

“QUANTUM MECHANICS / PROFESSIONAL ENGLISH STUDY”

COLLOQUIUM 1

*Developed by  
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**Wave-particle duality.**

1. The quantum light theory.
2. The wave properties of electrons. Phase velocity. Group velocity and wave packets.

**Schroedinger Equation.**

1. Hamilton-Jacobi equation.
2. Wave-equation for electrons.  $\psi$  -function.
3. Linear operators.

**Schroedinger Equation solutions.**

1. Stationary states. General solution. Statistical manner of wavefunction.
2. Discrete and continuous energy spectrum of operators.
3. Square potential well.
4. Free particle.
5. Born method.
6. Dirac's delta-function.
7. Normalisation of eigenfunctions of continuous-spectrum operators.
8. Solution of Poisson equation for charged particle.

**Schroedinger equation solution.**

1. Method of classical boundary approximation.
2. Barrier tunneling.
3. The ejection of electrons from the metal. Cold emission
4. Alpha-decay. The concept of quasilevels (quasi-discrete spectrum).

**Statistical properties of quantities.**

1. Mean values in quantum physics. Quantum Poisson brackets.
2. Indetermination relations.
3. Ehrenfest's theorems.

**Harmonic oscillator.**

1. Eigenvalues and eigenfunctions.
2. Matrix representation. Coordinate and momentum matrix elements.
3. Annihilation-creation operators representation for harmonic oscillator.

**Representation theory.**

1. Vector-state representation. Different operator representations.
2. Transformation of representations. Harmonic oscillator solution in momentum representation.
3. Heisenberg and Schroedinger representations.
4. Matrix representation.

## Additional questions

1. Estimation of wavepacket life-time for electron.
2. Fundamental consequences for physical quantities with noncommuting operators.
3. Conservation laws in quantum theory.
4. Classical approach for quantum systems.
5. Complete set of physical quantities of a system.
6. Complementary principle.
7. Probability density in quantum theory.
8. Momentum distribution function in quantum theory.
9. Degenerate quantum state.
10. Complete set of eigenfunctions. Theorem formulation.
11. Definition of coordinate representation for wavefunctions and operators.
12. Normalisation of eigenfunctions of continuous spectrum operator.
13. Parity of harmonic oscillator eigenfunctions.
14. Zero-energy of harmonic oscillator.
15. Heisenberg indeterminacy relations for adjoint coordinate and momentum. Fourth indeterminacy condition. Fundamental meaning of indeterminacy relations.
16. Definition of stationary states.
17. Eigenfunction parity for particle in square well potential.
18. Number of particles operator.
19. Matrix representation of coordinate in the basis of harmonic oscillator.
20. Momentum operator and coordinate operator in momentum representation.
21. Classical approximation breakdown.
22. The difference in Heisenberg and Schrödinger representation for operators and wavefunctions.
23. Matrix representation: solution of Schrödinger equation.
24. Orthonormalization equality for eigenfunctions of discrete spectrum operator.