a solute are contained in 1 liter of solution.

$$C = \frac{m(B)}{M(B) \cdot V_p}$$

$m(B)$  is a mass of solute, g.;

$M(B)$  is a molar mass of solute, g/mol;

$V_{\text{solution}}$  is volume of solution, l.

## 2. Methods for expressing the concentration of solutions

**Molar concentration of substance equivalents (normality) ( $C_{\text{eq}}$ ,  $C_n$ ,  $n$ ), [mol/l]** shows how many mole equivalents of a solute are contained in 1 liter of solution.

$$C_{\text{ЭК}} = \frac{m(B)}{M_{\text{ЭК}}(B) \cdot V_p}$$

$m(B)$  is a mass of solute, g.;

$M_{\text{ЭК}}(B)$  is a molar equivalent mass of solute, g/mol;

$V_{\text{solution}}$  is a volume of solution, l.

## 2. Methods for expressing the concentration of solutions

**Titer (T), [g/ml]** shows how many grams of a solute are contained in 1 ml of a solution.

$$T = \frac{m(B)}{V_p}$$

$m(B)$  is a mass of solute, g;

$V_p$  is a volume of solution, ml.



## 2. Methods for expressing the concentration of solutions

**Molality ( $C_m$ ), [mol/kg]** shows how many moles of a solute are contained in 1 kg of solvent.

$$C_m = \frac{m(B) \cdot 1000}{M(B) \cdot m_s}$$

$m(B)$  is a mass of solute, g;

$M(B)$  is molar mass of solute, g/mol;

$m_s$  is a mass of solvent, g.

## 2. Methods for expressing the concentration of solutions

**Mole fraction ( $x$ )** shows the ratio of the mole of one of the components of the solution to the sum of the moles of all components of the solution.

$$x = \frac{n(B)}{\sum n_i}$$

$$\sum n_i = n(B) + n_1 + n_2 + \dots + n_i$$

# 3. Theories of solutions

## 1. Physical Theory

(Van't Hoff, Arrhenius)

## 2. Chemical Theory

(Mendeleev, Kablukov)

## 3. Modern Theory (Physico-Chemical)

# 3. Theories of solutions

## Modern Theory (Physico-Chemical)

1. Solutions have a uniform composition throughout the phase
2. The dissolution process is accompanied by volumetric and thermal effects.
3. Stoichiometric laws do not apply to solutions
4. Solutions have compositional variability



## 4. Thermodynamics of dissolution and solubility

Three steps of the dissolution process :

- 1. Phase transition** is the destruction of chemical and intermolecular bonds in a substance.
- 2. Solvation (for H<sub>2</sub>O hydration)** is the chemical interaction of a solvent and a solute with the formation of new compounds - solvates (hydrates)
- 3. Diffusion** is a uniform distribution of solvates throughout the volume of the solution

# 4. Thermodynamics of dissolution and solubility

Relative to balance

**"solution - soluble substance"**



unsaturated

$$\Delta G_{\text{dissolution}} < 0$$

saturated

$$\Delta G_{\text{dissolution}} = 0$$

supersaturated

$$\Delta G_{\text{dissolution}} > 0$$

## 4. Thermodynamics of dissolution and solubility

**Solubility** is the ability of a substance to dissolve in a given amount of solvent.

A measure of the solubility of a crystalline substance is the concentration of its saturated solution.

**The solubility coefficient** is the mass of a solute that dissolves under given conditions in 100 g of water to form a saturated solution.

# 4. Thermodynamics of dissolution and solubility

## Factors affecting solubility:

### 1) nature of the components::

1. “like dissolves in the underground” (interaction energies);
2. hydrogen forces;
3. van der Wals forces.

### 2) temperature (Le Chatelier's principle);

### 3) pressure (Henry's law)

$$s = k \cdot P$$

where  $s$  – solubility of gas,  $P$  – pressure,  $k$  – Henry’s constant.



## 5. Solutions of non-electrolytes

- \* **Ideal solutions** are solutions the formation of which is not accompanied by volumetric and thermal effects.
  
- \* **Colligative properties** are properties that do not depend on the nature of the solute, depending on the concentration :
  1. Saturated steam pressure
  2. Boiling and freezing point
  3. Osmotic pressure

## 5. Solutions of non-electrolytes

### Saturated vapor pressure of the solvent over the solution

The dissolution of a substance in a liquid will cause a decrease in the saturation vapor pressure of the solvent.

#### Denote:

- \*  $P^{\circ}$  is saturated vapor pressure of a solvent over a pure solvent;
- \*  $P_1^{\circ}$  is saturation vapor pressure of the solvent over the solution;
- \*  $X_1$  – mole fraction of solvent;
- \*  $X_2$  – mole fraction of solute.

## 5. Solutions of non-electrolytes

### **Raoult's first law:**

«The saturation vapor pressure of a solvent over a solution is equal to its pressure over a pure solvent multiplied by the mole fraction of the solvent»

$$P_1^0 = P^0 \cdot \chi_1$$

## 5. Solutions of non-electrolytes

### **Raoult's first law:**

«The relative decrease in the pressure of the saturated vapor of the solvent over the solution is equal to the mole fraction of the solute»

$$\frac{P^0 - P_1^0}{P^0} = \chi_2$$



## 5. Solutions of non-electrolytes

$$\chi_2 = \frac{\frac{m_2}{M_2}}{\frac{m_1}{M_1} + \frac{m_2}{M_2}}$$

1 is a solvent

2 is a solute

## 5. Solutions of non-electrolytes

1. The boiling point ( $T_{\text{boil}}$ ) of the solution is higher than the boiling point of the solvent.
2. The freezing point (crystallization) ( $T_{\text{zam.}}$ ) of the solution is below the freezing point of a pure solvent.

## 5. Solutions of non-electrolytes

### **Raoult's second law:**

«An **increase in boiling point** and a **decrease in freezing point** of dilute solutions of non-electrolytes are proportional to the **molality of the solutions**»

## 5. Solutions of non-electrolytes

$$\Delta T_{\text{кип}} = K_{\text{э}} \cdot C_m$$

$$\Delta T_{\text{зам}} = K_{\text{к}} \cdot C_m$$

$C_m$  is molality of solution;

$K_{\text{э}}$  is ebullioscopic solvent constant;

$K_{\text{к}}$  is solvent cryoscopic constant.

$$K_{\text{э}} (H_2O) = 0,52$$

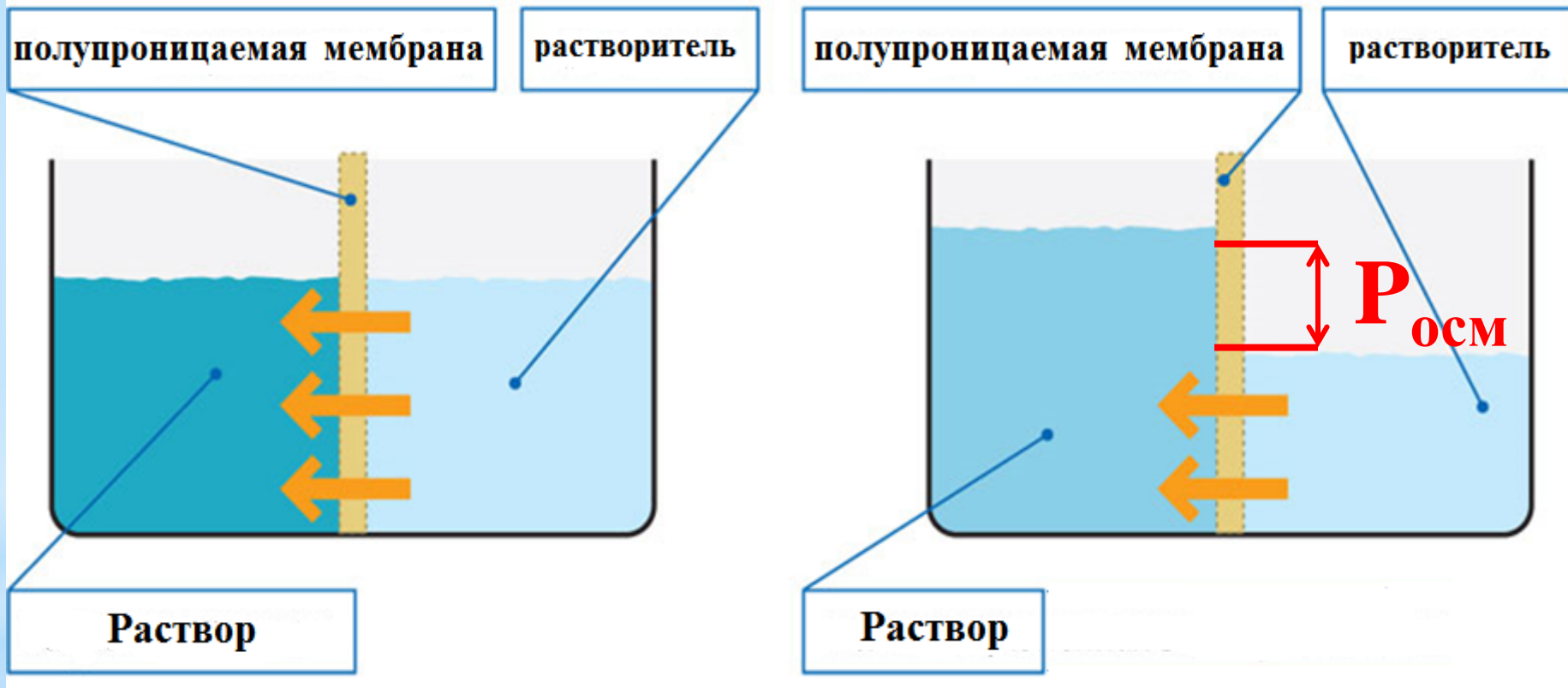
$$K_{\text{к}} (H_2O) = 1,86$$

## 5. Solutions of non-electrolytes

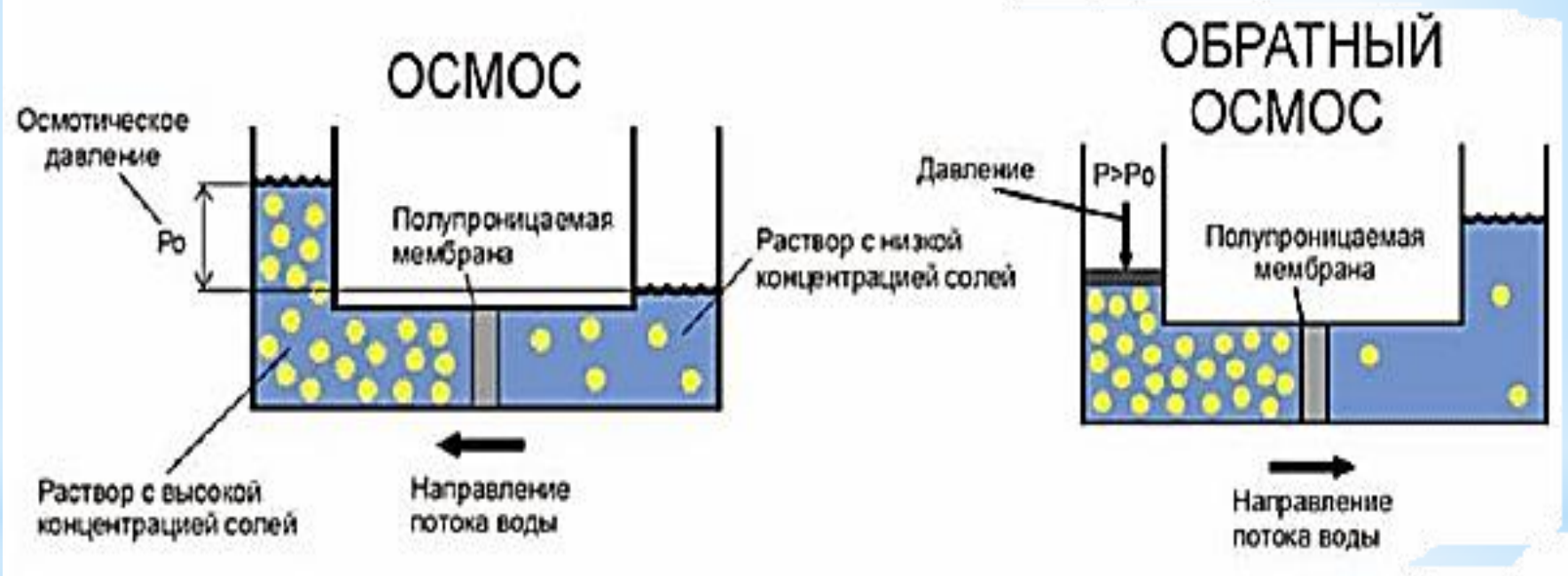
### Osmotic pressure

**Osmosis** is the phenomenon of one-way diffusion through a semi-permeable partition separating a solution and a pure solvent or two solutions of different concentrations.

## ОСМОС







## 5. Solutions of non-electrolytes

**Osmotic pressure** is the pressure that must be applied to suppress osmosis.

Van't Hoff :

$$P_{ocm} = C \cdot R \cdot T$$

C is the molar concentration of the solution, mol/L;

R is the universal gas constant, J/mol·K;

T is the absolute temperature, K.

## 6. Electrolyte solutions

**Electrolytic dissociation** is the process of disintegration of a substance into ions upon dissolution.

**Electrolytes** are substances capable of dissociating in solutions or melts into ions.

### Proof

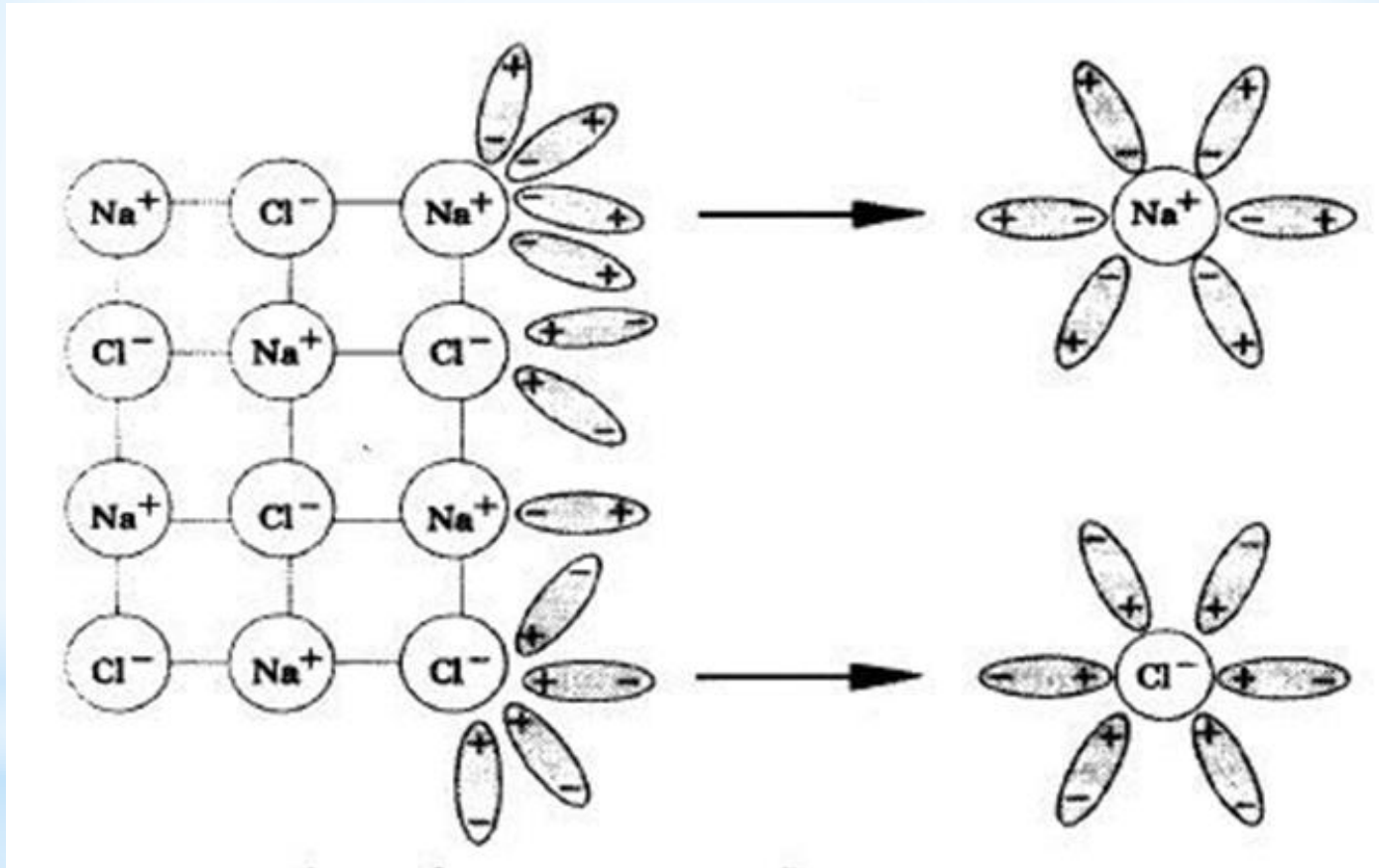
1. Electrical conductivity of solutions of electrolytes.
2. Deviation from the laws of Raoult and van't Hoff

## **6. Electrolyte solutions**

### **Theory of electrolytic dissociation (S. Arrhenius, 1887)**

1. Electrolytes in solutions dissociate (break down) into ions.
2. Dissociation is a reversible process, therefore the law of mass action applies to the dissociation process.
3. Electrolyte solutions are electrically conductive.

## 6. Electrolyte solutions



## 6. Electrolyte solutions

### Dissociation constant



$K_{\text{д}} \geq 10^{-2}$  - strong electrolytes,

$K_{\text{д}} < 10^{-2}$  - weak electrolytes.



## 5. Electrolyte solutions

**The degree of dissociation ( $\alpha$ )** is the ratio of the number of dislocated molecules to the total number of molecules.

$$\alpha = \frac{N_{\text{дис}}}{N_{\text{общее}}}$$

*Degree of dissociation ( $\alpha$ ):*

$\alpha < 0,03$  (less 3%) is weak electrolyte

$0,03 < \alpha < 0,3$  (3-30%) is medium strength electrolytes

$\alpha > 0,3$  (more 30%) is strong electrolyte

## 6. Electrolyte solutions

For weak electrolytes  $\alpha \rightarrow 0$ , a  $(1 - \alpha) \rightarrow 1$  From here :

$$\alpha = \sqrt{\frac{K_D}{C}}$$

C is molar concentration of electrolyte, mol/l

**Ostwald's law of dilution:** the degree of dissociation of a weak electrolyte increases with dilution of the solution

## 6. Electrolyte solutions

### Factors affecting the degree of dissociation :

1.  $\alpha$  depends on the concentration of the solution.
2.  $\alpha$  depends on T.
3.  $\alpha$  depends on the presence of similar ions in the solution.

## 6. Electrolyte solutions

### Strong electrolytes:

1) all soluble salts;

2) strong bases - alkalis (from metals I, II group of the main subgroup) **EXCEPT** Mg(OH)<sub>2</sub> and Be(OH)<sub>2</sub>:



3) strong acid:



## 6. Electrolyte solutions

Weak electrolytes	Strong electrolytes
<p><b>1 Weak bases:</b> NH<sub>4</sub>OH, Zn(OH)<sub>2</sub>, Mn(OH)<sub>2</sub>, Al(OH)<sub>3</sub>, Fe(OH)<sub>2</sub></p> <p><b>2) Weak acids:</b> H<sub>2</sub>S, H<sub>2</sub>CO<sub>3</sub>, H<sub>3</sub>BO<sub>3</sub>, H<sub>2</sub>SiO<sub>3</sub>, HCN, HClO, HBrO, HIO, CH<sub>3</sub>COOH, HNO<sub>2</sub>, H<sub>2</sub>O<sub>2</sub>.</p>	<p><b>1) almost all soluble salts;</b></p> <p><b>2) Strong bases:</b> NaOH, KOH, Ba(OH)<sub>2</sub>; RbOH, LiOH</p> <p><b>3) Strong acids:</b> HCl, HBr, HI, HNO<sub>3</sub>, H<sub>2</sub>SO<sub>4</sub>, HClO<sub>3</sub>, HClO<sub>4</sub>, HMnO<sub>4</sub>, H<sub>2</sub>CrO<sub>4</sub>.</p>

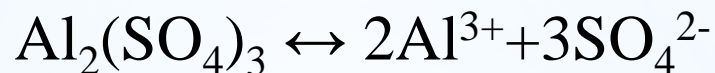
# 6. Electrolyte solutions

Электролиты		Неэлектролиты ( $\alpha=0$ )
Сильные электролиты ( $\alpha \approx 1$ )	Слабые электролиты ( $\alpha \ll 1$ )	
1. Растворимые соли (в т.ч. соли органических кислот)	1. Слабые кислоты, в т.ч. органические (НСООН, HNO <sub>2</sub> и др.)	1. Оксиды, не взаимодействующие с водой
2. Сильные кислоты (НСl, HI и др.)	2. Нерастворимые основания и гидроксид аммония NH <sub>4</sub> OH	2. Простые вещества
3. Щелочи (NaOH, KOH и др.)	3. Некоторые малорастворимые и нерастворимые соли.	3. Большинство органических веществ



## 6. Electrolyte solutions

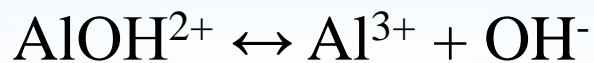
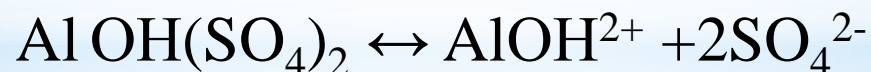
1. Soluble medium salts dissociate completely in **1 step**.



2. Acids and bases dissociate **in steps**.



3. Acid and basic salts dissociate **in steps**.



## 6. Electrolyte solutions

$$i = \frac{\Delta P_{\text{опыт}}}{\Delta P_{\text{выч}}} = \frac{\Delta T_{\text{кип(опыт)}}}{\Delta T_{\text{кип(выч)}}$$

**i** is the isotonic coefficient showing how many times the concentration of particles in a solution is greater than the number of dissolved molecules.

$$i = \frac{n_{\text{экспер.}}}{n_{\text{теор.}}}$$

## 6. Electrolyte solutions

$$\alpha = \frac{i - 1}{n - 1}$$

$n$  is a the number of ions into which a substance dissociates in solution.

## 6. Electrolyte solutions

$$\Delta P = i \cdot P_0 \cdot x(B)$$

$$\Delta T_{\text{кун}} = i \cdot K_{\text{э}} \cdot C_m$$

$$\Delta T_{\text{зам}} = i \cdot K_{\text{к}} \cdot C_m$$

$$P_{\text{осм}} = i \cdot C \cdot R \cdot T$$

## 7. Solubility product



$$K_c = \frac{[\text{Ba}^{2+}] \cdot [\text{SO}_4^{2-}]}{[\text{BaSO}_4]}$$

$$[\text{BaSO}_4] = \text{const}$$

$$[\text{BaSO}_4] \cdot K_c = \text{IP} = [\text{Ba}^{2+}] \cdot [\text{SO}_4^{2-}] = 1,1 \cdot 10^{-10}$$

## 8. Ionic product of water( $K_w$ )



$$\text{By } 25^\circ\text{C} \quad K_d = 1,8 \cdot 10^{-16}$$

$$K_d = \frac{[\text{H}^+] \cdot [\text{OH}^-]}{[\text{H}_2\text{O}]}$$

$$K_d \cdot [\text{H}_2\text{O}] = [\text{H}^+] \cdot [\text{OH}^-]$$

Water concentration  $[\text{H}_2\text{O}] = 1000 / 18 = 55,56 \text{ mol/l}$ .

$$K_w = [\text{H}^+] \cdot [\text{OH}^-] = K_d \cdot [\text{H}_2\text{O}] = 1,8 \cdot 10^{-16} \cdot 55,56 = 10^{-14}$$

$$K_B = [\text{H}^+] \cdot [\text{OH}^-] = 10^{-14}$$



# 8. Ionic product of water

**pH value** characterizes the concentration of hydrogen cations in solution

$$pH = -\lg[H^+]$$

**pOH** is hydroxyl index characterizes the concentration of OH<sup>-</sup> ions in solution

$$pOH = -\lg[OH^-]$$

$$pH + pOH = 14$$

Value pH	Medium
pH < 7	acidic
pH = 7	neutral
pH > 7	alkaline

# 8. Ionic product of water

## Indicators of acidity of aqueous solutions

Indicator	Transition interval pH	Color	
		acid medium	Alkaline medium
litmus	5 ÷ 8	Red	Blue
phenolphthalein	8,3 ÷ 10,0	Colorless	Magenta
methyl violet	0 ÷ 3	Yellow	Blue
methyl orange	3,1 ÷ 4,4	Red	Yellow

## Home task № 1.

1. A solution containing 100 g of  $\text{H}_2\text{SO}_4$  in 150 ml of water is prepared. Please, calculate the mass fraction of acid in solution (%).

## Home task № 2.

1. The crystallization temperature of a 15% solution of glycerin  $C_3H_8O_3$  ( $K_k (H_2O) = 1.858$ ) is \_\_\_\_\_  $^{\circ}C$ .
2. (Give your answer to the nearest hundredth).